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# ATOMIC SPECTRA

 $In\ two\ volumes$ 

VOLUME II

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# ATOMIC SPECTRA

# AND THE VECTOR MODEL

 $\mathbf{BY}$ 

#### A C. CANDLER

Sometime Scholar of Trinity College, Cambridge

'There is one thing I would be glad to ask you When a mathematician engaged in investigating physical actions and results has arrived at his own conclusions, may they not be expressed in common language as fully, clearly and definitely as in mathematical formulae? If so, would it not be a great boon to such as we to express them so—translating them out of their hieroglyphics that we also might work upon them by experiment?

Letter from Michael Faraday to Clerk Maxwell

VOLUME II
COMPLEX SPECTRA

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# CONTENTS

# VOLUME II. COMPLEX SPECTRA

Chap. XII	Displaced terms	page 1
XIII	Combination of several electrons	ξ
XIV	Short periods	21
$\mathbf{x}\mathbf{v}$	Long periods	45
XVI	Rare earths	75
XVII	Intensity relations	90
XVIII	Sum rules and (jj) coupling	122
XIX	Series limit	158
$\mathbf{X}\mathbf{X}$	Hyperfine structure	166
XXI	Quadripole radiation	215
, XXII	Fluorescent crystals	228
$App \ \mathrm{V}$	Key to references	247
VI	Bibliography	248
	A Books of reference	248
	B The spectra of the elements	248
	C The hyperfine structure of the element	s 261
Subject inde	rac	267
Author inde	x	275

# LIST OF PLATES

5	Fluorescent spectrum of a chromium phosphore and a multiplet from the	
	iron arc	facing page 62
6	Absorption spectra of two samarium compounds	86
7.	Hyperfine structure of various lines	168
8	Fluorescent spectra of samarium and a multiplet from the iron arc	240

#### CHAPTER XII

#### DISPLACED TERMS

#### 1. The alkaline earths

Only about half of the bright lines of the calcium are spectrum are accounted for by the simple terms described in a previous chapter. Most of the remaining lines, however, can be explained by the 'dashed' or 'displaced' terms introduced by Gotze\* in 1921, terms which Russell and Saunders† were later to attribute to the activity of two electrons (Fig. 12.2).

As an example of these terms consider the group of six bright lines occurring round 4300 A

l'erms	7 417		2 *1'3'		2 40,7
2 41.	d		4280 JBS (30) 23300 SBS		
2 414	1307 7 98 (45) 23207 53	47 23	52 20 4298 989 (30) 23254 76	HI 77	1283 008 (30) 23341 63
2 *P.			105 H5 131H H4H (15) 231 IN 91	жн 75	105-87 1302 525 (80) 23235-86

Fig. 12.1. Wave lengths and wave numbers of the 2.3P -2.3P multiplet of calcium. The numbers in brackets are intensities.

The intervals 52·2 and 105 0 are recognised as the intervals of the well known 2 <sup>3</sup>l' terms and these terms are therefore written in the left hand column. The intervals 47·2 and 86·8 do not occur in the earlier analysis, but Landó's interval rule suggests that an empirical ratio of 1·84 should arise from a <sup>3</sup>l' term, for the ideal interval ratios of <sup>3</sup>l' and <sup>3</sup>l' terms are 2 and 1·5 respectively.

If the combinations not observed are those forbidden by the J selection rule, then the empirical terms must have J values of 0, 1 and 2. Of the nine possible combinations, two are then forbidden because they have  $\Delta J > 2$ , and a third because the electron

- Gotze, AP, 1921, 68 285. A key to letters used in referring to periodicals is given in Appendix 19.
- † Russell and Saunders, AJ, 1925, 61 38. The authors write the terms 1 °P and 1 °P instead of 2 °P and 2 °P used here.

would have to jump from J=0 to J=0 The intersystem line  ${}^{3}P_{0} \rightarrow {}^{1}S_{0}$  is noticeably absent in the mercury spectrum

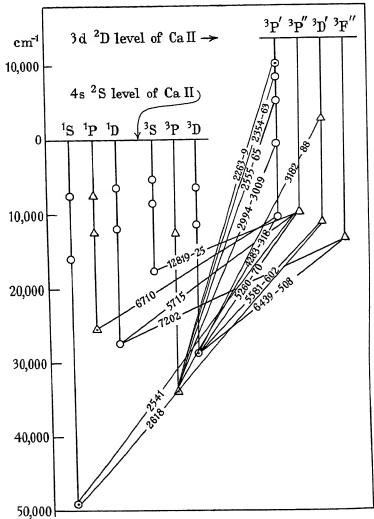


Fig 12 2 Level diagram of calcium, extended to show the displaced terms Even terms are shown by a circle, odd terms by a triangle

A critic might suggest that the above argument really only determines the values of J, but the Zeeman effect has also been examined and this, connecting as it does L, J and S, serves to fix L, when J and S are known Every indication therefore

suggests that the empirical terms should be written <sup>4</sup>P, or, since they are not of the usual <sup>4</sup>P series, <sup>5</sup>P'.

So far no use has been made of the series laws, but five terms of the <sup>3</sup>P' series have been observed, and if these are fitted to a Rydberg formula, they indicate that the limit of the series is some 13961 cm. <sup>4</sup> above the common limit of the earlier known series of the calcium atom. Indeed, the 4 <sup>4</sup>P', 5 <sup>4</sup>P' and 6 <sup>4</sup>P' terms are all above the limit, and contain energies of 0-68, 1 03 and 1-24 volts in excess of that required to ionise the atom. This surprisingly large energy content seems to be open to only one explanation. In the levels of this displaced series two electrons are excited, and when the atom returns to one of the normal states both electrons jump and both contribute energy to a single quantum of radiation.

This deduction may be still further refined. The second deepest term \*D of the calcium ion is 13711 cm<sup>-1</sup> or 1·72 volts above the basic \*S term, and this is not very different from the amount by which the limit of the D' series is raised above the normal limit. If then the two optical electrons are assumed to have orbital moments  $l_1$ ,  $l_2$ ,  $l_4$  must be assigned the value 2.

The difficulty of explaining why the P' terms combine with normal P terms is then surmounted by the hypothesis that  $\mathbf{1}_1$  and  $\mathbf{1}_2$  combine vectorially to give a resultant  $\mathbf{L}$ .  $\mathbf{L}$  combines in the usual way with  $\mathbf{S}$  itself the sum of the  $\mathbf{s}_1$ ,  $\mathbf{s}_2$  of the individual electrons, to give  $\mathbf{J}$ , but the quantum transitions allowed depend on  $\mathbf{1}_1$ ,  $\mathbf{1}_2$  individually and only indirectly on  $\mathbf{L}$ . The reasons already given for writing the unknown term  $^4\mathbf{P}'$  first determine  $\mathbf{J}$ , and then require L to be  $\mathbf{1}$ , but  $l_2$  is still unassigned. If the old rule  $\Delta L = \frac{1}{4}\mathbf{1}$  is to be written now  $\Delta l_2 = 1$ , then the fact that the  $^3\mathbf{P}'$  term combines with a P term shows that  $l_2$  is 0 or 2, and the former is ruled out, because if  $\mathbf{1}_1 + \mathbf{1}_2$ .  $\mathbf{L}$  it is inconsistent with the previous allotment of L and  $l_1$ .

Apply the same arguments to a so called <sup>3</sup>D' term found by Russell and Saunders, which has the J properties of a D term but combines with <sup>3</sup>D, <sup>1</sup>S and <sup>4</sup>D. Clearly the J properties indicate  $I_{\ell-2}$ , while the combining terms show that  $I_{2}=1$ , and as the <sup>3</sup>D' series has the same displaced limit as the <sup>3</sup>P' series,  $I_1$  is 2.

When two electrons are excited, the atom as a whole can no longer be said to have a chief quantum number, though each electron has Thus in the normal state of calcium, two electrons he outside the closed shell of argon, and these occupy 4s orbits, so that the ground state is  $4s^2 \, ^1S_0$  When one of these moves to a 4p orbit the configuration becomes  $4s \, 4p \, ^3P$ , this is the  $2 \, ^3P$  term of the normal spectrum. In the lowest  $^3P'$  term both electrons have moved to 3d orbits, so that the configuration is  $3d^2 \, ^3P'$ .

Often the chief quantum number does not need to be stressed, and then 3d<sup>2</sup> <sup>3</sup>P' is abbreviated to d<sup>2</sup> <sup>3</sup>P', or if the two d electrons have different chief quantum numbers, as in 3d 4d <sup>3</sup>P', then we write d d <sup>3</sup>P' Again as there is only one 3d nd <sup>3</sup>P series, the omission of the dash introduces no ambiguity, but in fact it is often retained as it gives a key to the transitions permitted

What are these? Or in other words, what is the selection rule governing the combination of displaced terms? Heisenberg stated, on the basis of the quantum mechanics, that when two electrons jump simultaneously one is bound by the condition  $\Delta l_1 = \pm 1$  and the second by  $\Delta l_2 = 0$  or  $\pm 2$  Of this rule the transitions from the displaced to the normal terms of the alkaline earths offer a first example

A very important consequence of this selection rule is that when an atom emits or absorbs a quantum of radiation the sum of the orbital quantum numbers of the individual electrons  $\Sigma l$  must change by an odd number, if the sum was even it must become odd, or if it was odd it must become even. Consequently all possible terms may be divided into two groups, an even group, written in accord with the suggestion of a number of physicists†  $S,P,D,\ldots$ , and an odd group, written  $S^\circ,P^\circ,D^\circ$ . A term of the one group can then combine only with a member of the other group.

Another notation adopted for several years by many spectroscopists differed somewhat from this The even group of terms

<sup>\*</sup> The 3d<sup>3</sup> <sup>3</sup>P' term is the 3 <sup>3</sup>P' term of this description, though the 3 <sup>3</sup>P', 4 <sup>3</sup>P' and 5 <sup>3</sup>P' terms arise from 3d nd configurations, the 2 <sup>3</sup>P' term arises from 4p<sup>2</sup>, it was wrongly assigned by Russell and Saunders

<sup>†</sup> Russell, Shenstone and Turner, PR, 1929, 33 900

was written S, P', D, F', . and the odd series S', P, D', F, This notation was convenient because it was in agreement with the notation of the earlier chapters of this book and could be extended But to-day it seems more important to be able to distinguish odd and even terms at sight, for the group to which an empirical term belongs can easily be determined, and this the dashed notation does not facilitate

In simple spectra only one electron is excited, and for it the S, D terms have L even, while the P, F terms have L odd, and so to be quite accurate should be written P°, F° Again, the displaced P′, D′ terms of Ca I have the sum  $(l_1+l_2)$  equal to 4 and 3 respectively, so that they are  $d^{2}$  and p  $d^{3}$ D°

Having dealt with two displaced series at considerable length, the other series found by Russell and Saunders, and written  $^3P''$ ,  $^3D''$  and  $^3F''$ , can be considered more briefly. All the series have the same elevated limit and consequently in every state one electron must occupy a d orbit. The double dash signified that these terms, unlike  $^3P'$  and  $^3D'$ , do not combine with the normal terms of the same letter. Thus  $^3P''$ , though it has the J properties of a P term, combines with  $^3S$ ,  $^3D$ ,  $^1S$ ,  $^1D$ , so that L=1 and  $l_2=1$   $^3P''$  is therefore identical with d p  $^3P^\circ$  and may be written in the latter form. Similarly,  $^3D''$  combines with  $^3P$ ,  $^1P$  and therefore must be identical with  $^2D$  Combinations of  $^3F''$  are known only with  $^3D$  and  $^1D$ , for combinations with  $^3S$  lie too far on the infrared and  $^3G$  is wholly unknown, but the energy of the term argues strongly in favour of d p  $^3F$  and against d f  $^3F$ , though the evidence here adduced allows the latter

Russell and Saunders in their analysis accounted for practically all the known lines of the three alkaline earths, though they hesitated to assign electronic states to all the terms which were suggested by the term differences, and whose energies were thus known Wentzel,\* however, has filled even this small gap, and the analysis of the visible and near ultra-violet region of calcium may be considered complete

#### 2 Beryllium and magnesium

In the spectra of beryllium and magnesium, and in the iso-

<sup>\*</sup> Wentzel, ZP, 1925, 34 730

electronic spark spectra B II to O v and Al II to Cl vI, there occur a striking group of five lines, the separations are nearly equal, and four of the five lines are of equal intensity, the central line of the group, however, is noticeably stronger, and in some spectra it may be resolved into two close components

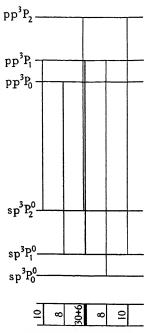


Fig 12.3 Structure of a displaced triplet of magnesium, this arises in a  $3p^2~^3P{\to}3s~3p~^3P^\circ$  transition

In 1925 Bowen and Millikan showed that these arise by the combination of the s p  $^3$ P° term with a  $^3$ P term, having so nearly he same intervals that the lines  $^3$ P $_2 \rightarrow ^3$ P $_2$ ° and  $^3$ P $_1 \rightarrow ^3$ P $_1$ ° often coincide. According to Sommerfeld's intensity rule, this central line is due to chief lines having  $\Delta J = \Delta L$ , while the other four lines are satellites of the first order. A more accurate theory would predict the intensities shown in Fig. 12.3. Both are in good agreement with observation

The wave-lengths and wave-numbers of the central line in spectra isoelectronic with magnesium are shown in Fig 124\*

<sup>\*</sup> Bowen and Millikan, PR, 1925, 26 150

The differences show how accurately linear is the progression of frequency with atomic number, and this means that the group of lines follows the irregular doublet law, which they can do only if the transitions take place between levels having the same chief quantum number

This argument applies as well to Be as to Mg, though figures are here adduced only for the latter. But in Be the jump ends in a 2s 2p orbit, so that it must start in a 2p<sup>2</sup> orbit, no other possibility exists, for there are no 2d orbits. The close similarity of

Spectrum	λ	ν	Dıff
Mgı	2780 64	35962 96	20727 9
Alm	1763 95	56690 9	20727 9
Sı mı	1298 93	76986 <del>4</del>	
Pıv	1030 53	97037 1	20050 7
Sv	854 81	116985 6	19948 5
Cl vi	730 31	136928 2	19942 6

Fig 12.4 The central line of displaced triplets in spectra isoelectronic with magnesium

the lines in Mg and Be suggests that in Mg too the  $^3P$  term arises from the  $3p^2$  configuration, and this hypothesis is confirmed, when the frequency of the arc line  $p^2 P \to s^3 P^\circ$  is compared with the spark line  $p^2 P \to s^2 S$ , the former is 35960 cm  $^{-1}$  and the latter 35760 cm  $^{-1}$ , so that both must surely arise in the same electron transition  $2p \to 2s$ 

A comparison of these displaced terms with those found in the alkaline earths shows that in Be and Mg the lines are produced by one electron jumping, whereas in Ca, Sr and Ba two electrons jump simultaneously. But in both alike the displaced terms arise from the second lowest term of the spark spectrum

#### 3. Zinc, cadmium and mercury

Displaced terms have also been identified in Cd by Ruark\* and in Zn and Hg by Sawyer†, but instead of the six lines to be expected four only have been found, these being interpreted as

<sup>\*</sup> Ruark, JOSA, 1925, 11 199

<sup>†</sup> Sawyer, JOSA, 1926, 13 431

the combination of the low s  $p^3P^{\circ}_{0,1,2}$  terms with the displaced terms  $p^2^3P_{0,1}$  (Fig. 12 5)

Whether the  $p^2 {}^3P_2$  term is really missing or whether, as Foote, Takamine and Chenault\* have suggested, it coincides with  $p^2 {}^3P_1$ ,

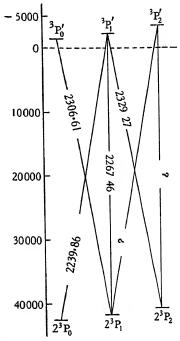


Fig 12.5 Level diagram showing a PP' triplet of cadmium, this arises as 5p²  $^3P\!\to\!5s$  5p  $^3P^o$ 

so that in Cd the 2329 A and 2268 A lines are really narrow doublets, remains a question still undecided. Certainly the intensities are somewhat irregular and the 2329 A line is much stronger than the other lines.

#### BIBLIOGRAPHY

These displaced spectra are fully discussed by Grotrian, Graphische Darstellung der Spektren, 1928, 1 188–210

\* Foote, Takamine and Chenault, PR, 1925, 26 174

#### CHAPTER XIII

#### COMBINATION OF SEVERAL ELECTRONS

#### 1 Combination of unlike electrons

The coupling of orbital and spin vectors, found to explain the displaced terms of the alkaline earths, gives also an adequate account of the terms of many more complex spectra

In this coupling the orbital and spin vectors of the electrons, commonly written  $\mathbf{l_1}$ ,  $\mathbf{l_2}$ ,  $\mathbf{s_1}$ ,  $\mathbf{s_2}$ , first combine to resultants  $\mathbf{L}$  and  $\mathbf{S}$  respectively, and then  $\mathbf{L}$  and  $\mathbf{S}$  combine to form  $\mathbf{J}$  The problem therefore is to determine all the values of L and S to which a given electron configuration can give rise, to solve this

Electron added	State of 10n							
	S	P	D	F				
S	S	P	D	F				
р	P	SPD	PDF	DFG				
d	D	PDF	SPDFG	PDFGH				

Fig 131 Atomic states resulting from the addition of an electron to an ion

problem, consider the orbital and spin vectors separately When a p and a delectron combine the l vectors are 1 and 2, so that their resultant must be 1, 2 or 3, values which correspond to P, D or F terms, further, each electron has a spin vector of  $\frac{1}{2}$ , so that the atomic spin vector due to two electrons may be 0 or 1, values which correspond to multiplicaties of 1 and 3 Accordingly, a p and a delectron combine to form six terms  $^{1}P$ ,  $^{1}D$ ,  $^{1}F$ ,  $^{3}P$ ,  $^{3}D$  and  $^{3}F$ 

A similar train of reasoning will determine the terms produced when an electron combines with an ion, for if an s electron is to be added to an ion in the <sup>4</sup>F state, the orbital vectors to be combined are 0 and 3, so that the resultant must be 3, while the s vectors are  $\frac{1}{2}$  and  $1\frac{1}{2}$ , so that the resultant may be 1 or 2, accordingly the terms produced are <sup>3</sup>F and <sup>5</sup>F Fig 13 1 summarises the results obtained in this way, for it shows the terms arising when an s, p

or d electron is added to an ion in the S, P, D or F state, the multiplicity being omitted since it always increases and decreases by unity

When three or more electrons have to be combined together, the work must proceed by steps, two electrons being combined and then the third added to each of the terms produced by the two Thus an spd configuration would give rise to the nine terms <sup>2</sup>(PDF), <sup>2</sup>(PDF) and <sup>4</sup>(PDF)

In the above discussion the word 'term' is used to denote a multiplet term, but in analysis each component of the multiplet appears as a separate empirical level or 'term' Theory thus states precisely how many levels will arise from a given configuration,

$M_L$ $m_l$	-2	-1	0	1	2
1	-1	0	1	2	3
0	-2	-1	0	1	2
-1	-3	-2	-1	0	1
Term of atom	F	D	P		

Fig 13.2 Addition of a p electron to an ion in the D state, showing how P, D and F states result

and what their J values will be, and it is an outstanding achievement of the theory that the empirical terms occur in just the number predicted and have the J values assigned. Sometimes, as might be expected, some of the levels are missing, but they are nearly always levels which would produce only lines of low intensity. In the great mass of spectra so far analysed, there is only a single level which seems to be adequately substantiated and is surplus to the theory, it is found in Pd I

Though the above method of combining two electrons is the simplest, another method due to Russell\* is not without interest Instead of combining the  $l_1$  and  $l_2$  vectors of ion and electron, combine the  $m_{l_1}$  and  $m_{l_2}$  values, all combinations are permitted,

<sup>\*</sup> Russell, PR, 1927, 29 782.

so that a matrix of  $(2l_1+1)(2l_2+1)$  values results, and this can be split into a number of sequences by Breit's alleys, exactly as in the theory of the Paschen-Back effect. Fig. 13 2 shows the calculation when a p electron is added to an ion in a D state

The same method can be used to combine the  $m_{s_1}$  and  $m_{s_2}$  of ion and electron to obtain the multiplicity of the atomic terms

#### 2 Combination of equivalent electrons

Two electrons having the same values of n and l are said to be 'equivalent'

When two equivalent electrons are to be combined, the above argument gives all the terms which might be produced, but it gives more than are produced, for the combination is restricted by Pauli's exclusion principle Of this complication the simplest example is the combination of two electrons in the alkaline earths, thus in magnesium the two valency electrons must have  $n \ge 3$ , since the first two groups are full, and so the lowest terms may be expected to arise from the combination of two 3s electrons s electrons, however, always have  $m_i = 0$ , so that if Pauli's exclusion principle is to be satisfied and the two electrons are not to occupy the same orbit,  $m_s$  must be  $+\frac{1}{2}$  for one and  $-\frac{1}{2}$  for the other Consequently  $M_s = 0$  and S = 0, showing that the lowest term is <sup>1</sup>S<sub>0</sub> and that a <sup>3</sup>S term can appear only when the two s electrons producing it have different chief quantum numbers Thus Pauli's exclusion principle clearly explains why the 13S<sub>1</sub> term is missing in all the alkaline earth spectra and the <sup>3</sup>S<sub>1</sub> sequence begins with a 2 3S1 term

$l_1$	$l_2$	$m_{l_1}$	$m_{l_2}$	$m_{s_1}$	$m_{s_2}$	$M_L$	$M_S$	Term
0	0	0	0	1/2	$-\frac{1}{2}$	0	0	1S

Fig 13.3 Combination of two equivalent's electrons, showing that only a  $^1\mathrm{S}$  term results

Fig 13 3 shows the argument summarised in a table A similar table for two equivalent p electrons appears in Fig 13 4

In this table all possible combinations of  $m_{l_1}$  and  $m_{l_2}$  are included, but the two electrons are to be considered interchange-

able, so that  $m_{l_1} = 1$  and  $m_{l_2} = 0$  is identical with  $m_{l_1} = 0$  and  $m_{l_2} = 1$  Further, the derivation of the terms, from the sums  $M_L$ and  $M_S$  needs to be explained A <sup>1</sup>D term has L=2 and S=0, so that it will give rise to a series of values of  $M_{\scriptscriptstyle L}$  from 2 to -2 all

$egin{bmatrix} l_1 & l_2 \ \hline \end{pmatrix}$	$m_{l_1}$ $m_{l_2}$	$m_{s_1}$ $m_{s_2}$	$M_L$	$M_S$	Terms
1 1	$ \begin{array}{cccc} 1 & 1 & \\  & 0 & \\  & -1 & \\ 0 & 0 & \\  & -1 & \\  & -1 & -1 & \\ \end{array} $	- 12-12-12-12-12-12-12-12-12-12-12-12-12-1	2 1 0 0 -1 -2	1 0 0 -1 1 0 0 -1 1 0 0 -1 1 0 0 -1	<sup>1</sup> D <sup>3</sup> P <sup>1</sup> S

Fig 134 Combination of two equivalent p electrons, showing how the resulting terms are calculated

having  $M_S = 0$  To work from  $M_L$  and  $M_S$  to L and S therefore, start with the highest value of  $M_{\scriptscriptstyle L}$  available, namely 2 in the above figure, and cross out both a series of values of  $M_{\scriptscriptstyle L}$  from 2 to -2 and the corresponding values of  $M_s$ , namely 0 When these values have been deleted, the table of Fig 13 4 reduces to that shown in Fig. 13 5

$M_L$	$M_{\it B}$	Terms
1 0	1 0 -1 1 0 -1	3P
-1	1 0 -1	18

Fig. 13.5. A step in the elucidation of the previous figure, the  $M_L$  and  $M_S$  values which remain when the <sup>1</sup>D term has been removed

Now repeat the operation The highest value of  $M_L$  is 1, and the greatest corresponding values of  $M_s$  also 1, so that the next term to be written in the margin must have L=1 and S=1, and the values to be deleted are  $M_L=1$ , 0, -1 and  $M_S=1$ , 0, -1Afterwards there remains only  $M_L = 0$  when  $M_S = 0$ , representing a <sup>1</sup>S term

The calculation of terms arising from three equivalent p electrons introduces no new principles, the work, summarised in Fig 13 6, shows that the terms to be expected are <sup>2</sup>D, <sup>2</sup>P and <sup>4</sup>S The combination of four equivalent p electrons is worked out in Fig. 13.7. The terms arising, be it noted, are those arising from two equivalent p electrons, and indeed this could have been predicted. For six p electrons form a closed group, in which every orbit permitted by the exclusion principle is occupied, and consequently  $M_L = M_S = 0$ . Therefore when there are four p electrons, the orbits left unoccupied will be precisely those

$l_{1}$	$l_2$	$l_3$	$m_{l_1}$	$m_{l_2}$	$m_{l_3}$	$m_{s_1}$	$m_{s_2}$	$m_{g_8}$	Mz	$M_{\it S}$	Terms
1	1	1	1	1	ō	1/2	-1	±\frac{1}{2}	2	± ½	<sup>2</sup> D
			0	0	-1	1 2	- ½	土泉	1	土	2P
			-1	-1	1	21	$-\frac{1}{2}$	土地	-1 -1	土章	
		Ш	1	0	0 -1	±½	士皇	土量	-2 0	±½ ±½ ±½ ±½	<b>4</b> S

Fig 13 6 Combination of three equivalent p electrons

$l_1$ $l_2$ $l_3$ $l_4$	$m_{l_1}$ $m_{l_2}$ $m_{l_3}$ $m_{l_4}$	$m_{g_1} \ m_{g_2} \ m_{g_3} \ m_{g_4}$	$M_L$	$M_{S}$	Terms
1 1 1 1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		2 1 0 0 -2 -1	1 0 0 -1 0 1 0 0 -1 1 0 0 -1 1 0 0 -1	1D

Fig 13 7 Combination of four equivalent p electrons

$l_1$	$l_2$	$l_{3}$	$l_4$	$l_5$	$l_6$	$m_{l_1}$	$m_{l_2}$	$m_{l_8}$	$m_{l_{\bullet}}$	$m_{l_5}$	$m_{l_{\epsilon}}$	$m_{s_1}$	$m_{s_2}$	$m_{s_3}$	m <sub>84</sub>	$m_{s_5}$	$m_{S_6}$	Mz	$M_S$	Term
1	1	1	1	1	1	1	1	0	0	-1	-1	1/2	-1/2	1/2	-1/2	1/2	- 1/2	0	0	1S

Fig 13 8. Combination of six equivalent p electrons

occupied by two electrons, and the values of  $M_L$  and  $M_S$  will be unaltered in magnitude. The change in sign will not affect the values of L and S or consequently the terms. For the same reasons five p electrons give rise to a  $^2\mathrm{P}$  term just as one electron does

The terms resulting from various numbers of p electrons are collected together in Fig. 13 9, while below are similar tables for d and f electrons. Of these, the first two were given by Hund and the last by Gibbs, Wilber and White \* To save space terms of the same multiplicity are sometimes bracketed together, thus <sup>4</sup>P <sup>4</sup>F is abbreviated to <sup>4</sup>(PF), and the number of times a particular term occurs is indicated by a figure written directly below the letter

Number of p electrons		Terms	resulting	g
0 or 6 1 or 5 2 or 4 3	<sup>1</sup> S <sup>1</sup> D	2P2D	\$P	<b>4</b> S

Fig 139 Terms resulting from the combination of equivalent p electrons

No of d electrons		Terms	
0 or 10	1S		
1 or 9	$^{2}D$		
2 or 8	¹(SDG)	3(PF)	
3 or 7	<sup>2</sup> (PDFGH)	4(PF)	
4 or 6	$^{1}(\stackrel{\mathbf{SDFGI}}{\underset{2}{2}})$	³(PDFGH)	⁵D
5	<sup>2</sup> (SPDFGHI) <sup>3</sup> <sup>2</sup> <sup>2</sup>	(PDFG)	6S

Fig 13 10 Terms resulting from the combination of equivalent d electrons

No of f electrons		Terms		
0 or 14	1 <u>S</u>			
1 or 13	3E			
2 or 12	1(SDGI)	<sup>8</sup> (PFH)		
3 or 11	PDFGHIKL)	(SDFGI)		
4 or 10	1(SDFGHIKLN)	<sup>3</sup> (PDFGHIKLM) <sup>8 2 4 3 4 2 2</sup>	<sup>5</sup> (SDFGI)	
5 or 9	<sup>2</sup> (PDFGHIKLMNO) 457675582	4(SPDFGHIKLM)	<sup>6</sup> (PFH)	
6 or 8	<sup>1</sup> (SPDFGHIKLMNQ) <sup>4</sup> <sup>6</sup> <sup>4</sup> <sup>8</sup> <sup>4</sup> <sup>7</sup> <sup>8</sup> <sup>4</sup> <sup>2</sup> <sup>2</sup>	*(PDFGHIKLMNO)	5(SPDFGHIKL)	7F
7	<sup>2</sup> (SPDFGHIKLMNOQ) <sup>2571010897542</sup>	4(SPDFGHIKLMN)	<sup>8</sup> 2 8 2 2 <sup>6</sup> (PDFGHI)	88

Fig 13 11 Terms resulting from the combination of equivalent f electrons

### 3 Deep terms of the short periods

If the terms of low energy arise from electrons of low energy then the deep terms of the short periods must be derived from

<sup>\*</sup> Gibbs, Wilber and White, PR, 1927, 29 790

equivalents and p electrons. Moreover, they can be read off from Fig. 13-9, for a closed shell contributes nothing to L or S, so that the terms which arise from an  $s^2p^n$  configuration are precisely those which would arise from  $p^n$ 

The elucidation of these deep terms is important, because a few terms often give the key to the whole spectrum, and transitions ending in deep terms yield the brightest lines

Ou	ter electi	deep Ground Other deep			Some spectra in which these terms		
Total	otal s p		term	terms	have been found		
1 2 4	1 2 2 2	1 2	<sup>2</sup> S <sup>1</sup> S <sup>2</sup> P <sup>3</sup> P	  	Nai, Csi, Caii, Aliii Mgi, Cai, Alii, Ciii Ali, Tli, Cii, Niii Ci, Pbi, Nii, Oiii		
5 6 7 8	2 2 2 2 2	3 4 5 6	4S *P 2P 1S	<sup>2</sup> D <sup>2</sup> P <sup>1</sup> D <sup>1</sup> S —	N 1, Sb 1, O 11, Cl 111 O 1, Se 1, Cl 11, A 111 F 1, Cl 1, A 11, Na 111 Ne 1, Kr 1, Na 11, Ca 111		

Fig 13 12 Low terms of the short periods

#### 4 Two energy rules

In the spectra of the short periods the deep terms are few in number, and so those predicted by theory are easily matched with those found empirically. But of the higher terms very many will arise from a single configuration, and to know which of these normally lie low and which high is a great help to the accurate labelling of the empirical terms. This problem was first studied by Hund, who solved it in two empirical energy rules.

The first rule states that those terms he deepest in which the electronic spin vectors are parallel to one another, and in which therefore S is a maximum. Thus in the alkaline earths, the triplet term arising from any electronic configuration has deeper than the corresponding singlet term, while in the short periods Fig. 13-12 shows that of the terms arising from the simplest electron configuration that of highest multiplicity is the ground term.

The second rule adds that of terms which have the same multiplicity, those lie deepest in which the electronic orbital vectors are also parallel, and in which therefore L is a maximum.

Accordingly, in carbon  $^1\!D$  hes lower than  $^1\!S$ , and in nitrogen  $^2\!D$  hes lower than  $^2\!P$ 

Thus of two terms arising from a set of equivalent electrons, that which lies furthest to the right in Figs 13 9–13 11 lies deepest in the spectrum. These rules never fail to predict the ground term of a spectrum correctly, but among higher configurations many exceptions occur.

#### 5. Inverted terms

When a group of electrons is more than half full the deep terms arising from it are inverted. Thus the <sup>2</sup>P ground term of Ali is erect, but the <sup>2</sup>P ground term of Cli is inverted, the <sup>3</sup>P ground term of silicon is erect, but that of oxygen is inverted.

This fact is best examined in the light of a third energy rule, which asserts that the deepest components of a term arise when the orbital and spin vectors of the electrons are anti-parallel. When there are no restrictions this rule ensures that in the lowest component J will be a minimum and the terms will therefore be erect, but when the group is more than half full the restrictions imposed by the exclusion principle interfere

The ground terms of the elements of a short period may be built up graphically by adding one electron at a time. The first electron, having its 1 and s vectors anti-parallel, as shown in Fig. 13-13, gives rise to a  ${}^{2}P_{1}$  term. On adding the second electron the first energy rule makes  $\mathbf{s}_{2}$  parallel to  $\mathbf{s}_{1}$ , and would make  $\mathbf{l}_{2}$  parallel to  $\mathbf{l}_{1}$  if the exclusion principle did not interfere, but equivalent electrons may not have the same values of  $m_{l}$  if they already have the same values of  $m_{s}$ , so if  $m_{l_{1}}$  was -1,  $m_{l_{2}}$  must be 0 or 1, and of these 0 will give the lower component since it will make the vectors more nearly anti-parallel, accordingly, in Fig. 13-13 the  $\mathbf{l}_{2}$  vector is drawn horizontal

The addition of a third electron emphasises no new principle, but the fourth, if it is to produce the empirical term, must set its orbital vector 1 anti-parallel not to the resultant S but to the electronic vector  $s_4$  The lowest component then appears as  $^3P_2$ , and as the other components of the ground term are  $^3P_1$  and  $^3P_0$  the term appears inverted.

This theory, which can of course be applied also to d and f electrons (Fig 13 14), explains well enough why the ground terms

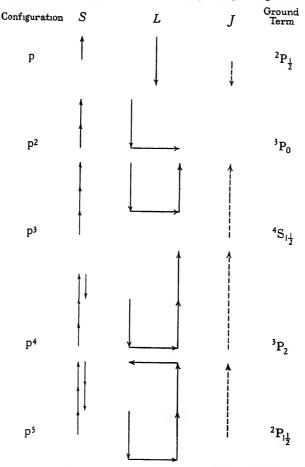


Fig  $13\,13$  Vector diagram showing how the ground terms of a p shell may be derived with the help of the Pauli exclusion principle

of certain spectra are inverted, but it would not necessarily lead one to expect that many of the higher terms would also be inverted as in fact they are A theory developed by Goudsmit,\* serves however to bring out this point

CASII

<sup>\*</sup> Goudsmit, PR, 1928, 31 946 Ruark and Urey, Atoms, molecules and quanta, 1930, 332

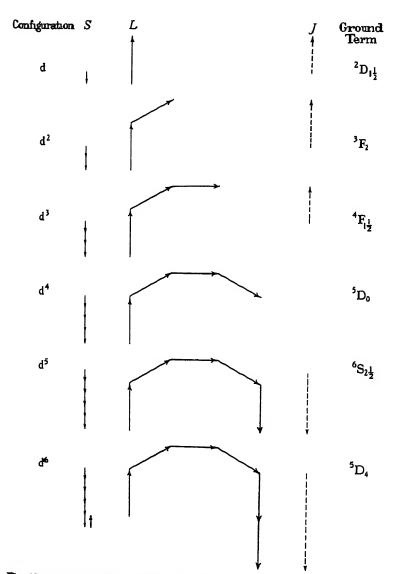


Fig 13 14 Vector diagram showing how the ground terms of a d shell may be derived.

Previously, the wave-number of a component of a multiplet term has been written  $E/hc = \nu_{\rm G} + \Gamma$ , (4 1)

Where  $\nu_{G}$  is the wave-number of the centroid Let us assume that When several electrons are active the atomic displacement  $\Gamma$  is itself the sum of electronic displacements  $\gamma_{1}, \gamma_{2}, \dots, \gamma_{n}$ 

In the vector model the energy of an electron having orbital and spin vectors  $l_1$ ,  $s_1$  is assumed proportional to them and to the cosine of the angle between them, so that

$$\gamma_1 = a_1 l_1 s_1 \cos \left( l_1 s_1 \right) \tag{13.1}$$

Now  $l_1$  precesses round L and  $s_1$  round S, so that

$$\gamma_1 = a_1 l_1 \cos(\mathbf{l}_1 \mathbf{L}) s_1 \cos(\mathbf{s}_1 \mathbf{S}) \cos(\mathbf{LS}),$$

Or summing for all the electrons,

$$\Gamma = \Sigma \gamma_1 = \cos(\mathbf{LS}) \sum a_1 l_1 \cos(l_1 \mathbf{L}) s_1 \cos(s_1 \mathbf{S})$$
 (13 2)

In order to advance beyond this equation, Slater\* had to make a further postulate, the electrons are to be divided into two groups according as their spin vectors are parallel or anti-parallel to the atomic spin vector, the resultants L' and L'' of the corresponding orbital vectors are then 'action variables', which interpreted in terms of the vector model means that they must both be integral

Consider now the  ${}^3P$  ground term of an element, such as oxygen, with four p electrons. Three of these will have s parallel to S, while one will be anti-parallel. Clearly then L'' = 1, while L' might assume any value less than 3 did the exclusion principle not instervene, requiring that if all three electrons have the same value of  $m_s$ , then they can none of them have the same value of  $m_l$ , consequently, when S' is  $1\frac{1}{2}$ , the only possible value of L' is zero  $\mathbb{E}$  quation (13 1) now reduces to

$$\Gamma = as \cos (\mathbf{LS}) (L' - L''), \tag{13.3}$$

for if all electrons are equivalent  $a_1 = a_2 = a_n$  and all may be written a

This formula accounts for the empirical facts So long as a shell is less than half full  $\Gamma$  will be positive and the terms erect, but

20 COMBINATION OF SEVERAL ELECTRONS [CHAP XIII when there are present three p, five d, or seven f electrons, L'=L''=0, and the ground term will be an S term of multiplicity one greater than the number of electrons present. When a shell is more than half full L', but not L'', is zero, so that  $\Gamma$  is negative and the terms are inverted

A very pretty confirmation of this theory is found in nitrogen, most of whose terms arise from the  $2p^{23}P$  configuration of N II and are consequently erect, two deep terms, however, a  $^4P$  and a  $^2P$ , are inverted, and it seems clear that these have the electronic structure 2s  $2p^4$ \*

#### BIBLIOGRAPHY

The consequences of Russell and Saunders' paper and the Pauli exclusion principle were first developed by Hund in Linienspektren und periodisches Systems der Elemente, 1927, more recent accounts appear in Ruark and Urey, Atoms, molecules and quanta, 1930, Pauling and Goudsmit, The structure of line spectra, 1930

\* Compton and Boyce, PR, 1929, 33 147

#### CHAPTER XIV

#### ELEMENTS OF THE SHORT PERIODS

#### 1 Elements to be considered

The seventh from last element of each period has a <sup>1</sup>S ground term, and this may be taken to mean that the configuration of each of these elements consists only of complete shells, the last six elements of each period shown in Fig. 14·1, are therefore

Column	III	IV	V	VI	VII	VIII
Configuration	p	p²	p <sup>3</sup>	p <sup>4</sup>	p <sup>5</sup>	p <sup>6</sup>
Elements	B Al Ga In Tl	C S1 Ge Sn Pb	N P As Sb Bı	O S Se Te Po	F Cl Br I	Ne A Kr Xe Nt
Ground term	²P	\$P	4S	³P	<sup>2</sup> P	18
Prominent multiplicities	2	1, 3	2, 4	3, 5	2, 4	1,3

Fig 14 l Elements arising from configurations of p electrons

formed by the entrance of six electrons into a new shell, the sixth electron completing the shell and forming the mert gas. As this shell must consist of p electrons in the first short period, it presumably consists of p electrons in the other periods

If this is true, then the partly filled shell of p electrons should produce the ground term of each spectrum, the terms being  ${}^{2}P$ ,  ${}^{3}P$ ,  ${}^{4}S$ ,  ${}^{3}P$ ,  ${}^{2}P$ ,  ${}^{1}S$  in successive columns, and in fact these are the terms found. Of the higher terms the great majority are formed by adding an electron to the ground term of the ion Consider, for example, the spectrum of carbon in which there are only two p electrons, the ground term of C II is  ${}^{2}P$ , and accordingly CI should consist of singlets and triplets, the terms produced being  ${}^{1}P$  and  ${}^{3}P$ ,  ${}^{1}(SPD)$  and  ${}^{3}(SPD)$ , or  ${}^{1}(PDF)$  and  ${}^{3}(PDF)$ , according as the second electron moves in an s, p or d orbit. And similarly in column VI the ground term of the spark spectrum is  ${}^{4}S$ , so that the arc spectrum should consist chiefly of the resulting

triplets and quintets, though some less prominent terms may arise by the addition of an electron to the metastable states  $p^{3}$  <sup>2</sup>P and  $p^{3}$  <sup>2</sup>D of the ion

#### 2 Irregularities and their cause

In the early days of spectrum analysis, spectroscopists were able to order only those spectra in which series are prominent, for a series was the only regularity which they had recognised To-day, the spectroscopist who has analysed a spectrum into a complex of terms can name those terms only if they exhibit some regularity, and the regularities on which he chiefly relies are the selection rules, which serve to determine J, the magnetic splitting factor, and the intensity and interval rules. The three last are linked together, for when a spectrum fails to obey one rule, it often fails to obey all three, and in terms of the vector model this is taken to mean that the coupling of the vectors ceases to be that postulated by Russell and Saunders

What then are the influences which make a term irregular? Briefly they may be summarised as three, first is an increase in atomic number, carbon is more regular than lead, and neon than krypton, secondly, the column of the periodic table is significant, for the spectra of the elements on the left-hand side are more regular than those on the right, beryllium is more regular than nitrogen and nitrogen than neon, while third stands the height or energy of a term, for the higher a term lies the less likely is it to obey the simple rules, and particularly the interval rule. These influences are here stated as empirical rules, their explanation will be attempted only in a later chapter.

### 3. The earth metals, s2p configuration\*

The spark spectra of the earth metals, like the spark spectra of the alkalis, have a <sup>1</sup>S ground term, so that the arc spectra should consist of doublets, and in fact a system of doublets has been found and analysed into principal, sharp, diffuse and fundamental series. Where the terms have been resolved they have been shown

<sup>\*</sup> Grotman, Graphische Darstellung der Spektren, 1928, 1 122f and 2 80, 96

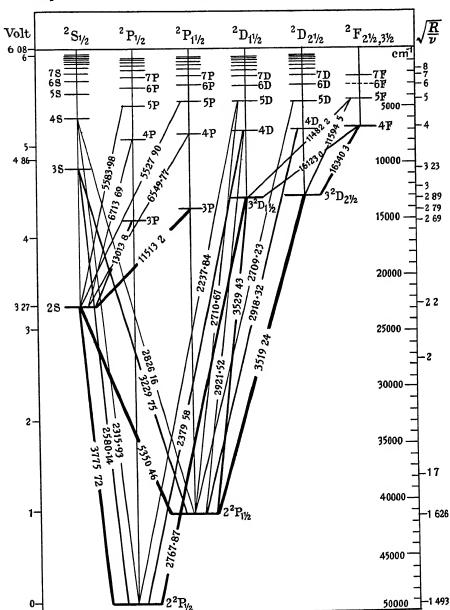


Fig 14.2 Level diagram of thallium (After Grotrian, Graphische Darstellung der Spektren)

to be usually erect, in Pb II, however, the  $^2\mathrm{D}$  and  $^2\mathrm{F}$  terms are inverted

The ground term is clearly a P term, for the principal series extends into the infra-red and has a limit of much greater wavelength than the limits of the sharp and diffuse series (Fig. 14.2), in this the doublets of the earth metals may be compared to the triplets of the alkaline earths. Moreover, the absorption spectra confirm the ground term, for when the metallic vapour is maintained at a low temperature, and illuminated with white light, the sharp and diffuse series are absorbed, but not the principal series

Al	п	Alı						
$l_1 \ l_2$	Term	$l_3$	Ter	l <sub>1</sub> l <sub>2</sub> l <sub>3</sub>				
382	18	3p	2]	<sup>2</sup> P°				
		4s 4p 3d 4f	2/ 2] 2] 2]	s <sup>2</sup> s s <sup>2</sup> p s <sup>2</sup> d s <sup>2</sup> f				
3s 3p	3s 3p <sup>3</sup> P°		4P	<sup>2</sup> (SPD)	$sp^2$			
		4s 4p 3d	4P° 4(SPD) 4(PDF)°	<sup>2</sup> P° <sup>2</sup> (SPD) <sup>2</sup> (PDF)°	sp s sp p sp d			
3p²	3P	3p	4S°	<sup>2</sup> P° <sup>2</sup> D°	p <sup>3</sup>			

Fig 14 3 Terms predicted in column III

Above the ground term of Aliles first an S and then a D term, and theory makes it clear that these arise by the addition of 4s and 3d electrons to the <sup>1</sup>S ground term of Alil Terms of the arc spectrum may, it is true, arise from spark terms other than <sup>1</sup>S, but they do not belong to the simple doublet system, in practice these terms do not produce bright lines in the elements of column III A, but they appear lying quite low in all the spark and higher spark spectra, which are isoelectronic with this column, such as Siii and Sbiii The structure of these terms is shown in Fig. 14.3

# 4. Column IV, s2p2 configuration

In the fourth column Hund's scheme predicts that the  $s^2p^2$  configuration will produce five low terms  $^3P_{0,1,2}$ ,  $^1D_2$  and  $^1S_0$  in

that order proceeding from the ground term up, and empirically in carbon, silicon, germanium, tin and lead five low terms have been found

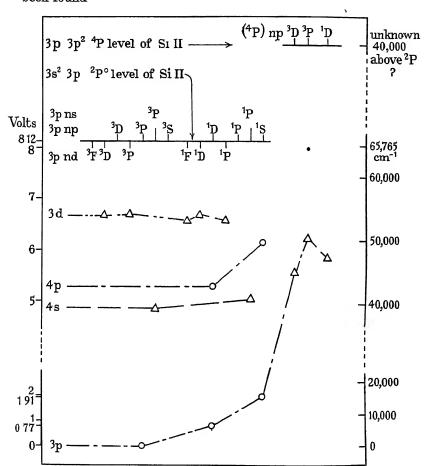


Fig 14.4 Level diagram of silicon. In this and the following diagrams, even terms are shown by a circle and odd terms by a triangle. Terms produced by the same electron are joined by a broken line, when the electron is an s electron the line is drawn — —, when a p electron — - — and when a d electron — - —

In the region extending from the red end of the spectrum down to  $2000\,\mathrm{A}$  the carbon arc produces only one line,  $2478\,\mathrm{A}$ , but when a trace of carbon dioxide is added to helium at a pressure

of 20 to 30 mm many lines occur which have been attributed to the neutral carbon atom. Analysis of the spectrum shows that the reason why the visible lines are difficult to excite is that they arise between high terms, the low terms produce lines in the ultra-violet, and these occur quite readily both in the arc and in vacuum tubes containing carbon compounds

C	п			С1				
$l_1 l_2 l_3$	$l_1 l_2 l_3$ Term $l_4$			Terms				
2s <sup>2</sup> 2p	2P°	2p	³P	1D	18	s <sup>2</sup> p <sup>2</sup>		
		3s 3p 3d	<sup>3</sup> (SPD) <sup>3</sup> (PDF)°		<sup>1</sup> P° <sup>1</sup> (SPD) <sup>1</sup> (PDF)°	s <sup>2</sup> p s s <sup>2</sup> p p s <sup>2</sup> p d		
2s 2p <sup>2</sup>	<sup>4</sup> P <sup>2</sup> (SPD)	2p	5S°	³(SPD)°	¹(SD)°	sp <sup>3</sup>		
	<b>4</b> P	3s 3p 3d	<sup>5</sup> P <sup>5</sup> (SPD)° <sup>5</sup> (PDF)		\$P \$(SPD)° \$(PDF)	sp² s sp² p sp² d		
	2D	3s 3p	<sup>8</sup> D <sup>8</sup> (PDF)°		<sup>1</sup> D <sup>1</sup> (PDF)°	sp² s sp² p		
	<sup>2</sup> P	3s 3p	³P ³(SPD)°		<sup>1</sup> P (SPD)°	sp <sup>2</sup> s sp <sup>2</sup> p		
	<sup>2</sup> S	3s 3p	3P°		<sup>1</sup> S <sup>1</sup> P°	sp² s sp² p		

Fig 145 Terms predicted in column IV

The CI spectrum arises from the  $^2\mathrm{P}$  ground term of CII and has been analysed quite regularly into a number of triplets and singlets, in contrast PbI has been analysed only into series. To understand this better, consider the changes which occur in the  $\mathrm{s}^2\mathrm{p}^2$  and  $\mathrm{s}^2\mathrm{p}$  s configurations with increasing atomic number. Thus in CI the  $^3\mathrm{P}$  ground term has nearly the ideal interval ratio of the Russell-Saunders coupling, while the extreme interval is small compared with the distance which separates the  $^3\mathrm{P}$  from the  $^1\mathrm{D}$  term. From this ideal the low terms of SiI, GeI and SnI fall further and further away until in lead  $\Delta^3\mathrm{P}_{01}$  is greater than  $\Delta^3\mathrm{P}_{12}$ , while the extreme triplet interval  $\Delta^3\mathrm{P}_{02}$  is as great as the separation of the  $^3\mathrm{P}_2$  and  $^1\mathrm{D}_2$  terms (Fig. 14.6)

Again examine the intervals of the s<sup>2</sup>p s configuration which produces a <sup>3</sup>P and <sup>1</sup>P term, in carbon the extreme interval of the <sup>3</sup>P term is only 60 cm <sup>-1</sup>, while 1500 cm <sup>-1</sup> separates <sup>3</sup>P<sub>2</sub> from <sup>1</sup>P<sub>1</sub>,

	С	Sı	Ge	Sn	Pb
$^{3}P_{0}^{-3}P_{1}$ $^{3}P_{1}^{-3}P_{2}$ $^{3}P_{2}^{-1}D_{2}$ $^{1}D_{2}^{-1}S_{0}$	14 8 27 5 10,150 11,452	77 1 146 1 6075 5 9095 4	557 1 852 8 5716 0 9241 2	1692 1736 5185 8550	7,817 2,831 10,818 8,000
$\Delta^{3}P_{1}_{2}/\Delta^{3}P_{0}_{1}$	1 86	1 90	1 53	1 02	0 36

Fig 14 6 Column IV Intervals in the ground configuration, s<sup>2</sup>p<sup>2</sup>

but in tin the triplet and singlet are transformed into two diads, having intervals of only 300 and 600 cm<sup>-1</sup>, but separated from one another by 4000 cm<sup>-1</sup> (Fig. 14.7)

	С	Sı	Ge	Sn	Pb
<sup>3</sup> P <sub>0</sub> - <sup>3</sup> P <sub>1</sub> <sup>3</sup> P <sub>1</sub> - <sup>3</sup> P <sub>2</sub> <sup>3</sup> P <sub>2</sub> - <sup>1</sup> P <sub>1</sub>	20 40 1589	77 195 1037	251 1415 903	274 3714 628	327 —
$\Delta^3 P_0$ 2 $\Delta^2 P_{\frac{1}{2} 1\frac{1}{2}}$ of ion	60 64	272 287	1666 1768	3988 4253	14,071

Fig 14.7 Column IV Intervals in the lowest s2p s configuration

These changes run parallel to the increasing interval of the  ${}^{2}P$  ground term of the spark spectrum, and the relation between the two may be explained in terms of the vector model, provided that the separation of two terms is assumed roughly proportional to the strength of the coupling producing it. This assumption is indeed implicit in the description of regular terms already given, for if, to fix ideas, the two p electrons of CI are considered, the triplet and singlet terms are found widely separated, a fact which the vector model translates to read that the spin coupling  $(\mathbf{s_1}\mathbf{s_2})$  is strong, or again the two singlet terms are also widely separated, and so the orbital coupling  $(\mathbf{l_1}\mathbf{l_2})$  must also be supposed strong, but the intervals of the  ${}^{3}P$  term are small and so the coupling responsible, namely  $(\mathbf{LS})$ , must be weak

Consider then the addition of an electron to an ion specified by L, S and J, if the coupling is Russell-Saunders, the coupling of

 $_{i}$ L and  $_{i}$ S must be split when the electron is added, and only after  $_{i}$ L has combined with 1 and  $_{i}$ S with s may their resultants L and S combine together to form an atomic resultant J In symbols, the coupling then appears as

$$\{(_{\imath}\mathbf{Ll})(_{\imath}\mathbf{Ss})\} = \{\mathbf{LS}\} = \mathbf{J}$$

And this theory may be expected to yield a satisfactory account of the facts, so long as the  $({}_{\iota}\mathbf{L}_{\iota}\mathbf{S})$  coupling is weak, that is, so long as the interval of the spark ground term is small, a condition satisfied in carbon but not in tin. In contrast, when  $({}_{\iota}\mathbf{L}_{\iota}\mathbf{S})$  is strong, we obtain a more satisfactory account of the term scheme by considering the ionic and electronic vectors permanently coupled to  ${}_{\iota}\mathbf{J}$  and  ${}_{\mathsf{J}}$  respectively, then the splitting is produced by the strong coupling  $({}_{\iota}\mathbf{L}_{\iota}\mathbf{S})$  and the weak coupling  $({}_{\iota}\mathbf{J}\mathbf{J})$ , so that in Sn i the  $\mathbf{s}^2$  p s configuration produces not a triplet and a singlet but two diads

This new coupling is commonly referred to as (jj) coupling, being written symbolically as

$$(_{\imath}\mathbf{L}_{\imath}\mathbf{S})(\mathbf{ls}) = (_{\imath}\mathbf{J}_{\mathbf{I}}) = \mathbf{J}$$

It is characterised by strong inter-system lines, and in fact these are easily discovered in lead and can be traced greatly weakened in intensity back to silicon, but there is still a little doubt about the three lines found by Jog\* in CI, for if the lines found are those sought, the singlet term values assigned by Fowler must be changed by no less than 667 cm  $^{-1}$ 

# 5 Column V, s<sup>2</sup> p<sup>3</sup> configuration

Hund's theory predicts that in the elements of column V the ground term should be  ${}^4S_{1\frac{1}{4}}$  and that above this should lie four metastable states  ${}^2D_{2\frac{1}{4},1\frac{1}{4}}$  and  ${}^2P_{1\frac{1}{4},\frac{1}{4}}$  And empirically these five terms have been found in the arc spectra of nitrogen, phosphorus, arsenic, antimony and bismuth

Of these spectra only NI and PI have been fully analysed NI was not easily observed, for many of the lines lie inconveniently far out in the infra-red or ultra-violet, moreover, when excited by an arc strong bands appear which are apt to mask the

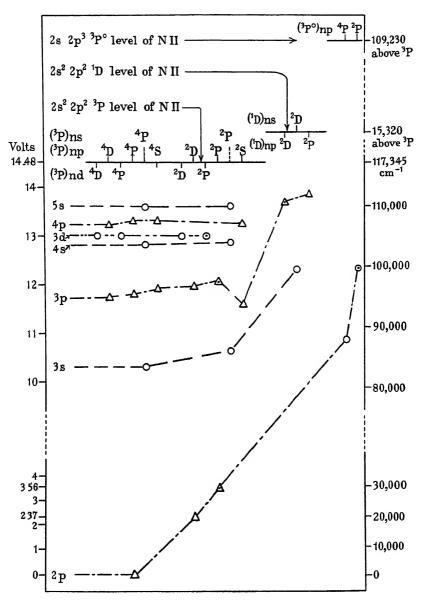


Fig 148 Level diagram of nitrogen

ultra-violet lines, while more vigorous excitation only brings out the spark lines. Compton and Boyce have, however, excited the ultra-violet lines with single electron impacts, a convenient technique because work on neon and argon shows that a single impact will not disturb more than two electrons, no lines of the

	Nπ						
$l_1 l_2$	$l_4$	Term	l <sub>s</sub>	Te	Term		
2s <sup>2</sup> 5	$2p^2$	3P	2p	4S° 2D°2P°		s <sup>2</sup> p <sup>3</sup>	
			ns np nd	<sup>4</sup> P <sup>4</sup> (SPD)° <sup>4</sup> (PDF)	<sup>2</sup> P <sup>2</sup> (SPD)° <sup>2</sup> (PDF)	s²p² s s²p² p s²p² d	
		<sub>1</sub> D	ns np		$^{2}\mathrm{D}$ $^{2}(\mathrm{PDF})^{\circ}$	s <sup>2</sup> p <sup>2</sup> s s <sup>2</sup> p <sup>2</sup> p	
		<sup>1</sup> S	ns $n$ p		<sup>2</sup> S <sup>2</sup> P°	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
2s 2	$p^3$	3Po	2p	<sup>4</sup> P	²(SPD)	sp4	

Fig 14 9 Terms predicted in column V

second spark spectrum being produced even when the potential is more than adequate

In PI many lines he even further out in the infra-red than in NI, so far out in fact that the usual sensitiser neo-cyanine would not serve, recently, however, at the Bureau of Standards a new sensitiser has extended the range which can be photographed and a thorough analysis of PI has been made

In the three remaining elements few terms outside the ground configuration have been named, though the energies of many are known, the intervals of these five terms, however, still show them as a singlet and two doublets in Sbi (Fig. 14 10), while in Bii the

Interval	N	P	As	Sb	Bı
$^{4}S_{1\frac{1}{4}}^{-2}D_{1\frac{1}{4}} \\ ^{2}D_{1\frac{1}{4}}^{-2}D_{2\frac{1}{4}} \\ ^{2}D_{2\frac{1}{4}}^{-2}P_{\frac{1}{4}} \\ ^{2}P_{\frac{1}{4}}^{-2}P_{1\frac{1}{4}}$	19,202	11,366	10,591	8512	11,418
	-8	15	322	1342	4,019
	9,606	7,346	7,272	6541	6,223
	0	25	461	2069	11,505

Fig 14 10 Column V Intervals of the ground configuration,  $s^2p^3$  Note the change from LS coupling in nitrogen to 11 coupling in bismuth

sequence of J values is still unchanged, so that the terms may be named by analogy, in an atom of high atomic weight (LS) coupling is not to be expected

Of the higher terms little need be said, in N i the lowest are <sup>2</sup>P and <sup>4</sup>P from the 2p<sup>2</sup> 3s configuration, while very little higher lies the 2s 2p<sup>4</sup> 4P term The energy relations are shown in Fig 14 8

Most of the term series of  $N_I$  approach the  $^3P$  ground term of  $N_I$  as limit, but experiment shows that different series approach different components of the limit, for if two components of a multiplet tend to the same limit the interval decreases very rapidly, roughly in fact as  $1/n^{*3}$ , but in  $N_I$  the intervals of some terms decrease only slowly or actually increase, this being true in particular of the  $2p^2$  ns  $^4P$  and  $2p^2$  nd  $^2D$  series

	Nı						
n	3	4	5	6	NII		
<sup>4</sup> P <sub>1</sub> - <sup>4</sup> P <sub>1</sub>	33 8	50 0	44 3	44 7	<sup>3</sup> P <sub>0</sub> - <sup>3</sup> P <sub>1</sub>	50	
<sup>4</sup> P <sub>11</sub> - <sup>4</sup> P <sub>21</sub>	46 7	68 7	70 1	72 0	<sup>3</sup> P <sub>1</sub> - <sup>3</sup> P <sub>2</sub>	84	
<sup>4</sup> P <sub>1</sub> - <sup>4</sup> P <sub>2</sub>	80 5	118 7	114 4	116 7	<sup>3</sup> P <sub>0</sub> - <sup>3</sup> P <sub>2</sub>	134	

Fig 1411 Intervals of the 2p2 ns 4P series in N I

With large values of n the intervals of the  $2p^2$  ns  $^4P$  series may reasonably be supposed to approach the values of 50 and 84 cm  $^{-1}$ , which are the intervals of the ground term of N II. And if this is true then  $^4P_{\frac{1}{2}}$  must tend to the lowest or  $^3P_0$  limit, while  $^4P_{\frac{1}{2}}$  must approach the highest or  $^3P_2$  limit. In Fig. 14-12 these facts are shown graphically, the separations being measured horizontally away from the middle terms,  $^4P_{1\frac{1}{2}}$  in N I and  $^3P_1$  in N II. Unfortunately in most series only two or three terms are known, and though the intervals of these may be roughly constant, they do not establish the limits beyond doubt as the above series do Even in the  $2p^2$  nd  $^2D$  series, of which five terms are known, one would hesitate to say whether the intervals tend to a limiting value of 50 or 84 cm  $^{-1}$ , though evidently they do not tend to zero (Fig. 14-13)

The passage of the different components of a multiplet term to

different limits often leads to wide departures from the interval rule, and these, like the departures due to increasing atomic number, may be described with the vector model For consider

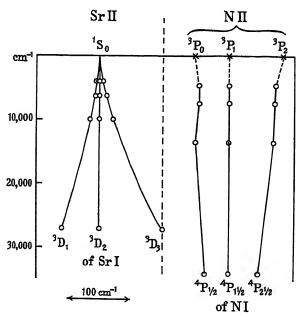


Fig 14 12 Intervals of the 5s nd <sup>3</sup>D series of Sr I contrasted with those of the 2p<sup>2</sup> ns <sup>4</sup>P series of N I, in the first the different series converge to the same limit, in the second they converge to three different limits

n	3	4	5	6	7
$^{2}D_{1\frac{1}{2}}$ $^{2}D_{2\frac{1}{2}}$	23 5	22 2	18 3	58 3	42 6

Fig 14 13 Intervals of the 2p2 nd 2D series of N r

the addition of an electron defined by n, l, s to an ion defined by  ${}_{i}$ L,  ${}_{i}$ S, then in the low terms the couplings ( ${}_{i}$ Ll) and ( ${}_{i}$ Ss) are strong, while (LS) and (ls) suffice only to produce the splitting of the multiplet term into its components, but (Ll) and (Ss) decrease as the chief quantum number of the electron increases and actually vanish when n tends to infinity, while (LS) remains constant, so that when n is sufficiently large the latter becomes

the more important and the splitting becomes that of the ionic ground term

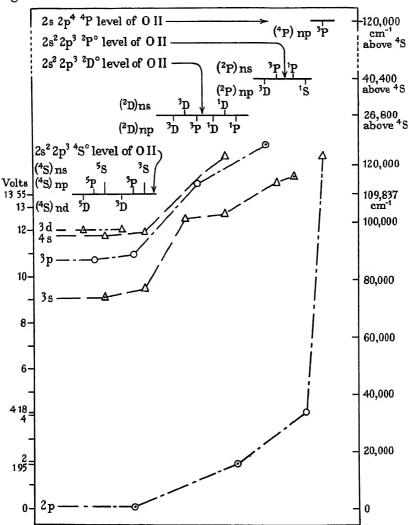


Fig 14 14 Level diagram of oxygen.

# 6 Column VI, s<sup>2</sup> p<sup>4</sup> configuration

Hund's theory predicts in column VI five low terms,  $^3P_{2,1,0}$ ,  $^1D_2$  and  $^1S_0$ , and empirically the  $^3P$  term has been identified in casin

the spectra of oxygen, sulphur, selenium and tellurium, while the two singlet terms are still missing only in sulphur (Fig. 14 14). The most notable changes in the energies of these low terms with increasing atomic number are first the closing together of the five terms, and secondly the movement of the  $^3P_1$  term from its normal position one-third of the distance between  $^3P_0$  and  $^3P_2$  up to and past  $^3P_0$ , so that in tellurium the  $^3P$  term is partially inverted (Fig. 14 15)

Interval	0	S	Se	Te
$\begin{array}{c} ^{3}\mathrm{P}_{2} - ^{3}\mathrm{P}_{1} \\ ^{3}\mathrm{P}_{1} - ^{3}\mathrm{P}_{0} \\ ^{3}\mathrm{P}_{0} - ^{1}\mathrm{D}_{2} \\ ^{1}\mathrm{D}_{2} - ^{1}\mathrm{S}_{0} \end{array}$	158 67 15,641 17,925	398 174 —	1,989 545 7,042 13,794	4,751 -44 5,852 12,640

Fig 14 15 Column VI Intervals of the ground configuration, s<sup>2</sup> p<sup>4</sup>

Beyond these low terms very little is known of Tei, while in Seionly a few quintet terms have been identified, but a list of the higher terms predicted for all spectra of column VI is given in Fig. 14-16

0 п		01					
$l_1 l_2 \qquad l_5$	Term	$l_6$		Terms		$l_1$ $l_6$	
2s² 2p³	4S°	2p ns np nd	<sup>5</sup> S° <sup>5</sup> P	3D° 3B 3S° 3B	<sup>1</sup> D <sup>1</sup> S	$\begin{array}{c} s^2 p^4 \\ s^2 p^3 s \\ s^2 p^3 p \\ s^2 p^3 d \end{array}$	
	2D°	$n_{ m p} \\ n_{ m d}$		³D° ³(PDF) ³(SPDFG)°	¹D° ¹(PDF) ¹(SPDFG)°	s <sup>2</sup> p <sup>3</sup> s s <sup>2</sup> p <sup>3</sup> p s <sup>2</sup> p <sup>3</sup> d	
	2P°	$n_{ m p} \\ n_{ m d}$		³P° ³(SPD) ³(PDF)°	<sup>1</sup> P° <sup>1</sup> (SPD) <sup>1</sup> (PDF)°	s <sup>2</sup> p <sup>3</sup> s s <sup>2</sup> p <sup>3</sup> p s <sup>2</sup> p <sup>3</sup> d	
2s 2p4		2p		3Po	¹P°	$sp^5$	

Fig 14 16 Terms predicted in column VI

In O<sub>I</sub> and S<sub>I</sub> series were identified by Paschen and Runge before the end of last century, and these are listed in Fowler's Report as singlets and triplets Theoretically these series should be prominent, because the normal state of the ion is an S state, but a 4S ground term should produce systems of triplets and quintets, not of singlets and triplets. This discrepancy between experiment and modern theory was only resolved in 1923 when Hopfield identified series of lines arising from the combination of Fowler's 'singlet' S and D series with a 3P ground term. The numerical values of the three components of the term are 109,833, 109,674 and 109,607,\* showing intervals of 159 and 67 respectively and an interval ratio of 2.4. In combinations of this term the line of shortest wave-length is the most intense, so that the 3P term must be inverted

As inter-system lines are seldom strong, the combination of this triplet term with a 'singlet' series suggested that the supposed singlets were really triplets too narrow to be resolved True, the <sup>3</sup>P ground term also combines with Fowler's Is 'triplet' term, but the lines are much weaker, and though the  $1s \rightarrow {}^3P_2$  and  $1s \rightarrow {}^3P_1$  lines are quite clear, the  $1s \rightarrow {}^3P_0$  line is missing in both O i and S i. If, however, the supposed triplets are really quintets the absence of this particular line is readily explained, for the 1s term is then  ${}^5S_2$ , and the combination with  ${}^3P_0$  is forbidden, since J would have to change by two units. This evidence alone seems conclusive, but in 1923 the argument from theory was of little weight and so Paschen and Landé† felt bound to settle the question by measuring the Zeeman splitting of two quintet combinations  $7771\,\mathrm{A}$ ,  $3p\,{}^5P_{123} \rightarrow 3s\,{}^5S_2$  and  $3974\,\mathrm{A}$ ,  $4p\,{}^5P_{123} \rightarrow 3s\,{}^5S_2$ 

Above the  $^3\mathrm{P}$  term thus identified the metastable states  $^1\mathrm{D}_2$  and  $^1\mathrm{S}_0$  should be, and recently combinations of these states with various higher terms have been identified in O I, but history records that these lines were found only after McLennan‡ had shown in a brilliant research that the green auroral line 5577 A arises in a jump between these two states. As the transition is forbidden by two selection rules the evidence requires careful scrutiny, it will be considered in a later chapter on quadripole radiation

35

<sup>\*</sup> Hopfield, AJ, 1924, 59 114

<sup>†</sup> Laporte, Nw, 1924, 12 598, attributes this work to Paschen and Landé, but the reference given is inaccurate and the paper does not appear under either name in Science Abstracts, 1922–24

<sup>|</sup> McLennan, PRS, 1928, 120 327

# 7 The halogens, s<sup>2</sup>p<sup>5</sup> configuration

According to Hund's scheme the p<sup>5</sup> configuration produces only an inverted <sup>2</sup>P term, and in fact this is the normal state of all halogen atoms

The higher terms may be divided into three groups according as they arise from the <sup>3</sup>P, <sup>1</sup>D or <sup>1</sup>S term of the spark spectrum Of the predicted terms shown in Fig. 14 17, a large number have been

Fn				Fı	
$l_1 l_2  l_6$	Term	L7	T	erms	l <sub>1</sub> l <sub>7</sub>
2s <sup>2</sup> 2p <sup>4</sup>		2p	2]	P°	s <sup>2</sup> p <sup>5</sup>
	3P	$n_{ m S} \\ n_{ m D} \\ n_{ m d}$	<sup>4</sup> P <sup>2</sup> P <sup>2</sup> (SPD)° <sup>2</sup> (SPD)° <sup>4</sup> (PDF) <sup>2</sup> (PDF)		s <sup>2</sup> p <sup>4</sup> s s <sup>2</sup> p <sup>4</sup> p s <sup>2</sup> p <sup>4</sup> d
	1D	ns np nd	— <sup>2</sup> D — <sup>2</sup> (PDF)° — <sup>2</sup> (SPDFG)		s <sup>2</sup> p <sup>4</sup> s s <sup>2</sup> p <sup>4</sup> p s <sup>2</sup> p <sup>4</sup> d
	1S	ns np nd	- 2S - 2P° - 2D		s <sup>2</sup> p <sup>4</sup> s s <sup>2</sup> p <sup>4</sup> p s <sup>2</sup> p <sup>4</sup> d

Fig 14 17 Terms predicted in the halogens

found in the arc spectra of all the halogens, and in the spark spectra of neon, argon and krypton. In particular, Bakker, De Bruin and Zeeman\* have made an extensive magnetic analysis of A ii and have studied the spectrum very thoroughly, it provides much material for the study of irregular g values and of series limits, and will be referred to again in that context, the terms obey the normal multiplet laws badly, but the Rydberg formulae rather well  $\dagger$ . In the lighter elements the empirical terms are easily named, for they approximate to the Russell-Saunders laws, but only the J values of the higher terms of I i are known

Directly above the ground term come even terms from the  $p^4$  s and  $p^4$  d configurations. Of these the  $p^4$  ( $^3P$ ) s configuration should produce five terms, named according to the Russell-Saunders scheme  $^4P_{2\frac{1}{2},1\frac{1}{2},\frac{3}{2}}$  and  $^2P_{1\frac{1}{2},\frac{3}{2}}$ , and in fact in Fi the extreme

<sup>\*</sup> Bakker, De Brum and Zeeman, K Akad Amsterdam, Proc , 1928, 31 780. † Rosenthal, AP, 1930, 4 80

intervals of the two multiplets are less than 450 and 350 respectively, while they are separated by nearly 2000 cm<sup>-1</sup> In II, on

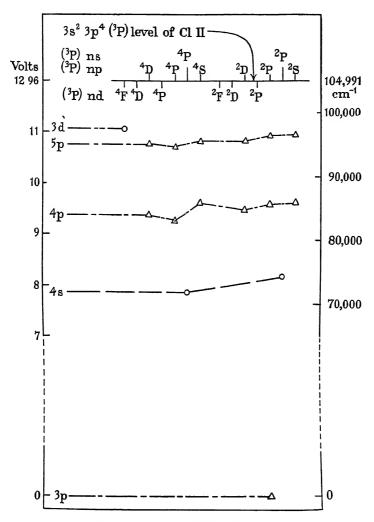


Fig 14 18 Level diagram of chlorine

the other hand, the division of the five terms into multiplets is not justified by their energies, as the sequence of J values is the same as in chlorine, the empirical terms may be named by

analogy, but if this is done  $\Delta^4P_{1\frac{1}{4},\frac{1}{4}}$  is 4800 cm  $^{-1}$  while  $^2P_{1\frac{1}{4}}$  is only 900 cm  $^{-1}$  (Fig. 14 20). If the five terms are divided by their energies, they form two diads below and a monad above, thus the lowest terms form a diad and have J values of  $2\frac{1}{2}$  and  $1\frac{1}{2}$ ,

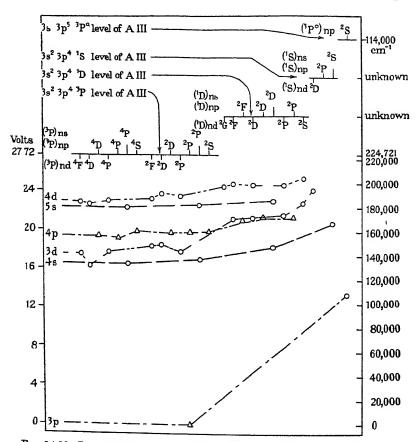


Fig 14 19 Level diagram of A  $\scriptstyle\rm II$  Note that the d levels lie deeper here than m the preceding figure, which shows the isoelectronic spectrum Cl  $\scriptstyle\rm I$ 

being formed presumably by the addition of an s electron to the  $^3P_2$  spark term, similarly, the next diad has J values of  $1\frac{1}{2}$  and  $\frac{1}{2}$ , and so may be assumed to arise from the addition of the s electron to the  $^3P_1$  spark term, and highest of all lies the single level with a J value of  $\frac{1}{2}$ , arising as  $(^3P_0)$ s. These energy values clearly justify

us in saying that the coupling in Fi is Russell-Saunders, but in Ii is (1j)

A comparison of the isoelectronic spectra Cli and AII brings out one common effect of increasing the nuclear charge, in Cli the succession of the configurations is apparently 4s, 4p, 5s, 5p, 3d,

	F	Cl	Br	I
$^{4}P_{2i}^{-4}P_{1i}^{1}$ $^{4}P_{1i}^{-4}P_{i}^{1}$ $^{4}P_{1i}^{-2}P_{i}^{1}$ $^{2}P_{1i}^{-2}P_{i}^{1}$	275 160 1892 325	530 338 1398 640	1471 1977 300 1787	1459 4803 924 4530
$\Delta^{3}\mathbf{P_{02}}$ of ion	491	991	_	_

Fig 14 20 Intervals of the  $p^4$  (<sup>3</sup>P) s configuration, showing the change from LS to 11 coupling

terms arising from all the configurations except 5s having been identified, but in A  $\pi$  the succession is 4s, 3d, 4p, 5s, 4d, the increased nuclear charge having thus moved the d terms down relative to the s and p terms. Of this movement much more will be heard in the long periods

## 8 The mert gases, s2p6 configuration

The p<sup>6</sup> group, being a complete shell, produces only a <sup>1</sup>S term, and empirically this always lies so much deeper than any of the odd terms that the lines which result lie in the far ultra-violet. The ground term and the lowest configuration of odd terms have been identified in the arc spectra of neon, argon, krypton and xenon and also in the spark spectra Na II, K II, Rb II and Cs II, of these neon was the subject of such a thorough study at a time when the structure of complex spectra was very little understood that it still deserves pride of place (Figs. 14-21, 22)

The spectrum of neon consists of two parts, one in the visible analysed into series by Paschen in 1918,\* and a few ultra-violet lines unknown to Paschen, but discovered by Lyman and Saunders in 1925; and attributed at once to the deep 'S ground term The large number of series discovered by Paschen may be

<sup>\*</sup> Paschen, AP, 1919, 60 405, 1920, 63 201

<sup>†</sup> Lyman and Saunders, PR, 1925, 25 886a

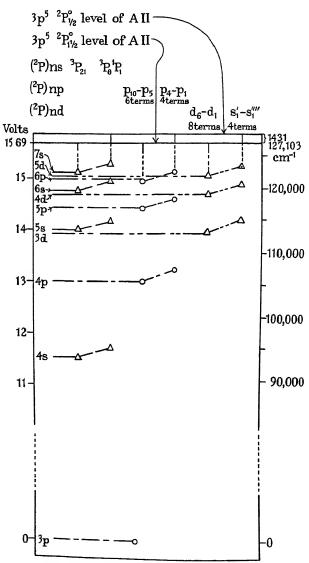


Fig 14.21 Level diagram of argon, this differs from the level diagram of neon only in the energies of the terms

divided by the energies of their lowest terms into three groups, of these the lowest contains four terms, named from below up  $s_5$ ,  $s_4$ ,  $s_3$  and  $s_2$ , and identified in modern theory with the  $2p^5(^2P) 3s$  configuration. Above these he ten terms called by Paschen p terms, and written from below up  $p_{10}$  to  $p_1$ , these combine with

	Ne п		Neı				
$l_1 l_2$	l <sub>7</sub>	Terms	$l_8$	Terms	Paschen's terms	l <sub>1</sub> l <sub>8</sub>	
2s <sup>2</sup>	$2\mathbf{p^5}$	<sup>2</sup> P°	$2\mathbf{p}$	1S	_	$s^2p^6$	
			ns np nd	<sup>3</sup> (PDF)° <sup>1</sup> (PDF)°	s <sub>2</sub> , s <sub>3</sub> , s <sub>4</sub> , s <sub>5</sub> p <sub>1</sub> p <sub>10</sub> s <sub>1</sub> and d	$     \begin{array}{ccccccccccccccccccccccccccccccccc$	

Fig 14 22 Terms predicted in the mert gases

the s terms and clearly arise from the  $p^5$  (<sup>2</sup>P) 3p configuration Higher still appear twelve terms written some of them d and some  $s_1$ , these arise from the  $p^5$  (<sup>2</sup>P) 3d configuration. All these terms were assigned J values by Landé\* as the result of a magnetic analysis (Fig. 14-23), and these J values agree precisely with those required by theory

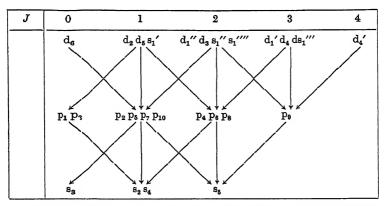


Fig. 14.23 Permitted combinations and J values of the empirical terms of neon

Though thus far agreement is so satisfactory the s terms alone come near to obeying the multiplet laws By Hund's energy rules these four terms should be  ${}^{3}P_{2,1,0}$  and  ${}^{1}P_{1}$  in order of increasing energy (Fig. 14 23), the empirical J values establish the  ${}^{3}P_{2}$  and  ${}^{3}P_{0}$  terms in the positions indicated, while for  $s_{4}$  and  $s_{2}$  Back\*

Terms		g fac	tor	Lamit		
Emp	Theor	Emp	Theor	Emp	Theor	
82 83 84 85	<sup>1</sup> P <sub>1</sub> <sup>3</sup> P <sub>0</sub> <sup>3</sup> P <sub>1</sub> <sup>3</sup> P <sub>2</sub>	1 04	1 15 15	Upper Upper Lower Lower	<sup>2</sup> P <sub>1</sub>	

Fig 14 24 The  $2p^5$  ns terms of neon, the empirical g values are those of the first or 3s term of the series

obtained g values of 1.46 and 1.03, in satisfactory agreement with the theoretical values of 1.5 for  ${}^3P_1$  and 1.0 for  ${}^1P_1$ . Moreover, this allotment is confirmed by the ultra-violet combinations with the  ${}^1S_0$  ground term, for the line of lower frequency  $s_4 \rightarrow {}^1S_0$  is weaker than the line of higher frequency  $s_2 \rightarrow {}^1S^{\dagger}$ , and this agrees with the general rule that inter-system lines are weaker than combinations between terms of the same system

The p terms present much greater difficulties, a very brief examination shows that the interval rule is quite useless, while the Landé g formula is none too well obeyed. Accordingly, the matching proposed by Hund‡ (Fig. 14-24) must be regarded at best as the reasoned guess of an expert, for a thorough study of the transition from Russell-Saunders to (jj) coupling is necessary before a satisfactory solution can be reached § Judging from H. N. Russell's success with the complex spectra of the iron row, a satisfactory solution might be expected from a careful study of intensities, but this does not seem to have been attempted yet

In ordering the high terms to series based on these low terms Paschen found clear evidence that the series might be divided into two groups, some tending to a lower limit and others to a limit 780 cm<sup>-1</sup> higher, these two limits appear in modern theory

<sup>\*</sup> Back, AP, 1925, 76 317

<sup>+</sup> Shenstone, N, 1928, 121 619

t Hund, ZP, 1929, 52 601

 $<sup>\</sup>$  Pogány, ZP, 1935, 93 376 and chapter xvIII,  $\S$  7

as the two components of the  $^2P$  ground term of Ne II, now known to have an interval of 782 cm  $^{-1}$  Of the s terms  $s_2$  and  $s_3$  tend to the upper limit,  $s_4$  and  $s_5$  to the lower limit, the limits of the p series are shown in Fig. 14 25

	E	The	retical		
Term	J	g	Limit	Terma	g
p <sub>1</sub> p <sub>3</sub>	0	<del>0</del> 000	Upper Lower	<sup>3</sup> P <sub>0</sub> <sup>1</sup> S <sub>0</sub>	0 0 0
P <sub>2</sub> P <sub>5</sub> P <sub>7</sub> P <sub>10</sub>	1 1 1	1 340 0 999 0 699 1 984	Upper Upper Lower Lower	<sup>3</sup> P <sub>1</sub> <sup>1</sup> P <sub>1</sub> <sup>3</sup> D <sub>1</sub> <sup>3</sup> S <sub>1</sub>	1 5 1 0 0 5 2 0
P <sub>4</sub> P <sub>6</sub> P <sub>8</sub>	2 2 2	1 301 1 229 1 137	Upper Lower Lower	$^{3}P_{2}$ $^{3}D_{2}$ $^{1}D_{2}$	1 5 1 167 1 0
Pa	3	1 329	Lower	$^{3}\mathrm{D}_{3}$	1 333

Fig 14 25 The 2p<sup>5</sup> 3p terms of neon

a The naming of the terms is based on the most exiguous evidence

Interval	Ne	A	Kr	Хe
<sup>3</sup> P <sub>2</sub> - <sup>3</sup> P <sub>1</sub>	417	607	945	978
<sup>3</sup> P <sub>1</sub> - <sup>3</sup> P <sub>0</sub>	359	803	4275	8152
<sup>3</sup> P <sub>0</sub> - <sup>1</sup> P <sub>1</sub>	1070	846	655	988

Fig 14 26 Intervals of the  $p^5$  (<sup>2</sup>P) s configuration in the inert gases

The spectra of the heavier mert gases are very similar to neon, but as the interval of the ground term of the spark spectrum increases, its influence on the arc spectrum becomes increasingly evident, it appears, for instance, in the intervals of the four (<sup>2</sup>P)s terms, shown in Fig. 14-26, while in Krithe p terms divide themselves into two groups with an interval of no less than 5200 cm<sup>-1</sup> between them, the upper group consists of four terms and the lower group of six just as theory will be shown to require, but the chance of fitting the Russell-Saunders notation to these terms is more remote even than in neon

Indeed, the heavy mert gases centre in themselves three influences which all conspire to break up the simple Russell-

Saunders coupling, first, increasing atomic number makes for loss of regularity, this was discussed particularly in columns IV and V, but it is visible in every column, secondly, the increasing separation of the ground term of the ion tends to divide the terms by limits rather than by multiplets, and lastly spectra grow less regular as one passes from left to right across the periodic table, neon is less regular than carbon and carbon less regular than sodium

### BIBLIOGRAPHY

The first systematic account was by Hund in Linienspektren und periodisches System der Elemente, 1927, and this is still standard

Term values are largely taken from Bacher and Goudsmit, Atomic Energy States, 1932 References to particular elements can be traced in the select bibliography of Appendix VI

#### CHAPTER XV

### LONG PERIODS

### 1 The ground terms

In the short periods the s electron carries appreciably less energy than the p electron, and very little study suffices to show that the first two electrons enter an s shell and the last six a p In the long periods however, while an s electron still carries less energy than a p, the s and d electrons carry roughly the same energy, so that a first glance shows one group of twelve elements instead of two groups of two and ten

1	2	3	4	5	6	7	8	9	10	11	12
		Sc									
		${f Y}$									
		La-Lu									

Bohr's work on the periodic system showed that in the first two of these twelve elements the electron enters an s orbit, but that thereafter as the nuclear charge increases the d orbits grow more stable and the s less, until in the spark spectrum of a system of ten electrons all ten occupy d orbits, and produce the  $^{1}S_{0}$  ground term characteristic of a complete shell. The eleventh and twelfth electrons then re-enter the s shell producing copper, zinc and their homologues. Thus in only eight of the twelve elements are the configurations still in doubt, these eight were enclosed by Bohr in a frame, and will be described in successive periods as the elements of the iron frame, the palladium frame and the platinum frame

Since only two electrons can enter an s shell, an atom with n outer electrons has the choice of only three configurations,  $d^n$ ,  $d^{n-1}$  s and  $d^{n-2}$  s<sup>2</sup>, the chief quantum numbers will usually be omitted, in order to simplify the discussion, for the orbits are always 3d and 4s in the iron frame, 4d and 5s in the palladium frame and 5d and 6s in the platinum frame

The terms, which any configuration produces, can be calculated, and if the lowest term of each configuration is that with

largest spin and orbital vectors, a list of possible configurations and the ground terms which they produce can be compiled, as Fig 15 1 shows But the ground term is the easiest of all terms to determine empirically, so that the argument which produced this table may be reversed, and the ground term used to decide which configuration produces the lowest term (Figs 15 2-4) When

No of	Configuration						
electrons	$\mathbf{d}^n$	d <sup>n-1</sup> s	dn-2 s2				
0 1 2 3 4 5 6 7 8 9 10 11	S F F S S F F S S F S S F S S S S S S S	25 20 4F 4F 25 20 5F 4F 25 25	18 2D 3F 4F 68 5D 4F 3F 2D				

Fig 15 1 Ground terms of three configurations

No of elec- trons		Arc spectr	В.	S	No of		
	Atom	Ground term	Con- figuration	Atom	Ground term	Con- figuration	elec- trons
1 2 3 4 5 6 7 8 9 10 11 12	K Ca So Ti V Cr Mr Fe Co Ni Cu Zn	2S 1S 2D 2F 4F 7S 6S 5D 4F 2S 1S	8 82 d 82 d 8 83 d 8 82 d 10 8 d 10 8	Ca+ Sc+ Tr+ V+ Cr+ Mn+ Fe+ Co+ Nr+ Cu+ Zn+ Ga+		s d s (d² s) d⁴ d⁵ s d⁵ s d⁵ d⁵ d¹	1 2 3 4 5 6 7 8 9 10 11 12

Fig 152 Ground terms of the iron frame elements

In this and the two following figures, the ground term is given only when it is known empirically; a? following the term shows that it is still open to doubt A configuration enclosed in brackets cannot be deduced from the ground term alone, but is known from further study of the spectrum, where a configuration is given in the absence of the ground term, reliance has been placed on the argument of §4 of this chapter

there are 3, 6 or 9 electrons, two configurations produce the same ground term, and then further study is necessary to distinguish between them, where a configuration has been obtained in this way, it is enclosed in brackets

No of		Arc spect	ra.	S	No of		
elec trons	Atom	Ground term	Con- figuration	Atom	Ground term	Con- figuration	elec trons
1 2 3 4 5 6 7 8 9	Rb Sr Y Zı Cb Mo Ma Ru Rh	SOUP OF PERSON	s s² d s² d² s² d⁴ s d⁴ s d⁵ s² d7 s (d³ s) d10	Sr+ Y Zr+ Cb+ Mo+ Ma+ Ru+ Rh+ Pd+ Ag+ Cd+	<sup>2</sup> S <sup>1</sup> S <sup>4</sup> F <sup>5</sup> D <sup>6</sup> S <sup>7</sup> <sup>4</sup> F <sup>2</sup> D <sup>2</sup> S	s s <sup>2</sup> d <sup>2</sup> s d <sup>4</sup> d <sup>5</sup> d <sup>5</sup> s d <sup>7</sup> d <sup>8</sup> d <sup>9</sup> d <sup>10</sup>	1 2 3 4 5 6 7 8 9
11 12	Ag Cd	<sup>2</sup> S <sup>1</sup> S	d <sup>10</sup> s d <sup>10</sup> s	Cd+ In+	<sup>2</sup> S <sup>1</sup> S	d <sup>10</sup> s <sup>2</sup>	11 12

Fig 15 3 Ground terms of the palladium frame elements

No of		Arc spect	ra	S	tra	No of	
elec- trons	Atom	Atom Ground Co		Atom	Ground term	Con- figuration	elec trons
1 2	Cs Ba	<sup>2</sup> S <sup>1</sup> S	s s²	Ba+ La+ Lu+	<sup>2</sup> S <sup>3</sup> F <sup>1</sup> S	s d <sup>2</sup> s <sup>2</sup>	1 2
3	La Lu	<sup>2</sup> D <sup>2</sup> D	d s² d s²	Hf+	<sup>1</sup> S <sup>2</sup> D	d s²	3
4	Hf	3H	d2 s2	Ta+	l —		4 5
4 5 6	Ta	_	d³ s²	W+	l —	_	5
6	w	5D	(d4 s2)	Re+	l —	_	6 7
7	${f Re}$	<sup>6</sup> S	d <sup>5</sup> s <sup>2</sup>	Os+		_	7
8 9	Os	<u> </u>	$d^6 s^2$	Ir+			8 9
9	Ir	<sup>2</sup> D <sup>9</sup>	d <sup>9</sup> ۶	Pt+	1 —		9
10	$\mathbf{Pt}$	3D	d <sup>9</sup> s	Au+	1 1S	$d^{10}$	10
11	Au	<sup>2</sup> S	d10 s	Hg+	2S	d10 s	11
12	Hg	1S	d <sup>10</sup> s <sup>2</sup>	Tl <sup>+</sup>	<sup>1</sup> S	d <sup>10</sup> s <sup>2</sup>	12

Fig 154 Ground terms of the platinum frame elements

With only one exception the arc spectra of the iron frame (Fig 15 2) have  $d^{n-2}$  s<sup>2</sup> as their ground configuration, while the spark spectra have  $d^{n-1}$  s or  $d^n$ , a contrast which shows how general is the tendency of the d electrons to sink relative to the s electrons as the nuclear charge increases, of this tendency an oft-

1/2

quoted example is the descent of the s electron of K I and Ca II into the d orbit of Sc III In the palladium frame (Fig 15 3) the tendency is again in evidence, the d<sup>n</sup> configuration produces the ground terms of six spark spectra, but only one are Comparison of the iron and palladium frames shows that the d orbits are more stable in the latter, of the platinum frame (Fig 15 4) not much is yet known, but there is some reason to think that in the early elements the d orbits are more stable still, but that after the intrusion of the f shell between lanthanum and lutecium, the d shell is less stable even than in the iron frame. Thus La II has a d<sup>23</sup>F ground term in contrast to the ds <sup>3</sup>D of Sc II and the s<sup>21</sup>S of Y II, but the ground states of Lu II, Lu I, Hf I and Re I all seem to contain two s electrons, besides varying numbers of d electrons

## 2. Configurations and analysis

In all three frames the s and d electrons have roughly the same energy, and this determines the general form of the spectra A configuration which contains only s and d electrons outside the last closed shell will consist of even terms, and accordingly the low terms of all elements are even, they will usually arise from two different configurations, and as no combinations are permitted, the higher of the two is metastable

Above these low terms come a group of odd terms containing a p electron, and above those again a second group of even terms containing only s and d electrons. Theory allows many higher terms, but in practice the lines involving these terms are weak or absent, so that series consist of only two or at most three terms.

This means that the method of analysis differs from that applied to simple spectra\*, the spectroscopist tries to find not series, but multiplets As in other spectra constant differences between the frequencies of pairs of lines indicate terms, and these may be separated into odd and even, because an odd term combines only with an even The ground term can usually be picked out because it gives rise to the rares ultimes and most of the absorption lines, the spark produced under water is also useful,

<sup>\*</sup> For an account of methods of analysis, see Russell, AJ, 1927, 66 348

for the spectrum consists of a few lines all ending in the ground term

The approximate energy of a term can be determined by examining the temperature class of the lines to which it gives rise. If it is of low energy content, then it will appear bright at a low temperature and in King's classification will belong to a low class. This and the division into odd and even terms will often determine the configuration to which a term belongs

Finally, the terms of a configuration may be divided into multiplets by examining the intensities of the lines to which they give rise, for when the coupling is not normal the intensities are far less seriously disturbed than either Landé's interval ratios or the magnetic splitting factors

To suit these new methods of analysis, new ways of specifying the empirical terms have had to be developed, thus the analysis may succeed in finding terms, but be unable to divide them into multiplets, the terms are then numbered 1, 2, 3, beginning from the term of lowest energy, or if the J value is also known then this may be added as a suffix  $1_{2\frac{1}{2}}$  Or again the terms may have been worked out, and then each term is specified by a small letter placed before its term symbol, in this notation the letters a to e are reserved for the low terms, z, y, x, for the middle or odd terms, and f, g, h, for the high terms, in each group the terms are lettered from low to high energy

## 3 Individual spectra

The spectra of the long periods are most naturally classified by the number of electrons outside the last mert gas shell, and in this order they will be reviewed

The energies of all the low terms and a varying number of odd terms are tabulated, the energy given for any multiplet is that of the component with greatest J, for this will produce the strongest lines, the energies are measured up from the ground term, and the ground term itself is in clarendon type. To avoid any misunder-standing the chief quantum number is added for spectra of the iron frame, to apply to the palladium and platinum frames it should be increased by one and two respectively

CASII

One electron KI, RbI, CsI, CaII, SrII, BaII, RaII, ScIII, YIII, LaIII, LuIII, Tiiv, Zriv, Ceiv

In the arc spectra of the alkalis and the spark spectra of the alkaline earths the ground term is always <sup>2</sup>S, the single electron occupying a 4s, 5s or 6s orbit With further increase in the nuclear charge, however, the electron falls into a d orbit, for Sc III, Y III, Zr IV, and Ce IV are all known to have a <sup>2</sup>D ground term

The introduction of a group of f electrons produces, however, a surprising change, Lu III, which differs from La III only in having this group, has a <sup>2</sup>S ground term, so that the 6s orbit must have grown more stable than the 5d

#### Low terms

	K	Rb	Cs	Ca 11	Sr 11	Вап	Ra rr
${}^{4s}{}^{2}S_{\frac{1}{2}}$ 3d ${}^{2}D_{2\frac{1}{2}}$	0 21,539	0 19,355	0 14,597	0 13,711	0 16,837	0 5,675	0 26,209

	Sc III	Ym	La m	Lu m	Tı ıv	Zr IV	Ce IV
4s <sup>2</sup> S <sub>1</sub>	25,537	7466	13,590	0	80,379	38,258	5152
3d <sup>2</sup> D <sub>21</sub>	198	725	1,604	8648	348	1,250	3305

Fig 15 5 One electron Energies of the low terms

Two electrons. Cai, Sri, Bai, Scii, Yii, Laii, Luii, Tim, Zriii.

The ground terms of the arc spectra of the alkaline earths and the second spark spectra of column IV are respectively  ${}^{1}S_{0}$  and  ${}^{3}F_{2}$ , the first arising from the  ${}^{2}$  configuration and the second from the  ${}^{2}$ , and this is natural enough, since the d orbit normally sinks relative to the s as the nuclear charge increases. Between these two extremes the singly ionized earth metals should provide a natural transition, and in some measure they do, for the ground term of Schidalder should should

electron to the ground term of the next higher spark spectrum, but Y  $\pi$  forms an exception to this rule also, for the single electron of Y  $\pi$  occupies a d orbit

The other low terms which theory dictates are shown in Fig 157, and just these terms are actually found in the spark

Low	terms
-----	-------

	Ca	Sr	Ba	Sc 11	Υп	La 11	Lu 11	Тип	Zr m
4s <sup>2</sup> <sup>1</sup> S	0	0	0	11,736	0	7,395	0		
3d 4s <sup>3</sup> D <sup>1</sup> D	$\begin{bmatrix} 20,371 \\ 21,849 \end{bmatrix}$	18,320 20,149	9,596 11,395	178 2,541	1,450 3,296	3,250 1,395	14,199 17,332	38,425 41,704	19,533 16,122
3d <sup>2</sup> <sup>3</sup> F	48,564	32,625	23,919	4,988 12,154	8,743 14,098	1,971 6,227	32,504	422 10,721	1,487 8,840
¹G ¹D	4 _	=	_	14,261 10,945	15,683 14,833	7,473 10,095	_	14,398 8,473	2,534 3,392
1S		_	_	1 -	_	<u> </u>	_	14,053	3,835

Fig 156 Two electrons Energies of the low terms

#### Low terms

Configuration	Terms			
Comiguration	Triplets	Singlets		
4s² 3d 4s 3d²	D PF	S D SDG		

#### Middle terms

I	on	Atom				
l <sub>1</sub> Term		$l_2$	Terms	$l_1 l_2$		
3d 4s	<sup>2</sup> D <sup>2</sup> S	4p 4p	³(PDF)° ¹(PDF)°	dp sp		

### Hıgh terms

Id	n	Atom				
$l_1$	Term	l <sub>2</sub>	Terms	$l_1 l_2$		
Зđ	²D	nd	<sup>3</sup> D <sup>1</sup> D <sup>3, 1</sup> (SPDFG)	d s d d		
49	<sup>2</sup> S	ns nd	<sup>3</sup> D <sup>1</sup> D	s s s d		

Fig 15 7 Terms predicted from two electrons

spectra,  $d^2$  1S has been a little difficult to locate, but it has been found all right in Ti III and Zr III These low terms are in satisfactory agreement with Hund's energy rules, in the d s configuration of Sc II, for example, the <sup>3</sup>D term lies below <sup>1</sup>D, while in the d<sup>2</sup> configuration <sup>3</sup>F lies below <sup>3</sup>P, among the singlets, however, b <sup>1</sup>D is lower than a <sup>1</sup>G Deviations such as this are common in all spectra

The middle and high terms have also been collected in Fig 157, and the general relations of a typical spectrum are shown in

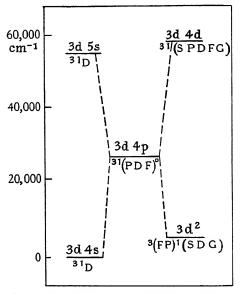


Fig 15.8 Simplified level diagram of Sc  $\pi$ 

Fig 15 8, where the four groups of even terms, arising from the configurations 3d<sup>2</sup>, 3d 4s, 3d 4d and 3d 5s, all combine with the central group of odd terms, but not at all with each other. This means, of course, that all terms of the 3d<sup>2</sup> configuration are metastable, for no direct return to the ground state is possible.

In the high 3d 4d configuration of Sc II the agreement with Hund's energy rules is much less satisfactory than among the low terms, among the triplets <sup>3</sup>F and <sup>3</sup>P lie close together, but some 4000 cm <sup>-1</sup> above the <sup>3</sup>G, <sup>3</sup>D and <sup>3</sup>S levels, while among the



singlets, on the other hand, <sup>1</sup>F and <sup>1</sup>P he some 4000 cm <sup>-1</sup> below the <sup>1</sup>G, <sup>1</sup>D and <sup>1</sup>S levels, each group being fairly compact. This curious alternating arrangement of energy levels finds a parallel in pentads of similar origin in other spectra, but it is quite contrary to Hund's energy rules and has only recently received any theoretical explanation.

All the triplet terms of Sc II are erect, and most of them obey the interval rule well (Fig. 15 9)

Configuration	Inter	rval	Interval quotient
3d 4s	$\begin{array}{cccc} \Delta^3 D_{1 & 2} \\ \Delta^3 D_{2 & 3} \end{array}$	67 7 109 9	33 8 36 6
3d²	$\Delta^3 F_{2\ 3} \atop \Delta^3 F_{3\ 4}$	80 7 104 2	26 9 26 0
3d²	$\Delta^{3}P_{0}$ 1 $\Delta^{3}P_{1}$ 2	27 4 52 9	27 4 26 4

Fig 15 9. Interval rule in the low terms of Se  $\pi$ 

Three electrons Sci, Yi, Lai, Lui, Tiii, Zrii, Ceii, Hfii The ground terms of the arc spectra of scandium, yttrium and lutecium are d s²²D, while the usual subsidence of the d relative to the sorbit produces d² s³F in the spark spectra of titanium and

#### Low terms

		Sc	Y	La	Lu	Tı m	Zr II	Сеп	Hfп
3d 4s2	<sup>2</sup> D <sub>1</sub>	168	530	1053	1994	25,193	18,397	420	_
3d2 4s	4F.	11,677	11,532	4122	_	393	1,323	1923	78362
	*Pai	<u></u>	15,477			10,025	8,058	1870	
}	2(+.,	20,237	18,499	_		15,258	14,190		
	2 F'21	15,042	15,864	_	_	4,898	6,468	_	
	~ 1 /	17,013	16,159			8,744	4,505		<sup>9</sup> 3051
	2 P. 1		19,406	=		16,625	6,112	_	
	"D+	_		—	_	21,338	25,202	- /	
3d³	4T.	33,906	29,843	<u> </u>	_	1,216	3,758	_	_
	*P.1	1 30.073	32,366	—	_	9,518	9,969		_
		_		-		12,775	12,360		
	44			_		9,118	8,153		
	-F-01		_	-	_	20,892	19,433		
1	-D11	30.330	-	-		12,758	14,733		
	4 1)	_		_	_	_	14,163		
	${}^{2}P_{1\frac{1}{4}}^{2\frac{1}{4}}$	_		-		9,976	20,080	- 1	

Fig 15 10 Three electrons Energies of the low terms

zirconium It has been suggested that the ground term of Hf  $\Pi$  is  $d^2$  s  $^2D$ , but this irregularity still awaits confirmation

The low terms predicted by theory are collected in Fig 15 10, every one of these terms has been found in Zrii, while all the odd terms have been found in Yi, thus once again the great power of Hund's theory is demonstrated. The greatly increased complexity of Sci and Yi compared with Scii and Yii is perhaps so obvious that it hardly deserves mention

T.nen	terms
шош	LET TILS

Configuration	Terms		
	Quartets	Doublets	
3d 4s <sup>2</sup> 3d <sup>3</sup> 4s 3d <sup>3</sup>	PF PF	D SPDGF PDFGH	

#### Middle terms

Ion		Atom				
<i>l</i> <sub>1</sub> <i>l</i> <sub>2</sub>	Term	l <sub>a</sub>	Terms	l <sub>1</sub> l <sub>2</sub> l <sub>3</sub>		
461	1S	4p	2P	s <sup>2</sup> p		
3d 4s	¹D	4p 4p	*(PDF)	d sp		
3dª	*F *P 'G 'D	4p 4p 4p 4p 4p	4(DFG) 4(SPD) 2(FGH) 2(PDF) 2P	d² p		

Fig 15 11 Terms predicted from three electrons

The lines due to transitions from high to middle terms are, in the spectrum of Y I, so much weaker when the terms are doublet than when quartet, that very few high doublet terms have been identified.

Four electrons. Til, Zri, Hfi, Vii, Chii

The arc spectra of titanium, zirconium and hafnium all have as ground term <sup>3</sup>F<sub>2</sub> of the d<sup>2</sup> s<sup>2</sup> configuration, but the d orbit evidently falls abruptly relative to the s at this point, for the spark spectra seem to have d<sup>4</sup> D as ground term

The spectra of titanium and zirconium have been very thoroughly analysed at the Bureau of Standards by Russell and Kiess, and almost all the low terms from the d<sup>2</sup> s<sup>2</sup> and d<sup>3</sup> s configurations have been identified. In their analysis of hafnium

#### Low terms

	Tı	Zr	Hf	V m	Cb 11
3d2 4s2 3F4	387	1,241	4568		
<sup>3</sup> P <sub>2</sub>	8,602	4,186	8984		
1(7.	12,118	8,057			
1 1)	7,255	5,101	5639	_	
1S <sub>0</sub>	15,167	13,142	-		-
3d3 4s 5F5	6,843	5,889	<b>—</b>	3,163	4147
, он'.	11,777	12,342	_	9,097	_
1 P-	14,106	11,258	_	13,741	-
8P.	18,912	15,932	-	_	_
۰ н.	18,193	15,120	-	20,363	
1HT	20,796	18,739		_	_
3(7.	15,220	12,773		14,655	-
1 1(3.	18,288	17,753	—	_	
*F4		15,700	l —		<u> </u>
<sup>1</sup> F <sub>3</sub>	29,818		—	l —	- 1
( 8)).	17,540	14,697		_	
1 1).	20,210	17,228	_	<u> </u>	
1 3D.	_		_	_	- 1
1 1).	-			_	- 1
8P.	18,145	17,143	_		
<sup>1</sup> P <sub>1</sub>	20,063		-		_
3d4 5D4	_	22,398		339	1225
1 8H.	l —	<u> </u>	_	_	- 1
3(7-	36,201	l —	_	16,532	I — I
3F.	<u> </u>	-		13,608	
°F.			l —	<b>—</b>	
31).		_		_	
8P.			_	11,908	_ _ _ _
<sup>3</sup> P <sub>2</sub> <sup>2</sup>	_		_	<u> </u>	-

Fig 15 12 Four electrons Energies of the low terms.

Meggers and Scribner had to rely on wave-lengths and furnace intensities only, but this has not prevented them from identifying seven even and 63 odd terms. From a study of the observed combinations, J values have been assigned and the suggestion put forward that the lowest three terms are  $d^2 s^2 F$ . The J values would allow the next terms to be  $^1D_2$  and  $^3P$ , and this allotment would make the low terms very similar to those of Tii, but further discussion must wait on the promised measurements of the Zeeman effect

Among the odd terms those due to the configuration d<sup>2</sup> sp lie lowest in the arc spectra, but terms from the two other configurations have been recognised

Numerous combinations have been found between both singlet and triplet terms, and between triplet and quintet terms, but very

#### Low terms

Configuration		Terms	
Comiguration	Quintet	Triplet	Singlet
3d² 4s² 3d² 4s	PF	PF PDFGH	SDG PDFGH
3d4	D	PDFGH	SDFGJ 22 2

#### Middle terms

Ion		Atom		
l <sub>1</sub> l <sub>3</sub>	Term	14	Terms	l1 l4
3d* 4s	4F 4P 2G 2F 2D 2P 2S	<b>4</b> p	5,3(DFG) 5 2(SPD) 8,1(FGH) 8,1(DFG) 8 1(PDF) 8,1(SPD) 8,1P	d² sp
3d³	4F 4P 2H 2G 2F 2D 2D 2P	<b>4</b> p	5,8(DFG) 5,8(SPD) 8,1(GHI) 8,1(FGH) 8,1(DFG) 8,1(PDF) 8,1(PDF) 8,1(SPD)	d₃ p
3d 4s2	2D	<b>4</b> p	8,1(PDF)	d s²p

Fig 15 13. Terms predicted from four electrons.

few between singlets and quintets, and even these few are all susceptible of the same explanation. When two terms of the same configuration and the same J have nearly the same energy, they share both their intensities and their g values. Thus  $d^3 p^1D_2^\circ$  combines with the low even  $^5D_3$  term because the former lies very near to the  $^5P_2^\circ$  term of the same configuration, the empirical g values of the  $4d^3$   $5p^1D_2^\circ$  and  $^5P_2^\circ$  terms of Zr1 are both  $1\cdot 42$ ,

whereas the Landé values are 1 000 and 1 833 respectively, their respective energies are 34,850 and 34,761 cm  $^{-1}$ 

Five electrons VI, CbI, CrII, MoII

The ground term of these spectra starts as  $^4F$  of the  $d^3$  s<sup>2</sup> configuration in the iron row, changes to  $^6D$  from  $d^4$  s in the palladium row, and settles down as  $d^5$  s in both the spark spectra, these changes clearly conform to the general type

		Vт	Cb 1	CrII	Моп
3d3 4s2	4F41	553	_	_	_
	$^{4}P_{2\frac{1}{2}}^{4\frac{1}{2}}$	9,825	_		_
3d4 4s	6D.,	2,425	1050	12,498	known
	*H	15,063		30,393	
	*(+	17,242		33,696	
	*15".	15,770		31,221	
	*1Je t	8,716		20,025	known
8	*P.1	15,572	_	_	_
	"P1+	_	_	17,593	_
345	6S	_		0	ground?
	~( ·			20,514	
l.	* H'. 1	_		32,856	_
	~ 1 / 2 1		_	25,035	
	*12.1	_			<del></del>
	$^{2}D_{2\frac{1}{4}}^{2\frac{1}{4}}$	_	_	21,824	_

#### Low terms

Fig 15 14 Five electrons Energies of the low terms

Of the other low terms little is known outside the Cr II spectrum, in which many quartet but only two doublet terms have been found, these doublets are conspicuous in breaking Hund's energy rules, for they lie among the lower of the quartet terms

The odd terms are best developed by the addition of a p electron to the lowest terms of the parent spectrum, in this way a number of triads are formed, and these agree very satisfactorily with the terms found empirically. Thus in VI there occur a triad of sextet terms at 18,000 cm $^{-1}$  and a triad of quartet terms at about 22,000 cm $^{-1}$ , the J values show that in fact these are the two triads  $^6(\mathrm{DFG})^\circ$  and  $^4(\mathrm{DFG})^\circ$  which should arise by the addition of a p electron to the low d³ s  $^5\mathrm{F}$  term of VII

Of all these five electron spectra CrII has been the most thoroughly analysed, and in it nearly all the terms both obey the interval rule reasonably well and have normal g values. The  $^6\mathrm{D}^\circ$  and  $^4\mathrm{P}^\circ$  terms of the  $\mathrm{d}^4$  p configuration are irregular judged by either criterion, but a term which deviates from one rule, often deviates from the second as well

Low terms

Configuration	Terms  Sextet Quartet Doublet				
3d <sup>3</sup> 4s <sup>2</sup>	_	PF	PDFGH		
3d4 4s	D	PDFGH	SDFGJ		
3d <sup>5</sup>	S	PDFG	SPDFGHJ		

Middle terms

	Ion	Atom				
$l_1$ $l_4$	Term	$l_{5}$ Terms $l_{1}$ $l_{5}$				
d <sup>4</sup> d³s	₽E. ₽D	p p	<sup>6,4</sup> (PDF) <sup>6,4</sup> (DFG)	$\frac{\mathrm{d}^4}{\mathrm{d}^3}$	p sp	

Fig 15 15 Terms predicted from five electrons

Six electrons Cri, Moi, Wi, Mnii

The analysis of these spectra has hardly extended beyond the septet and quintet systems, only a few triplets having been found, and no singlets though these undoubtedly occur. The arc spectra of chromium and molybdenum and the spark spectrum of manganese all have d<sup>5</sup> s <sup>7</sup>S as ground term, in contrast the ground term of tungsten is probably <sup>5</sup>D, but the analysis is so little advanced

Low terms

	Crı	Мог	Wт	Mn II
3d4 4s2 5D4	8,307	12,346	6219	_
3d <sup>5</sup> 4s <sup>7</sup> S <sub>3</sub> <sup>5</sup> S <sub>2</sub> <sup>5</sup> G <sub>6</sub>	7,593	10.700	2951	0
5G <sub>6</sub>	20,519	10,768 16,828	_	9,473
<sup>5</sup> F <sub>5</sub> <sup>5</sup> D <sub>4</sub>	24,282		_	
$^{5}P_{3}$	21,841	18,229	_	
3d6 5D4		_	_	14,324

Fig 15 16 Six electrons Energies of the low terms



that this cannot be surely assigned to the  $d^4\,\,\mathrm{s}^2$  as against the  $d^6\,$  configuration

### Low terms

Con	Terms					
figuration	Septet	Quintet	Triplet	Singlet		
3d4 4s2	D	D	PDFGH	SDFGJ		
3d <sup>5</sup> 4s	s	SPDFG	SPDFGHJ	SPDFGHJ		
3d <sup>6</sup>	_	D	PDFGH	SDFGJ 222		

#### Middle terms

Ion			Atom	
$l_1$ $l_5$	Term		Terms	$l_1$ $l_6$
3d <sup>3</sup> 4s <sup>2</sup> 3d <sup>4</sup> 4s 3d <sup>5</sup>	<sup>4</sup> F <sup>6</sup> D <sup>6</sup> S	4p 4p 4p	5,3(DFG) 7 5(PDF) 7P 5P	$egin{array}{c} \mathbf{d^3 \ s^2p} \ \mathbf{d^4 \ sp} \ \mathbf{d^5 \ p} \end{array}$

Fig 15 17 Terms predicted from six electrons

The list of low terms is complete, but the middle terms are developed from the low terms of the spark spectrum, a complete list would be so long as to give no guidance at all

## Seven electrons Mni, Rei, Fen, Run

The ground term of the arc spectra of manganese and rhenium is  $d^5$  s<sup>26</sup>S, but it changes first to  $d^6$  s <sup>6</sup>D and then to  $d^7$  4F in the spark spectra of iron and ruthenium respectively, thus once again the d orbit is seen to sink relative to the s orbit, when we pass from one period to the next or from an arc to a spark spectrum

#### Low terms

		Mn	Re	Fe 11	Run
3d <sup>5</sup> 4s <sup>2</sup>	6S	0	0	23,318	_
3d <sup>6</sup> 4s	<sup>6</sup> D <sub>41</sub> <sup>4</sup> G <sub>51</sub> <sup>4</sup> F <sub>41</sub> <sup>4</sup> D <sub>31</sub>	17,052	11,754	0	9,151
	4G <sub>5</sub>			25,429	<u> </u>
	4F41			22,637	_
	$^4D_{31}$	23,297	_	7,955	19,379
	$^4P_{2\frac{1}{2}}$	_	_	20,830	_
3d7	<sup>4</sup> F <sub>4</sub> <sup>4</sup> P <sub>2</sub>	_	_	1,873	0
	4P.	_	_	13,474	8,257
	2F34		_	<u> </u>	22,289

Fig 15 18 Seven electrons Energies of the low terms

The ground term of Mn I has been recently confirmed by showing that all the resonance lines arise from jumps ending in the <sup>6</sup>S state \*

Io	1		Atom			
$l_1$ $l_6$	Term	$l_{7}$	Terms	l1 l7		
d⁵ s	7S	s d	6S 8D	$d^5$ $s^2$ $d^6$ $s$		
	5S	s d	<sup>6</sup> S (as above) <sup>6</sup> D (as above) <sup>4</sup> D	d <sup>5</sup> s <sup>2</sup> d <sup>6</sup> s		
d4 s2	5D	d	<sup>6</sup> S (as above) <sup>4</sup> (PDFG)	d <sup>5</sup> s <sup>2</sup>		

Fig 15 19 Low terms of Mn I developed from the low terms of Mn II

Configuration		Terms	
	Sextets	Quartets	Doublets
3d <sup>5</sup> 4s <sup>2</sup>	S	PDFG	SPDFGHJ
3d <sup>6</sup> 4s	D	PDFGH	SDFGJ
3d <sup>7</sup>	_	2 2 2 PF	$\Pr^{2\;2}_{\mathbf{DFGH}}$

#### Middle terms

Io	Ion		Atom	
l <sub>1</sub> l <sub>6</sub>	Term	l <sub>7</sub>	Terms	l <sub>1</sub> l <sub>7</sub>
d <sup>5</sup> s	7S 5S	p p	<sup>8</sup> P <sup>6</sup> P <sup>6</sup> P <sup>4</sup> P	d <sup>5</sup> s p
d4 s2	5D	р	<sup>8</sup> 4(PDF)	d4 s2 p
d <sup>6</sup>	⁵D	р	6,4(PDF)	d <sup>6</sup> p

Fig 15 20 Terms predicted from seven electrons

With the increasing number of electrons, even the low terms become so complex that they are not easily identified, to meet this difficulty the low terms may be developed from the lowest terms of the spark spectrum, just as the odd terms have been developed. Thus in Fig. 15-19 there are only a few terms where in Fig. 15-20 there is a huge mass.

<sup>\*</sup> Fridrichson, ZP, 1930, 64 43

Since the ground term of the spark spectra of Mn and Re is <sup>7</sup>S, series are to be expected in the arc spectra, and in fact Catalan\* did first analyse Mn i into a number of series. The lowest terms of the odd series are shown in Fig. 15 20

The terms of these spectra are nearly all inverted, while those of Ru  $\Pi$  show very regular g values

## Eight electrons Fei, Rui, Com

The ground term of the arc spectrum of iron is d<sup>6</sup> s<sup>2</sup> <sup>5</sup>D, but the ground term changes in the normal way to d<sup>7</sup> s <sup>5</sup>F and then to d<sup>8</sup> <sup>3</sup>F in the arc spectrum of ruthenium and the spark spectrum of cobalt respectively.

Low terms						
		<b>F</b> e 1	Ruı	Соп		
3d <sup>6</sup> 4s <sup>2</sup>	<sup>5</sup> D <sub>4</sub>	0	° 7,483	_		
$3d^7 4s$	${}^{5}\mathrm{F}_{5} \\ {}^{5}\mathrm{P}_{3} \\ {}^{3}\mathrm{F}_{4} \\ {}^{8}\mathrm{P}_{2}$	6,928	0	3,350		
	$^{5}P_{3}$	17,550	9 8,771	17,771		
	$^3\mathbf{F_4}$	11,976	6,545	9,813		
	$^{8}P_{2}^{-}$	22,838	·—			
$3d^8$		_	9,120	0		
	$^3\mathrm{F}_4$ $^3\mathrm{P}_2$		910,623	_		

Low terms

Fig 15 21 Eight electrons Energies of the low terms

Ion		Atom				
$l_1$ $l_7$	Term	l <sub>8</sub> Terms		$l_1$ $l_8$		
d <sub>6</sub> s	6D	s d	<sup>5</sup> D <sup>5</sup> (PF)	d <sup>6</sup> s <sup>2</sup> d <sup>7</sup> s		
	4D	s d	<sup>5</sup> D (as above) <sup>3</sup> (PDFG) <sup>5</sup> (PF) (as above) <sup>3</sup> (PDFG)	d <sup>6</sup> s <sup>2</sup> d <sup>7</sup> s		
d <sup>7</sup>	1F	s d	<sup>5</sup> F <sup>3</sup> F <sup>3</sup> (PF)	d <sup>7</sup> s d <sup>8</sup>		
	<sup>4</sup> P	s	5P 3P	d <sup>7</sup> s		
		d	³(PF) (as above)	d <sup>8</sup>		

Fig 15 22 Low terms of Fe i developed from the low terms of Fe ii

Hund's theory predicts for the  $d^6$  s<sup>2</sup> configuration one quintet and seven triplet levels besides a number of singlets. In the iron

<sup>\*</sup> Catalan, Phil Trans RS, 1922, 223 127.

are the <sup>5</sup>D term is inverted and follows the interval rule fairly well, as the following table shows (Fig. 15 24)

#### Low terms

		Terms	
Configuration	Quintet	Triplet	Singlet
3d8 4s2	D	PDFGH	SDFGJ
3d7 4s	PF	PDFGH	PDFGH
3d8		PF	SDG

#### Maddle terms

Io	Ion		Atom	
l <sub>1</sub> l <sub>7</sub>	Term	$l_8$	Terms	$l_1$ $l_8$
d <sup>6</sup> s	6D	p	7,5(PDF)	d <sup>e</sup> s p
	4D	p	5,8(PDF)	d <sup>6</sup> s p
d <sup>7</sup>	4 <b>F</b>	p	5,3(DFG)	d <sup>7</sup> p
	4P	p	5,8(SPD)	

Fig 15 23 Terms predicted from eight electrons

Interval $\Delta E/ch$	A
89 9	89 9
184 1	92 1
288 1	96 0
415 9	104 0
	89 9 184 1 288 1

Fig 15 24 Intervals of the d<sup>6</sup> s<sup>2</sup> <sup>5</sup>D term of Fe 1

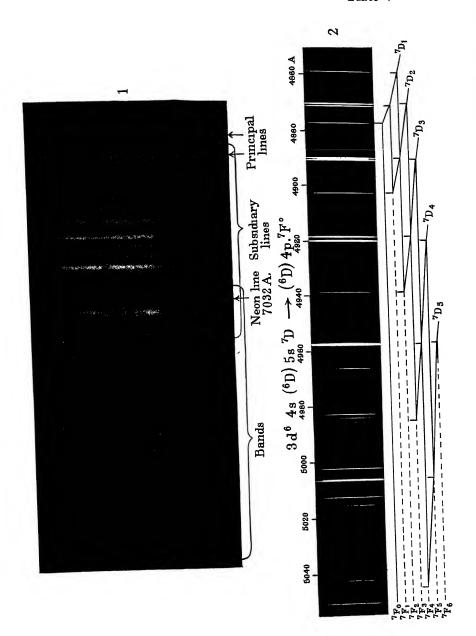
Of the triplet levels, only four have been found, these are all inverted and obey the interval rule about as well as the <sup>5</sup>D term Goudsmit's theory of the displacement sum predicts that the <sup>3</sup>D term will be erect, but the term is still unidentified.

The other low configuration of the iron arc is d<sup>7</sup>.s, the four terms so far identified being clearly produced by an s electron adding itself to the d<sup>7</sup> F and 4P terms, for the derivation is in-



### PLATE V

- I Fluorescent spectrum of chromium in  ${\rm Al_2O_3}$  at  $-186^{\circ}$  C At the right-hand or blue end of the spectrum a strong principal doublet appears, a thousand times over-exposed. Next to these are the subsidiary lines, weaker but shaip, while on the left are still weaker bands. The line near the centre is the 7032 A of neon. (After Deutschbein, PZ, 1932, 33 875.)
- 2 DF septet from the iron arc This multiplet arises as  $3d^6$  4s ( $^6D$ ) 5s  $^7D \rightarrow$  ( $^6D$ ) 4p  $^7F^\circ$  (Lent by Prof H Dingle)





dicated both by the energies and the intervals of the terms. In the spark <sup>4</sup>F lies 11,000 cm <sup>-1</sup> below <sup>4</sup>P, and in the arc <sup>5</sup>F and <sup>3</sup>F lie about the same distance below the corresponding <sup>5</sup>P and <sup>3</sup>P terms. Again, <sup>4</sup>F obeys the interval rule well, while the derived <sup>5</sup>F and <sup>3</sup>F terms do not deviate much (Fig. 15.25). But the ionic <sup>4</sup>P term is quite inegular and so are the derived terms of the arc spectrum, even the irregularities are similar (Fig. 15.26).

Term	$\Delta E/eh$		Term	$\Delta E/\epsilon h$	A	Term	$\Delta E/ch$	A
ek' ek' ek' ek'	168 9 257 7 351 3 488 5	81 5 85 9 87 8 97 7	3F <sub>2</sub>	407 6 584 7	135 9 146 2	4F <sub>1</sub> ; 4F <sub>2</sub> ; 4F <sub>3</sub> ; 4F <sub>4</sub> ;	279 6 407 7 557 6	111 8 116 5 123 9

Fig. 15.25 Intervals of the  $d^7$  (\$F) s 5, \$F terms of Fe I and the  $d^7$  \$F term of Fe II

Term	\(\Delta E \) (h	1	Term	$\Delta E/\epsilon h$	A	Term	$\Delta E/\epsilon h$	A
nl,' 'l,' nl,'	200 4 176 8	100 2	3P <sub>0</sub> 3P <sub>1</sub> 3P <sub>2</sub>	1019	104 9 54 2	4P <sub>4</sub> 4P <sub>11</sub> 4P <sub>21</sub>	231 7 198 7	154 5 79 5

Fig 15 26 Intervals of the d7 (4P) s 5.3P terms of Fe I and the d7 4P term of Fe II

A very large number of odd terms have been identified and named in the spectra of Fer and Con, for the terms satisfy the simple laws, their intervals are regular, and almost without exception they are inverted. But the terms of Rur are much less regular, so that a thorough Zeeman analysis was necessary before the terms could be mamed, and even now only a J value has been assigned to very many, the interval law is only roughly satisfied

Nine electrons. (501, Rhi, Niii, Pdii

The ground term starts as  $d^7$  s<sup>24</sup>F in the arc spectrum of cobalt, changes to  $d^8$  s<sup>4</sup>F in the arc spectrum of rhodium and finishes as  $d^{92}$ D in the spark spectra of nickel and palladium,

Low terms

	Со 1	Rhı	N1 II	Pd II
3d7 4s2 4F44	0	12,733	_	_
4P01	15,184	_	_	=
2 F'01	_	_	_	_
<sup>2</sup> P <sub>1½</sub>	20,501	_	_	-
3d8 (3F) 4s 4F.,	3,483	0	8,393	25,081
2F <sub>8±</sub>	7,442	5,691	13,549	32,278
(3P) 4s 4P <sub>2</sub>	13,795	9,221	25,035	36,281
<sup>2</sup> P <sub>1</sub>	18,390	11,968	29,069	43,648
(¹G) 4s ²G <sub>4½</sub>	16,468	16,018	32,498	44,506
( <sup>1</sup> D) 4s <sup>2</sup> D <sub>2</sub>	16,778	13,521	23,107	41,198
(1S) 4s 2S <sub>1</sub>	_	_	24,825	-
$3d^9$ $^2D_{2\frac{1}{4}}$	21,920	3,310	0	0

### Middle terms

	Cor	Rhı	Nı 11	Pdп
$3d^{7}$ 4s ( <sup>5</sup> F) 4p $^{6}G_{6\dagger}$ $^{6}F_{5\dagger}$ $^{6}D_{4\dagger}$ $^{4}G_{5\dagger}$ $^{4}F_{4\dagger}$ $^{4}D_{3\dagger}$	25,138 23,612 24,628 28,845 28,346 29,294			_ _ _ _
$^{(3F)}_{4p}$ $^{4G_{51}}_{4F_{4+}}$ $^{4F_{4+}}_{4D_{31}}$ $^{2G_{4+}}_{2F_{3+}}$ $^{2F_{3+}}_{2D_{21}}$	41,528 41,225 39,649 31,700 31,871 33,463		91,797 — 93,525	_ _ _ _
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	32,431 32,842 32,027 33,440 35,451 36,092	29,105 29,431 27,076 31,614 32,004 32,046	53,495 54,556 51,557 55,299 57,079 57,419	68,611 69,878 65,247 72,285 73,327 72,733
( <sup>3</sup> P) 4p <sup>4</sup> D <sub>31</sub> <sup>4</sup> P <sub>21</sub> <sup>4</sup> S <sub>11</sub> <sup>2</sup> D <sub>21</sub> <sup>2</sup> P <sub>21</sub> <sup>2</sup> P <sub>11</sub> <sup>2</sup> S <sub>1</sub> <sup>2</sup> S <sub>2</sub> <sup>2</sup> S <sub>1</sub> <sup>2</sup> S <sub>2</sub>		36,787 35,334 — — — —	70,776 66,569 74,299 71,770 72,984 74,282	83,056 76,767 86,280 83,802 85,151 85,071
$^{(1G)}_{4p}$ $^{2}_{15}_{5}$ $^{2}_{64}_{1}$ $^{2}_{7}_{3}$	=	<del>-</del>	75,719 79,923 ?75,916	85,593 89,982 86,043
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-	=	67,693 68,634 68,864	79,708 82,057 80,956
( <sup>1</sup> S) 4p <sup>2</sup> P <sub>1</sub>	<u> </u>		60,502	

Fig. 15 27 Nine electrons Energies of the low and middle terms

moreover, whereas the ground  $^2\mathrm{D}$  term is only  $8000~\mathrm{cm}^{-1}$  below the next lowest term in  $N_{1}\pi$  it is 25,000 cm  $^{-1}$  in  $Pd\pi$  These changes are in the usual order

The energies of the low and middle terms are always related, but no group of electrons shows these relations more clearly than the group of nine here considered In CoI the ground term is of the 3d7 4s2 configuration and the lowest odd terms are derived

Low	terms

Conference	Terms				
Configuration	Quartet	Doublet			
3d7 4s2	PF	PDFGH			
3d <sup>8</sup> 4s 3d <sup>9</sup>	PF —	SPDFG D			

### Middle terms

Ior		Atom			
$l_1$ $l_8$	Term.	Term l <sub>9</sub> Term		$l_1$ $l_9$	
d <sup>8</sup>	3E	p	4 2(DFG)	d <sup>8</sup> p	
	*P	p	4,2(SPD)		
d's	*F	p	6,4(DFG)	d <sup>8</sup> sp	
	<sup>5</sup> P	p	6 4(SPD)		

Fig 15 28 Terms predicted from nine electrons.

from  $3d^7$  4s 4p, on the other hand, when the ground term is from  $d^8\,$  s as it is in Rh i or from  $d^9$  as in Ni II and Pd II, practically all the known odd terms are from  $d^8\,\,p\,\,$  Agam, in  $N_1\pi$  the energies of the even and odd terms run strikingly parallel, of the  $3d^8$  4s configuration <sup>2</sup>D and <sup>2</sup>S he exceptionally low, and this is matched among the odd terms by the anomalous positions of 2(PDF) and <sup>2</sup>P from 3d<sup>8</sup> p Presumably these two irregularities have a common cause in the  $\rm d^{81}D$  and  $\rm d^{81}S$  terms of N1III, but unfortunately the latter spectrum has not yet been analysed

In  $N_{1}\Pi$  all but one of the low even terms are inverted, but of the odd  $d^8$  p configuration eight terms are erect or only partially inverted In Pdn the intervals are rather irregular 5

Ten electrons Nii, Pdi, Pti, Cuii, Agii, Auii, Cdiii, Hgiii, Iniv, Tliv

The ground term of all the spark and higher spark spectra is d<sup>10</sup> <sup>1</sup>S, but the arc spectra exhibit two irregularities. Thus the ground term of nickel is 3d<sup>8</sup> 4s<sup>2</sup> <sup>3</sup>F, although the ground term of Ni II is 3d<sup>9</sup> <sup>2</sup>D and the ground term of an arc spectrum is usually obtained by adding an electron to the ground term of the spark, the only other exception to this rule seems to be Y II. Again, if the ground terms of nickel and platinum are respectively d<sup>8</sup> s<sup>2</sup> <sup>4</sup>F and d<sup>9</sup> s <sup>4</sup>F, the ground term of palladium might be expected to be one or the other of these, whereas in fact it is d<sup>10</sup> <sup>1</sup>S

#### Low terms

		N1 1	Pd 1	Ptı	Cu II	Agп	Aun
3d8 4s2	3F.4	0	25,101	824	_	_	_
	<sup>3</sup> P <sub>2</sub>	15,610 22,102	37,952 —	6,567 21,967	_	=	=
	<sup>3</sup> P <sub>3</sub> <sup>1</sup> G <sub>4</sub> <sup>1</sup> D <sub>2</sub> <sup>1</sup> S <sub>6</sub>	13,521	=	26,639 —	=	_	=
3d9 4s	<sup>1</sup> D <sub>3</sub>	204 3,410	6,564 11,722	0 13,496	21,925 26,261	39,164 46,045	15,036 29,618
3d10	<sup>1</sup> S <sub>0</sub>	14,729	0	6,140	0	0	0

Fig 15 29 Ten electrons Energies of the low terms

#### Low terms

C C	Terms			
Configuration	Triplet	Singlet		
d <sup>8</sup> s <sup>2</sup> d <sup>9</sup> s d <sup>10</sup>	PF D —	SDG D S		

### Maddle terms

Ior	L	Atom			
$l_1$ $l_2$	Term	l <sub>10</sub> Terms		$l_1$ $l_{10}$	
q <sub>a</sub>	<sup>2</sup> D	p	8 1(PDF)	d <sup>9</sup> p	
d <sup>8</sup> s	4F 2F	p p	**************************************	d <sup>8</sup> sp	

Fig 15 30 Terms predicted from ten electrons

The changes in the arc spectra in passing from row to row are also instructive, in Nii the term separations are wide and the multiplets overlap, but, though complex, the spectrum is admirably regular, all the even terms and nearly all the odd terms are inverted, and the intervals conform to Landé's rule, so simple was the analysis indeed that the Zeeman effect has not been studied In the PdI spectrum the wide interval, 3512 cm -1, of the 2D ground term of Pdn begins to exert an effect, as some triplet series tend to the lower and some to the higher limit, the interval ratios change rapidly with the serial number And the terms of Ptr are even less regular than those of Pdr, in analysis the interval rule is useless, and the intensity rules can be treated only as approximations, the measurements of g, too, depart from Landé's values, but they suffice with the J selection rule to determine the J value of all the empirical terms. The determination of the orbital and spin vectors is, however, far more difficult, for the failure of the simple rules is a sure sign that the coupling is no longer Russell-Saunders However, all the low terms predicted from d8 s2, d9 s and d10 seem to have been identified, save only d8 s21S, which has not yet been found in any spectrum Names have also been assigned to some of the odd terms arising from the d8 sp and d9 p configurations

In Cu II and Ag II the terms are generally inverted, but the interval rule is very badly satisfied, in Ag II irregular g values are also indicated

In the analysis of PdI there is a surplus level, known as  $k_1$ , which is of interest chiefly as being the only level which fails to fit into the Hund scheme. The level is determined by five exact combinations, but the lines due to  $k_1$  are all listed as diffuse and differ in this from all other lines of the palladium spectrum, the level can hardly be a hyperfine component, for no other levels show a similar structure, and the interval separating it from the nearest normal level is over 3 cm<sup>-1</sup>

Eleven electrons Cui, Agi, Aui, Znii, Cdii, Hgii

As the d level can hold only ten electrons, the elements copper, silver and gold, which have eleven electrons outside the last mert

gas shell, should exhibit the simple alkali spectra provided only that d<sup>10</sup> is firmly bound. In fact all three elements do exhibit doublet series and they all have a <sup>2</sup>S ground term. But besides

#### Low terms

	Cu 1	Agı	Auı	Zn II	Cd 11	Hgп
3d <sup>9</sup> 4s <sup>2</sup> <sup>2</sup> D <sub>21</sub>	11,203	<u> </u>	9161	62,721	69,259	35,514
3d <sup>10</sup> 4s <sup>2</sup> S <sub>1</sub>	0		0	0	0	0

Fig 15 31 Eleven electrons Energies of the low terms

this simple system, which was discovered in very early days, the last decade has revealed in copper and gold other quartet and doublet terms, in silver these terms have not been found, though all the lines of AgI have been classified \*

Cu	+		Cu				
l <sub>1</sub> l <sub>10</sub>	Term	l <sub>11</sub>	Terms				
3d10	1S	s	2S				
		P	²P°	Alkalı-lıke systems			
		đ	2D				
3d9 4s	\$D 1D	4s	2D	Deep even term			
	3D	4p	4(PDF) 2(PDF)	Middle group of odd			
	1 <b>D</b>	4p	²(PDF)	voi ma			
	*D	ns	4D 2D				
		nd	4(SPDFG) 2(SPDFG)	High even terms			
	¹D	ns	²D				
		nd	²(SPDFG)				

Fig 15 32 Terms predicted in copper

The lowest term of  $Cu\pi$  is  $d^{10\,1}S$ , and from it arise by the addition of s,p and d electrons the alkali-like system, from the  $^3D$  and higher  $^1D$  terms of  $Cu\pi$  arise all the other known terms, those predicted are shown in Fig. 15-32, while those actually found are

<sup>\*</sup> Blair, PR, 1930, 36 1531

arranged to their proper ionic limits in Fig. 15 33. In both the  $(^{3}D)$  ns  $^{2}D$  and the  $(^{1}D)$  ns  $^{2}D$  series two terms are known, and the

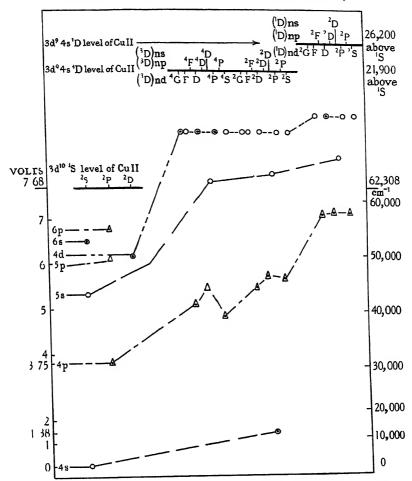


Fig. 15.33 Level diagram of copper. The even terms are shown by circles, the odd terms by triangles

Rydberg formula then determines the height of the  $^3\mathrm{D}$  series limits above the  $^1\mathrm{S}$  limit as 22,200 cm  $^{-1}$ 

In gold the deep <sup>2</sup>D term has been found and also some higher terms, but as the coupling is roughly of the (11) type only the five lowest terms can be named

The contrast between copper and gold on the one hand and silver on the other appears not only in their spectra but also in their chemical properties. Both copper and gold can be monovalent, but copper is commonly divalent and gold may be trivalent, showing that the lower electron group is not as firmly established as in the alkali metals, silver on the other hand is always monovalent.

# 4. The three rows compared

The structure of a spectrum is primarily a function of the number of electrons, but it is also affected by the relative positions of the low terms, for they will determine which multiplets appear bright and which faint Usually the ground term changes from frame to frame, and when this happens in a spark spectrum, even the prominent multiplicaties of the arc spectrum change. In the Fer spectrum triplets, quintets and septets are known, but in the homologous Rui only triplets and quintets, Coi has doublets, quartets and sextets, but Rh1 only doublets and quartets, N11 has singlets, triplets and quintets, but PdI only singlets and triplets And the reasons for these differences are not far to seek, the ground term of Fe  $\pi$  is d<sup>6</sup> s <sup>6</sup>D, but of Ru  $\pi$  d<sup>7</sup> <sup>4</sup>F, and if the ground terms of Ni II and Pd II are identical, as presumably are also the ground terms of Co  $\pi$  and Rh  $\pi$ , though Rh  $\pi$  has not yet been analysed, the d\* s\*F term lies so much lower in N1 $\pi$  than  ${
m in}\,{
m Pd}\,{
m II}$  that terms derived from it appear in one arc spectrum and not in the other

Since the energies of the three low configurations are of such importance, they are worth detailed consideration. Relative energies alone are known, and we therefore elect to consider the energies of the  $s^2$   $d^{n-2}$  and  $d^n$  configurations relative to s  $d^{n-1}$ , since the last has been identified in more spectra than either of the other two. Many figures are still missing from the tables, but a fair sequence of  $s^2$   $d^{n-2}$  is available in the arc spectra of the iron and palladium rows, while rather less complete sequences for  $d^n$  are found in the spark spectra of the same rows, accordingly ( $s^2$   $d^{n-2}-s$   $d^{n-1}$ ) and (s  $d^{n-1}-d^n$ ) are plotted against n for the arc (Fig. 15.34) and spark (Fig. 15.35) spectra respectively.

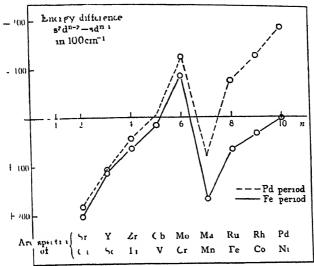


Fig. 15.34. The energy difference of the  $s^2$   $d^{n-2}$  and s  $d^{n-1}$  configurations in the are spectra of the iron and palladium frames. n is the number of electrons outside the mert gas shell. Due to a slip in diafting the energy scales of this and the two succeeding figures read down instead of up.

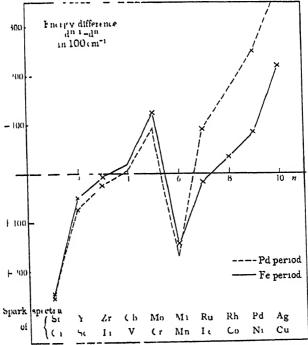


Fig 15.35 The energy difference of the s  $d^{n-1}$  and  $d^n$  configurations in the spark spectra of the non and palladium frames

the curves for the iron and palladium rows would resemble one another might have been anticipated, but the resemblance between the ( $s^2 d^{n-2}-s d^{n-1}$ ) and ( $s d^{n-1}-d^n$ ) differences is altogether surprising, true the first curve is displaced a step to the right relative to the second, but closer examination reveals that

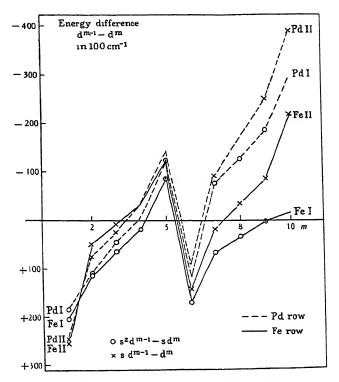


Fig 15 36 The energy difference of the  $d^{m-1}$  and  $d^m$  configurations m is here n-1 in the arc and n in the spark spectra, n is still the number of electrons outside the inert gas shell

the (s<sup>2</sup> d<sup>n-2-s</sup> d<sup>n-1</sup>) curve for the iron row arc actually resembles the (s d<sup>n-1-dn</sup>) curve of the iron row spark more closely than it resembles the (s<sup>2</sup> d<sup>n-2-s</sup> d<sup>n-1</sup>) curve of the palladium row arc The fourfold magnification which occurs in all simple spectra does not affect these low terms at all, though it does still affect the ionisation potentials

To make these facts stand out, write m = (n-1) in the  $(s^2 d^{n-2} - s d^{n-1})$  difference and m = n in  $(s d^{n-1} - d^n)$ , and then plot both the differences  $(s^2 d^{m-1} - s d^m)$  and  $(s d^{m-1} - d^m)$  against m (Fig. 15-36). That the four curves are so very similar can only mean that they all measure essentially the difference between the configurations  $d^{m-1}$  and  $d^m$ , the number of s electrons being of little moment.

The regularity thus revealed enables us to fill up certain gaps in our knowledge, thus in the palladium row, there now seems little doubt that the ground terms of Mai, Maii and Rhii—the

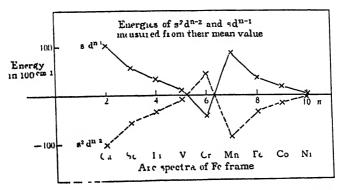


Fig 15.37 Arc spectra of the non-trame. The energies of the  $s^2$   $d^{n-2}$  and s  $d^{n-1}$  configurations measured from their mean value

only spectra whose ground terms are not known—must be d<sup>5</sup> s<sup>2</sup> <sup>6</sup>S, d<sup>5</sup> s <sup>7</sup>S and d<sup>8</sup> <sup>3</sup>F respectively, while if in the platinum row the ground term of W i is <sup>5</sup>D as has usually been supposed, then it must arise from the d<sup>4</sup> s<sup>2</sup> configuration and probably the ground configuration of every are spectrum from Lui to Osi is of the d<sup>n-2</sup> s<sup>2</sup> type. The supposed <sup>2</sup>D ground term of iridium must be accepted with extreme reserve, for it would necessitate a d<sup>9</sup> configuration in the normal atom.

The similarity of the four  $(d^{m-1}-d^m)$  curves further excites a desire to explain at least their more striking features, and in fact Hund has already done this, for if the energies of the  $s^2$   $d^{n-2}$  and s  $d^{n-1}$  configurations are measured from their mean value (Fig. 15.37), the sharp rise of the  $(d^{m-1}-d^m)$  curves at m=5 and

the precipitate drop at m=6 are revealed as both due to the low energy of the  $d^5$  configuration compared with either  $d^4$  or  $d^6$ 

### BIBLIOGRAPHY

As for the short periods, the only systematic account seems to be by Hund in Linienspektren und periodisches System der Elemente, 1927

The values of energy levels are taken largely from Bacher and Goudsmit, Atomic Energy States, 1932 Other statements about particular elements are based on the select bibliography appearing in Appendix VI

#### CHAPTER XVI

### THE RARE EARTHS

# 1 In the periodic system\*

Bohr's theory explains the intrusion of fourteen rare earths into the sixth period as due to the filling of a shell of 4f electrons. Now Bohr's theory also explains the increase in metallic properties which occurs in descending a column of the table as due to the valency electrons occupying orbits of successively higher quantum numbers, while the decrease in metallic properties which occurs in passing across the table from left to right he ascribed to the firmer binding of the electrons as the nuclear charge increases. If these predictions are general, they should be valid in the rare earth elements. Yttrium should be more metallic than scandium, and lanthanum than yttrium, but in passing through the rare earths from lanthanum to lutecium the elements should grow steadily less metallic.

The firmness with which the valency electron is bound is best measured by the ionisation potential, but for most of the rare earths the potential has only been estimated from the conductivities of the oxides in a flame, † and many have felt that the values are not so sure as those obtained by more direct methods. In the last two years this view has been confirmed by the analysis of the spectra of lanthanum and cerium, the ionisation potentials thus obtained are 5 59 and 6 54, which compare with the flame values of 5 49 and 6 91 volts

For confirmation turn first to the molecular volume of homologous compounds, and then to two chemical reactions. The more firmly the valency electrons are bound, the smaller should be the volume of the compound, and in fact this prediction is fulfilled in the sesqui-oxides and sulphates. The sesqui-oxides of the rare earths exist in three crystalline forms, which Goldschmidt named A, B and C A is stable at high temperatures, C at low, but the

<sup>\*</sup> Von Hevesy, Die seltenen Erden, 1926, 21f

<sup>†</sup> Rolla and Piccardi, PM, 1929, 7 286, and Fig 10 13 of Volume I

transition temperature changes from element to element, rising from lanthanum to lutecium, so that at room temperature the form A is stable in lanthanum and the form C in lutecium. The hexagonal crystal A has been measured in four elements between lanthanum and neodymium, the pseudo-trigonal crystal B in four between neodymium and gadolinium, and the regular crystal C in scandium, yttrium and in all the elements which succeed samarium (Fig. 16.1). These measurements show that in the sixth

	Sc	Y	La	Ce	e Pr		Nd		11	Sm	Eu
Sesquioxide $\begin{cases} A \\ B \\ C \end{cases}$	 35 53	_ 45 13	50 28 c 57	47 89 — —	46 65		46 55 c 51 °			46 9 48 38	46 5 48 28
Sulphate octahydrate Element	_	240 8	 22 6					252 4 20 7		247 9 —	247 3 —
	Gd	Tb	D <sup>2</sup>	7   I	H <sub>0</sub> I		Cr	Tu		Yb	Lu
Sesquioxide $\begin{cases} A \\ B \\ C \end{cases}$	c 43 47 58						- 1 38	<u>-</u> 3 44 11			42 25
Sulphate octahydrate Element	246 4	=	242 8		11	239	3	-	_	235 1 19 8	234 7

Fig 16 1 Molecular volumes of some rare earth compounds

period the molecular volume of all three crystal forms decreases as the atomic number increases, while in travelling from scandium through yttrium to lanthanum there is a considerable expansion. These two variations are in the directions predicted by Bohr, together they bring yttrium out with very nearly the same atomic volume as holmium, an interesting coincidence, as a comparison of chemical properties would assign yttrium the same place in the rare earth sequence, the four elements which succeed holmium are thus actually less metallic than yttrium, though still much more metallic than scandium

When the rare earth sulphates crystallise as the octahydrates, all except cerium are isomorphous. Their densities, which have been measured by Auer von Welsbach, show that once again the molecular volume decreases in passing from praseodymium to lutecium, and once again yttrium appears next to holmium.

There are also chemical methods by which the decreasing basicity may be demonstrated. If one measures the iodine liberated in the reaction

 $E_2(SO_4)_4 \cdot 5K1 + K1O_3 + 3H_2O - 2E(OH)_3 + 3K_2SO_4 + 3I_2$ , increase in the iodine is a sign of decreasing basicity. The order in which this reaction places the elements is identical with that obtained from the molecular volumes, while the difference between samarium and europium is abnormally small here as there

Another method is to warm a solution of the sulphate with an exactly equivalent weight of sodium carbonate, and to measure the rate at which carbonic acid is liberated. The order obtained is again the same as that of the molecular volumes. Pr., Nd., Sm., Eu., Gd., Tb., Dy., Y., Tu., Yb.

# 2. Valency

If the periodic system was based solely on chemical grounds, there would be no choice but to crowd all the fifteen elements between lanthanum and lutecium into column III, elsewhere in the periodic system the valency changes by one when the atomic number changes by one, but all fifteen rare earths are trivalent

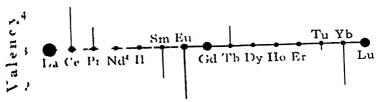


Fig. 16.2. Valencies of the rare earths, all are trivalent, and the size of the point show the relative stability of the ion,  $Me^{14}$ , the appearance of quadrivalent compounds is shown by a line running up, and of divalent compounds by a line running down, the lengths of these lines give a rough measure of stability (After Juntsch and Klemm, Z J anorq u ally (them 1933, 216.80)

and so similar in other ways that chemists have been able to separate them from one another only by such laborious methods as fractional crystallisation of their salts and fractional decomposition of their nitrates. Six of the rare earths however form compounds, in which they exhibit a second valency. Cerum, prascodymum and terbium can all be quadrivalent, samarum, europium and ytterbium divalent (Fig. 16.2).

1

Five of these deviations can be linked up with the theories of atomic structure developed in earlier chapters. The more electrons a shell contains the less willing is it to part with one of them, sodium is more reactive than magnesium, and aluminium than silicon, if then the 4f shell obeys the same laws, it should be easier to remove an electron from cerium in which only one is present than from succeeding elements in which there are several. And in fact the first two elements are quadrivalent, while cerium becomes quadrivalent much more readily than praseodymium, for compounds of the latter readily oxidise cerous compounds to ceric, further, only one quadrivalent compound of praseodymium has been isolated pure, whereas a whole series of ceric compounds are known

The divalency of europium and the quadrivalency of terbium are due to quite another cause Both the p and d shells show that they are more stable when they are just half full than when they contain one electron more or less, nitrogen with three p electrons has a higher ionisation potential than either carbon or oxygen, while the examination of the low terms of the frame elements, carried out in the last chapter, shows that the d5 configuration is more stable than  $d^4$  or  $d^6$ , the difference is not so great as between do and do, but the evidence is too clear to admit of doubt. Now the f shell is half full in the Gd3+ ion, which contains seven electrons, and one might reasonably expect the elements on either side of gadolinium to try to assume this configuration, europium which precedes gadolinium by keeping an extra electron and being divalent instead of trivalent, and terbium which succeeds gadolinium by parting with an extra electron and becoming quadrivalent

The divalency of ytterbium exhibits the tendency to form the closed shell of fourteen f electrons, but the divalency of samarium remains unexplained, for there is no reason to think the f<sup>6</sup> configuration much more stable than the f<sup>5</sup>, in the d shell d<sup>4</sup> is more stable, but not much more stable, than d<sup>3</sup> But we must not make too much of this failure, for SmCl<sub>2</sub> is definitely less stable than EuCl<sub>2</sub>

# 3. Arc and spark spectra

The paramagnetic susceptibilities of the rare earths have already been cited as strong evidence that in the trivalent ions, which occur in crystals and in solution, all electrons outside the xenon core occupy f orbits But to obtain evidence of the structure of the elements themselves, appeal must be had to the arc and spark spectra These exhibit an exceptional number of lines, in the spectrum of dysprosium, for example, over 3000 have been measured This naturally makes the identification of small amounts of the rare earths very difficult, for if one finds the weak yttrium line  $3468\ 0\ A$  , one cannot distinguish it from four other lines, 3467 4 A of Gd, 3467 8 A of Cd, 3468 2 A of Tb or 3468 4 A of Th, unless one can measure the wave-length to a few tenths of an angstrom To surmount this difficulty spectroscopists have been driven to use the 'residual lines', that is, the lines which are the last to fade when the proportion of the element in the mixture is steadily reduced. For example, if the line measured as 3468 0 A. is really an yttrium line, then the strongest yttrium line 3710 3A. must appear much stronger than 3468 0A on the same plate; moreover, as 3710 3A is a residual line, it must be the last to vanish as the material examined is diluted

As long ago as 1922 Bohr\* stated that the atom in which an  ${f f}$ electron first appears is cerium, and that the f shell is full in ytterbium, this statement he based on chemical properties and on a mathematical comparison of the stabilities of alternative orbits Since then many spectra of elements lying just before and just after the rare earths have been analysed, while within the rare earth frame the low terms of CeI, SmI, EuI and GdI are now known †

The fifty-fifth electron occupies the 6s shell in CsI and BaII, and sinks into a 5d orbit in Lam, on Bohr's authority it was commonly expected to sink into a 4f orbit in Cerv, but when the

<sup>\*</sup> Bohr, Theory of Spectra and Atomic Constitution, 1922, 110

<sup>†</sup> Recent analyses of rare earth spectra are Ce I, Karlson, ZP, 1933, 85 482; Ce III, Kaha, Indian Journ Phys., 1933, 8 137, Eu II, Albertson, PR, 1934, 45 499  $\alpha$ , Eu I, Russell and King, PR, 1934, 46 1023, Sm I and Gd I, Albertson, PR, 1935, 47 370

Ce IV spectrum was analysed the ground term was found to be <sup>2</sup>D \* Thereafter it seemed rather improbable that any of the three electrons required to produce neutral cerium would enter a 4f orbit, but apparently Bohr was correct after all, for the ground term of Ce I is <sup>3</sup>H and this arises in the 4f 5d 6s<sup>2</sup> configuration

No of electrons	Atom	Ground term	Configuration	
1	Cs I Ba II La III Ce IV	<sup>2</sup> S <sup>2</sup> S <sup>2</sup> D <sup>2</sup> F	s d f	
2	Ba I La II Ce III	3E 3E 7S	$egin{array}{c} \mathbf{s^2} \\ \mathbf{d^2} \\ \mathbf{d^2} \end{array}$	
3	Laı	$^{2}\mathrm{D}$	d s²	
4	CeI	3H	f d s²	
8 9 10	Sm 1 Eu 11 Eu 1 Gd 1	<sup>7</sup> F <sub>0</sub> <sup>9</sup> S <sub>4</sub> <sup>8</sup> S <sub>3</sub> <del>1</del> <sup>9</sup> D <sub>2</sub>	f <sup>6</sup> s <sup>2</sup> f <sup>7</sup> ( <sup>8</sup> S) s f <sup>7</sup> s <sup>2</sup> f <sup>7</sup> d s <sup>2</sup>	
15	Tur Ybr Lum	2S	f <sup>14</sup> s	
16	Yb 1 Lu 11	¹S	f <sup>14</sup> s <sup>2</sup>	
17	Lu 1 Hf II	<sup>2</sup> D <sup>2</sup> D	$f^{14} d s^2$ $f^{14} d s^2$	

Fig. 16.3 Ground terms of the arc and spark spectra with the configurations in which they arise

At the other end of the rare earth frame the ground terms of Lum and Lum are 2S and 1S respectively, showing that the 4f shell is complete when the nuclear charge is 71, for these terms must arise from the configurations f<sup>14</sup> s and f<sup>14</sup> s², but as the f shell is bound to grow more stable, when the nuclear charge increases, like the d shell of preceding periods, these results do not prove that the f shell is complete in ytterbium. Thus the spectra which have been analysed since 1922 are not inconsistent with Bohr's hypothesis, but they have not yet banished doubt

<sup>\*</sup> Gibbs and White, PR, 1929, 33 157 Lang has since found a lower <sup>2</sup>F term PR, 1936, 49 552a

## Absorption spectra

As there are no specific chemical tests for any of the rare earths except cerum, the chemist relies on optical tests instead Of these at least six are available, the arc and spark spectra, the absorption and phosphorescent spectra of a crystal or solution, and X-ray lines and absorption edges. Any of these can be used to identify an element, but of them all the absorption spectrum is often the simplest, for many of the trivalent ions are brightly

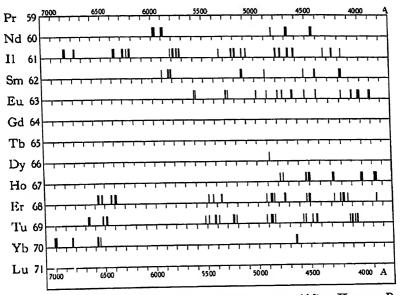


Fig 164 Absorption spectra of the rare earth ions (After Hevesy, Die seltenen Erden, 1926, 39

coloured Praseodymium is green, neodymium red-violet, samarium yellow and element 61 probably yellowish green, dysprosium and holmium are both yellow, erbium is rose and thulium green, of the rest, four, cerium, gadolinium, ytterbium and lutecium, are quite colourless, while europium and terbium show little trace (Fig 164) Thus the elements near the ends of the block, and those round gadolinium, show little or no colour, this can be explained as depending on the depth of the ground term Thus the 8S ground term of the gadolinium ion, calculated by 6

Hund and confirmed by the paramagnetic susceptibility, should be peculiarly stable, since it arises in an f<sup>7</sup> configuration, and in fact the absorption bands of gadolinium lie in the ultra-violet

When the absorption spectrum is more carefully examined, it is found to consist of surprisingly narrow bands, many indeed are only 1 or 2 A wide, whereas the absorption bands of the coloured ions of earlier periods often cover 100 A or more, indeed the rare earth bands are better described as 'lines more or less diffuse' than as bands. Thus if one dilutes the solution of a rare earth salt until all trace of colour disappears, the stronger absorption lines still appear in the spectroscope, though if a solution of potassium permanganate is similarly diluted, the lines disappear with the colour, and this difference is to be attributed to the sharpness of the rare earth bands.

Do these bands arise in the molecule like the bands of a gas in a discharge tube, or are they atomic lines broadened by the varying fields of a crystal? In the band spectra of compounds, and especially of complex ions such as uranyl, homologous groups of lines recur at regular intervals, being due to atoms oscillating within the ion, but in the crystals of the rare earths no group of lines recurs Again, the rare earth absorption lines split in a magnetic field, though the band spectra of uranyl compounds do not \* Moreover, at temperatures as low as 1 7°A. some are still bright, though a molecule could not vibrate at so low a temperature and could not therefore absorb radiation True, the intensities of the lines change as the temperature falls, for while some remain bright, others fade, but the lines which fade are easily explained as arising from levels above the ground state, levels in which the Boltzmann distribution allows very few atoms at low temperatures †

The positions of the bands are largely independent of the anion and are the same in the solid as in solution. This alone is strong evidence that the lines are atomic in origin, and arise in a shell

<sup>\*</sup> Becquerel, le Radnum, 1907, 4 328, K Akad Amsterdam, Proc 1929, 82 749

<sup>†</sup> Becquerel, Lure jubiliare de Kamerlingh Onnes, 1922, 288, Ehrenfest, ibid 362.

Freedand Spedding\* worked first with the chloride, GdCl<sub>3</sub> 6H<sub>2</sub>O, which crystallises in colourless plates. The spectra were taken along the principal axis, that is, perpendicular to the faces, but tests made perpendicular to the principal axis showed that within the limits of measurement the spectrum is independent of the direction in which the light passes. Moreover, in solutions of varying concentration, photographs show that the positions and general spacing of the multiplets are similar to that found in the crystal, except that the lines are rather more blurred and the multiplets are shifted slightly towards higher frequencies

When the absorption spectrum of the chloride is compared with that of other gadolinium salts, the negative ion is seen to produce little change in the positions of the multiplets, though it changes the number of lines and their positions within the multiplet Accordingly, the multiplets must arise from electronic transitions of the Gd³+ ion, but the splitting of these levels must depend on the forces exerted by the surrounding atoms. These forces seem to depend more on the crystal symmetry than on the negative radical, the spectra of monoclinic Gd₂(SO₄)₃ 8H₂O, GdCl₃ 6H₂O† and GdBr₃ 6H₂O‡ are almost identical, but different from hexagonal Gd(C₂H₅SO₄)₃ 9H₂O and Gd(BrO₃)₃ 9H₂O, while work on the triclinic acetate § suggests still a third type, but only one band of the acetate has been examined, so it is perhaps unwise to generalise

As the temperature as reduced little change appears in the spectrum, true the multiplet intervals increase slightly, and the whole spectrum shifts slightly towards the red, but this movement averages only some 4 cm<sup>-1</sup> in a change from the laboratory to liquid hydrogen. These two changes are primarily due to the contraction of the crystal, which brings the ions closer together, and therefore makes the electric field more intense.

<sup>\*</sup> Freed and Spedding, PR, 1929, 34 945 GdCl<sub>3</sub> 6H<sub>2</sub>O, Gd<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> 8H<sub>2</sub>O

<sup>†</sup> Spedding and Nutting, PR, 1931, 38 2294a

 $<sup>\</sup>ddagger$  Spedding and Nutting, Am Chem Soc J 1930, 52 3747 GdBr<sub>8</sub> 6H<sub>2</sub>O

 $<sup>\</sup>$  Spedding and Nutting, Am Chem Soc J 1933,55503  $\rm Gd(C_2H_5SO_4)_3$   $\rm 9H_2O$  and  $\rm Gd(BrO_3)_3$   $\rm 9H_2O$ 

### 6 Samarıum

At room temperature the absorption spectrum of samarium consists of diffuse lines and bands, lying chiefly between 3000 and 5000 A. As the temperature is reduced the lines sharpen, until when the crystal is in liquid hydrogen the lines are very fine, the lines also change in intensity, and this change is much more striking in samarium than in gadolinium, at low temperatures some lines disappear, while new lines make their appearance\*, and this is to be expected, since Hund's theory makes the ground term f<sup>56</sup>H, and at low temperature lines arising in the higher components of this term must be very weak

The Boltzmann distribution law indeed makes it certain that any absorption lines which appear below room temperature must arise in a level lying less than 500 cm  $^{-1}$  above the ground level The visible spectra of crystals of chloride and bromate thus arise between half a dozen levels lying below 500 cm  $^{-1}$  and other levels lying between 17,000 and 27,000 cm  $^{-1}$  In order to follow the changes in intensity more closely, the absorption spectrum of the chloride, SmCl<sub>3</sub> 6H<sub>2</sub>O, was photographed at five temperatures between  $293^{\circ}$  and  $20^{\circ}$  A , first with a single crystal and then with powdered crystals†, the latter method brings out the weak lines, though it blurs the strong, as multiple internal reflection lengthens the path Comparison of these photographs suggests the division of the lines into two groups, one consists of lines which increase in intensity as the temperature is lowered, many only appearing when the temperature has already fallen to  $-195^{\circ}\,\mathrm{C}$  , while in the other group the lines decrease in intensity as the temperature falls, many being absent at 20° A These two groups are conveniently referred to as 'low temperature lines' and 'high temperature lines' Many of the fainter low temperature lines appear on the violet side of a multiplet, while the high temperature lines seem to congregate on the red side

The intensities of both groups of lines depend in part on the populations of the lower levels, and this in turn is governed by

<sup>\*</sup> Freed and Spedding, N, 1929, 123 526

<sup>†</sup> Spedding and Bear, PR, 1932, 42 58, 76 SmCl<sub>3</sub> 6H<sub>2</sub>O, single crystal and powdered crystal

Boltzmann's law, if three low levels exist, separated by intervals of  $150~\rm cm^{-1}$ , and all are of equal weight, the numbers of atoms in these levels at  $20^\circ$  and  $78^\circ$ A are those given in Fig. 16.5 Thus in

Level Temp	0 cm <sup>-1</sup>	150 cm <sup>-1</sup>	300 cm <sup>-1</sup>
20° A 78° A	1	8 3 10 <sup>-6</sup> 2 4 10 <sup>-2</sup>	6 9 10 <sup>-11</sup> 5 7 10 <sup>-4</sup>

Fig 16 5 Normal fraction of atoms existing at any time in three low levels

liquid hydrogen the number of ions lying in levels above the ground level is small, and there seems little doubt that the low temperature lines may be attributed to the ground level, while the high temperature lines arise in a group of levels lying between 100 and  $300\,\mathrm{cm}^{-1}$ 

These predictions are very satisfactorily confirmed by a search for constant intervals between lines of the low and high temperature groups (Fig. 16.6). In the crystals of  $SmCl_3$   $6H_2O$ 

Low tempe	erature line	High tem- perature line	$\Delta  u  ext{ cm}^{-1}$
λΑ	$\nu$ cm $^{-1}$	ν cm <sup>-1</sup>	
5592 6 5582 5 4988 2 4899 6 4513 2 5592 6 5582 5	17875 8 17908 0 20042 5 20404 5 22151 8 17875 8 17908 0	17730 6 17763 1 19897 0 20259 0 22006 0 17716 3 17748 6	145 2 144 9 145 5 145 5 145 8 159 5 159 4 159 8
4988 2 4899 6 4866 0	20042 5 20404 5 20544 8	19882 7 20246 0 20386 0	158 5 158 8

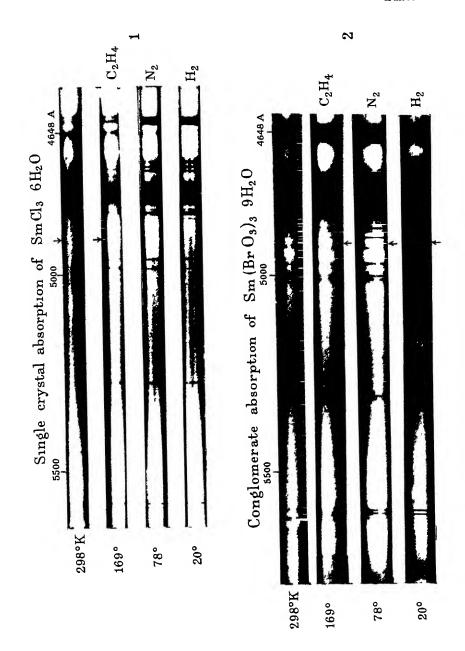
Fig. 16.6 Doublet intervals of 145 and 159 cm  $^{-1}$  found in the absorption spectra of SmCl<sub>3</sub>.6H<sub>2</sub>O at low temperatures.

these differences reveal levels at 145, 160, 204, 217 and 300 cm $^{-1}$  above the ground level. Some of these levels are probably complex, the 300 cm $^{-1}$  level in particular consisting perhaps of components at 295 and 315 cm $^{-1}$ , for the spread varies with the

### PLATE VI

- 1 Single crystal absorption spectrum of SmCl<sub>3</sub> 6H<sub>2</sub>O at four different temperatures. The photographs were taken at the temperatures shown on the left, these being the boiling points of the substances shown on the right All the lines grow sharper as the temperature is reduced, but the intensity may increase or decrease
- 2 Conglomerate absorption spectrum of  $Sm(BrO_3)_8$   $9H_2O$  at four different temperatures A conglomerate or mass of small crystals has a longer optical path than a single crystal, so that it brings out the weak lines, but it blurs the stronger multiplets

(Photographs lent by Prof F H Spedding)





height of the level from 2 to 30 cm<sup>-1</sup>, and these involve errors rather greater than might be reasonably expected

Turning again to the photographs, the lines which originate in the 300 cm $^{-1}$  level are found entirely absent at  $-195^{\circ}\,\mathrm{C}$ , while those arising in the 204 and 217 cm $^{-1}$  levels fade rapidly as the temperature is further reduced

Examined by the same methods hexagonal crystals of the bromate,  $\rm Sm(BrO_3)_3~9H_2O$ , behave very much like the crystals of the chloride until the temperature falls to  $78^{\circ}$  A, the shift in position and widening of the multiplets may perhaps be slightly

Tem- peraturo	Low tempera ture line	Satellite A		Δυ、		Satellite B			$\Delta  u_{ m B}$	
78° A	17847 18857 19987 20382 28125	17809 18817 19949 20342 28087		38 40 38 40 38		17783 18790 19920 20315 28055		64 67 67 67 70		67 67 67
Tem perature	Low tempera- ture line	Аі	Δν <sub>Ατ</sub> Α π		$\Delta  u_{A\pi}$	Ві	ΔνΒι	Вп		$\Delta \nu_{B\pi}$
20° A	17847 4 (II) 17857 2 (II) 17949 (I) 19985 6 (I II) 20385 9 (I) 28125 2 (II)	17912 19949 7 20348 9	- 17802 5 - 18812 37		44 9 45 — 45 — 45	17867 19904 —	82 82 82 —	17780 — 19919 —		67 

Fig 16.7 Low temperature lines and their high temperature satellites in the absorption spectrum of Sm(BrO<sub>3</sub>)<sub>3</sub> 9H<sub>2</sub>O, this shows how the energy levels split as the temperature is reduced from 78° to 20° A

greater, but only slightly, between 78° and 20° A however most of the lines split into two components, of which the red one is almost certainly complex (Fig. 16.7). Thus above 78° A the temperature variation of the lines and a search for constant intervals reveals levels at 39 and 68 cm<sup>-1</sup> above the ground level, with perhaps other levels between 100 and 230 cm<sup>-1</sup>, but at a temperature of 20° A the levels revealed are at 0, 37, 45, 67 and 82 cm<sup>-1</sup> (Fig. 16.8)

Moreover, the transitions observed at 20° A suggest that these levels form two independent sets, 0, 37, 82 combine with one group of high levels, and 0, 45, 67 with another (Fig. 16 8) That

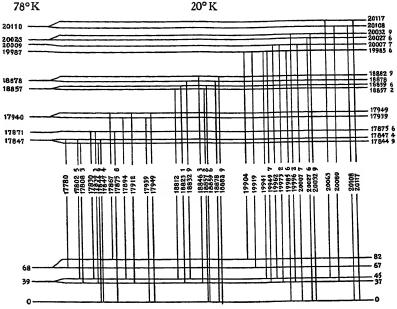


Fig 16 8 Energy levels of  $\rm Sm(BrO_3)_3$  9 $\rm H_2O$  at 20° A , with the lines arising in transitions between them The figures are wave numbers (After Spedding and Bear, PR, 1933, 44 290)

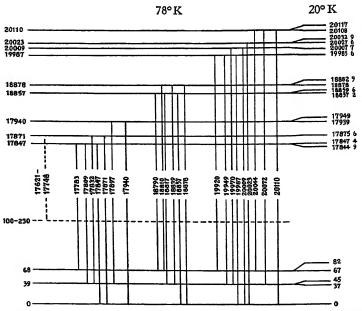


Fig. 16 9 Energy levels of  $Sm(BrO_3)_3$  9H<sub>2</sub>O at 78° A (After Spedding and Bear PR, 1933, 44 290 )

the ground term appears in both groups means nothing, for in fact the method, by which the splitting of the low levels is calculated, automatically reduces any real interval to zero, if all the low levels developed the same interval, one would be free to ascribe this splitting entirely to the high levels \*

The existence of more than three low levels in the samarium salts makes it probable that in  $\mathrm{Sm^{3+}}$  there is a second electronic level lying close to the  ${}^{6}\mathrm{H}_{2\frac{1}{4}}$  term predicted by Hund, for in an electric field this term splits into only three components, and this fits in well with the magnetic susceptibility which does not agree with the value predicted, if  ${}^{6}\mathrm{H}_{2\frac{1}{4}}$  is the only low term †

### BIBLIOGRAPHY

The last three sections of this chapter should be read with chapter XXII Spencer, J F, The metals of the rare earths, 1919, is a very thorough study with full references, but it was written before Bohr had outlined the electronic structure of the elements Hevesy, Die seltenen Erden, 1926, makes full use of Bohr's theory

<sup>\*</sup> Spedding and Bear, PR, 1933, 44 287  $Sm(BrO_3)_3$   $9H_2O$ 

<sup>|</sup> Spedding, Am Chem Soc J 1932, 54 2593

#### CHAPTER XVII

### INTENSITY RELATIONS

### 1 Experimental

For rough estimates of intensity the spectroscopist has often relied on his eye, but the eye is subjective and far from accurate, so that in recent years much attention has been paid to methods of estimating the density of a photographic plate. In general if the intensity of one component of a multiplet is expressed as a percentage of the brightest line, then these methods ensure that the percentage is correct to the nearest integer, but this statement is subject to a few restrictions, of which the most important is that the lines must not be too far apart, for no one knows quite how the sensitivity of a photographic plate varies with wavelength

This is not the place to indulge in a description of experimental procedure, especially as it is fully described elsewhere,\* but the wedge method may be briefly reviewed as illustrating the chief points of interest. As the density of a photographic image is not proportional to the length of exposure or the intensity of the incident light, but shows an initial lag (Fig. 17.1), one is not justified in comparing two densities and then saying that the intensities must have been in the same ratio. Instead, one may only say that if the density at one point is equal to that at another, then the intensities were also equal. The word 'density' is here a technical term, being defined as

$$\log \left\{ \frac{\text{intensity of incident light}}{\text{intensity of transmitted light}} \right\}$$

This means that a scale ought to appear on each plate, and one way of obtaining this is to photograph a wedge of dull grey glass, the density will then be proportional to the distance from the edge of the wedge, and this may be measured by a micrometer fixed to the microscope Thus one may say that the density of a

<sup>\*</sup> Dobson, Griffith and Harrison, Photographic photometry, 1926

certain line is equal to that at a certain place on the wedge, and the latter may be measured on a scale which is a linear scale of intensity

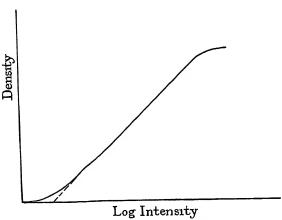


Fig 17 1 Density-intensity graph of a photographic plate

# 2 The normal multiplet

The Sommerfeld intensity rule has already been discussed, but in a form applicable only to multiplets in which  $\Delta L=\pm 1$  Multiplets of the P $\rightarrow$ P $^{\circ}$  type, in which  $\Delta L=0$ , give their strongest lines when  $\Delta J$  is zero, while the two groups arising from  $\Delta J=\pm 1$  are less intense than the chief lines but equal to one another. To include this type of transition the Sommerfeld rule may be restated \*

The chief lines of any multiplet are due to those transitions in which  $\Delta J = \Delta L$ , a weaker group, technically known as satellites of the first order, arise when  $\Delta J = \Delta L \pm 1$ , while satellites of the second order occur when  $\Delta J = \Delta L \pm 2$ 

This rule is qualitative only, attempting to make it quantitative Sommerfeld in 1923 considered first those multiplets which arise by the combination of a single level with a multiplet level, the three SP lines in spectra of all multiplicaties are of this type, and experiment | shows that the intensities due to the three transitions

<sup>\*</sup> Sommerfeld and Heisenberg, ZP, 1922, 11 131

<sup>†</sup> Dorgelo, ZP, 1924, 22 170

vary as (2J+1) for the three P terms, thus the intensities of the triplet lines  ${}^3S_1 \rightarrow {}^3P_{2,1,0}$  of Mg are in the ratio of 5–3–1, while those of the octet lines  ${}^8S_{3\frac{1}{4}} \rightarrow {}^8P_{4\frac{1}{4},3\frac{1}{4},2\frac{1}{4}}$  of Mn are in the ratio of 10–8–6

From this result three important rules emerge. First, the intensity ratio is independent of the serial number n. Secondly, the intensity is determined as much by the level to which an electron is going as the level which it is leaving, in calcium, for example, the intensity ratios of  $2^3S \rightarrow 2^3P$  and  $3^3P \rightarrow 2^3S$  are identical, though one triplet is of the sharp and the other of the principal series. The third is a point of theory, the intensities are in the

Term	$P_0$	P <sub>1</sub>	$P_2$	
$\mathbf{D_1}$	4425 43 25	4435 67 19	4456 61 1	45
$\mathbf{D_2}$	_	4434 95 54	4455 88 18	72
D <sub>3</sub>	_		4454 77 100	100
	25	73	119	Intensity sum

Fig 17 2. Intensities in a diffuse triplet of calcium, the upper number is the wave-length, the lower the intensity measured by Burger and Dorgelo

ratios of the number of Zeeman components possessed by the level, and this fits in well with the practice of taking this number as the statistical weight of a level, a further significance will appear when the intensities of Zeeman multiplets are considered.

The next step was to examine the transitions between two multiplet levels. Working in this direction Burger and Dorgelo\* first verified the validity of the above rules for the PD doublet of sodium where the D levels are not resolved, and then turned to the PD multiplet of calcium, in it they found that the sum of the intensities of the lines originating from one P level was to the sum of the intensities from another P level as the statistical weights of the levels. And the same held true for the three D levels

Fig. 17 2 gives their measurements, the upper figure in each

<sup>\*</sup> Burger and Dorgelo, ZP, 1924, 23 258

square being the wave-length and the lower the intensity adjusted to a scale in which 100 represents the brightest line. The sums of the intensities of the lines originating from the various P levels are given at the bottom, 25–73–119, and it will be observed that they are roughly in the ratio of 1–3–5. Similarly, the intensities, 45, 72, 100, arising from the three D levels are roughly in the ratio 3–5–7.

The summation rule used alone enables us to calculate the intensities resulting from the combination of two doublet levels (Fig. 17.3), but it will not suffice for more complicated multiplets

Term	P4 P14	
D <sub>1</sub> 1/2	5 1 — 9	6 9
	5 10	ΣΙ

Term	$D_{1\frac{1}{4}}\ D_{2\frac{1}{4}}$	
$\begin{matrix}\mathbf{F_{2\frac{1}{2}}}\\\mathbf{F_{3\frac{1}{2}}}\end{matrix}$	14 1 — 20	15 20
	14 21	ΣΙ

Fig. 17.3 Theoretical intensity ratios of diffuse and fundamental doublets

Thus, consider a PD triplet in which the intensities are those shown in Fig. 17.4 Burger and Dorgelo's summation rule shows that  $a_1 + b_2 + c_3 + c_4 + c_5$ 

$$\frac{a_1}{1} = \frac{b_1 + b_2}{3} = \frac{c_1 + c_2 + c_3}{5}$$

$$\frac{a_1 + b_1 + c_1}{3} = \frac{b_2 + c_2}{5} = \frac{c_3}{7}$$

But this gives only four equations to determine five ratios To resolve the problem Russell,\* among others, called in the corre-

	<sup>3</sup> P <sub>0</sub> <sup>3</sup> P <sub>1</sub> <sup>3</sup> P <sub>2</sub>	
<sup>3</sup> D <sub>1</sub> <sup>3</sup> D <sub>2</sub> <sup>3</sup> D <sub>3</sub>	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

Fig. 17 4 Assumed intensities of a diffuse triplet

	<sup>3</sup> P <sub>0</sub> <sup>3</sup> P <sub>1</sub> <sup>3</sup> P <sub>2</sub>	
<sup>3</sup> D <sub>2</sub> <sup>3</sup> D <sub>3</sub>	20 15 1 45 15 84	36 60 84
	20 60 100	

Fig 17 5 Theoretical intensities of a diffuse triplet

spondence principle His argument cannot be given here, but his result may be reviewed

\* Russell, Nat Acad Sci Proc 1925, 11 314, 322, Sommerfeld and Honl, Preuss Akad Wiss Berlin, 1925, 9 141, Honl, AP, 1926, 79 274, Kronig, ZP, 1925, 31 885, 33 261, Dirac, PRS, 1926, 111 281

711

As the intensities of a multiplet are determined by the levels between which the electron jumps and not by the direction of the jump, it is not necessary to consider  $\Delta L = \pm 1$  but only one of these, arbitrarily, then, we elect to consider only  $L \rightarrow (L-1)$  and  $L \rightarrow L$ . For each of these transitions there are three values of  $\Delta J$ , so that six formulae may be expected, and these take their simplest form if J is defined as the larger of the two quantum numbers concerned.

In the transition  $L \rightarrow (L-1)$  the correspondence principle gives

$$\begin{array}{lll} \text{for } J \! \to \! (J \! - \! 1) & I_- \! = \! \frac{S}{4L} \; \frac{1}{J} P \, (J) \; P \, (J \! - \! 1), \\ \\ \text{for } J \! \to \! J & I_0 \! = \! \frac{S}{4L} \; \frac{(2J \! + \! 1)}{J \, (J \! + \! 1)} \; P \, (J) \; Q \, (J), \\ \\ \text{for } (J \! - \! 1) \! \to \! J & I_+ \! = \! \frac{S}{4L} \; \frac{1}{J} \, Q \, (J) \; Q \, (J \! - \! 1). \\ \end{array}$$

In the transition  $L \to L$  the summation rule shows that the two groups of satellites arising from  $\Delta J = \pm 1$  must be identical, so that only two formulae are needed

$$\begin{array}{ll} \text{for } J \to J & I_0 = & \frac{S\left(2L+1\right)}{4L\left(L+1\right)} \; \frac{(2J+1)}{J\left(J+1\right)} \; R^2\left(J\right), \\ \text{for } J \to (J-1) & \\ \text{or } (J-1) \to J & I_{\pm} = & \frac{S\left(2L+1\right)}{4L\left(L+1\right)} \; \frac{1}{J} P\left(J\right) \; Q\left(J-1\right) \\ \end{array}$$

In these equations P(J), Q(J) and R(J) are convenient abbreviations defined as

$$P(J) = (J+L)(J+L+1) - S(S+1),$$
  
 $Q(J) = S(S+1) - (J-L)(J-L+1),$   
 $R(J) = J(J+1) + L(L+1) - S(S+1)$ 

In theory these formulae should compare the intensities of any two lines arising in a transition from one configuration to another, but they are valid only when the coupling is Russell-Saunders and there are no inter-system lines. As very few spectra satisfy this condition the formulae are normally applied only to the intensities of components of a single multiplet, and for this purpose the first factor, which is a function of S and L only, may be dropped

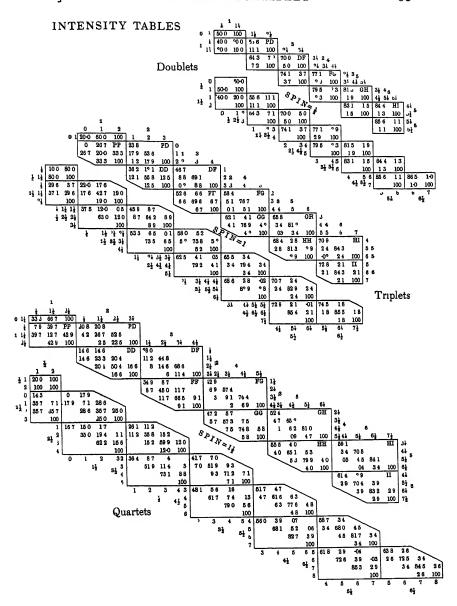
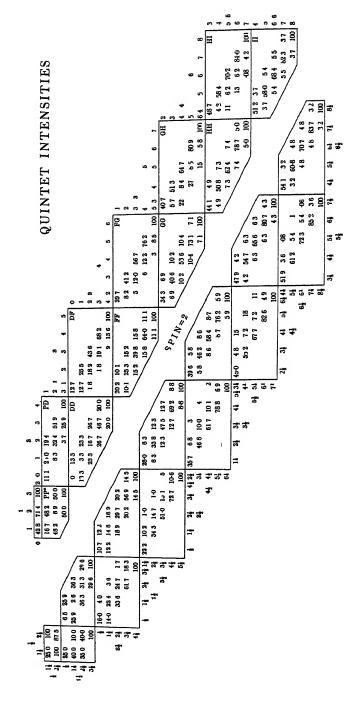
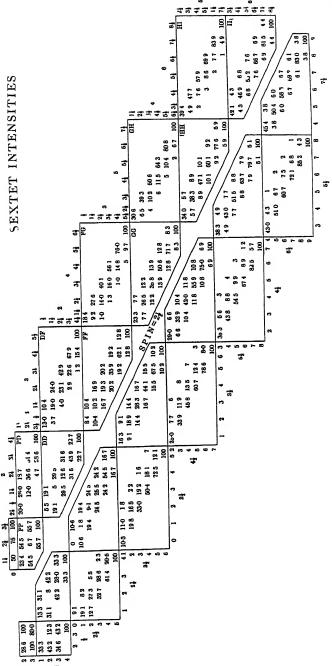
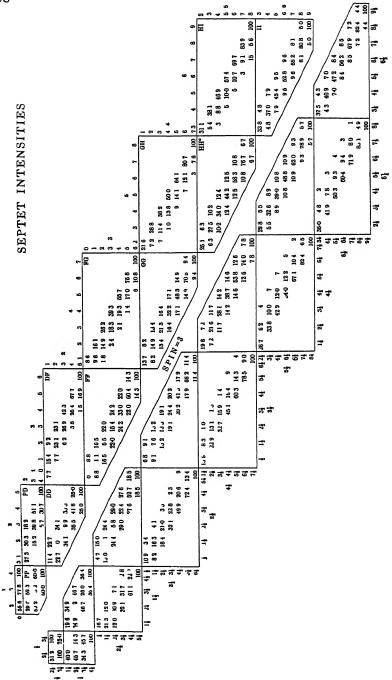


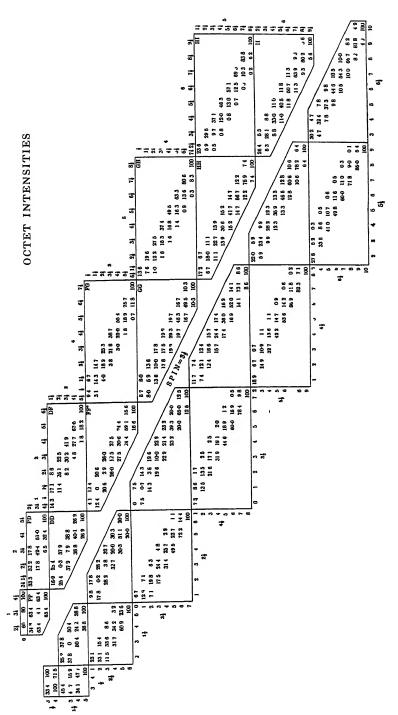
Fig 17.6 Multiplet intensities The intensity of each component is given as a percentage of the strongest line of the multiplet. The numbers outside the frames are L and J, the former in heavy type. The tables may be applied to (11) coupling (p 150), related multiplets (p 104) and hyperfine structure (p 183) (After White and Eliason, PR, 1933, 44 753)







1 81



The equations for the jump  $L \rightarrow (L-1)$  may be illustrated by the three lines  ${}^3D_{1,2,3} \rightarrow {}^3P_2$  In the  ${}^3D$  term L is 2 and S is 1, so that in the jump

from 
$$J=3$$
 to  $J=2$   $I_{-}=\frac{1}{3}(5 \ 6-1 \ 2)(4 \ 5-2)=168,$   
from  $J=2$  to  $J=2$   $I_{0}=30,$   
from  $J=1$  to  $J=2$   $I_{0}=2$ 

This leads to the intensity scheme of Fig 17.5 Incidentally, too, this result satisfies the early qualitative rule of Sommerfeld, which stated simply that

$$I_{-} > I_{0} > I_{+}$$

Fig 17 6 gives a list of the intensities calculated by these formulae, each line being expressed as a percentage of the

Terms	<sup>6</sup> P <sub>1</sub>	<sup>6</sup> P <sub>2</sub>	<sup>6</sup> P <sub>8⅓</sub>
$^6\mathrm{D}_{rac{1}{4}}$	3079 6 (20) 18 3		
<sup>6</sup> D <sub>1</sub>	3073 1 (28) 25 8	3081 3 (12) 13 1	_
6D <sub>2+</sub>	3062 1 (18 7) 18 7	3070 3 (36 6) 34 4	3082 1 (4 8) Lapped
6D <sup>3</sup> <sup>1</sup>		3054 4 (51 4) 51 3	3066 0 (28 6) 26 1
°D41	_	_	3044 6 (100) 100

Fig 17.7 Intensities of the  $w^6P^o \rightarrow 3d^6$  (<sup>5</sup>D) 4s <sup>6</sup>D multiplet of Mn I. The upper figure is the wave-length, the middle the theoretical intensity, and the lower the observed intensity

strongest line, this being a convenient practice because one per cent is about the accuracy which can be attained with the photographic technique developed in recent years. This technique leaves no doubt that these formulae are valid in very many spectra, as examples, Fig. 17.7 shows a PD sextet from Mn I, and Fig. 17.8 a DF quartet from Ti II

The formulae are very seldom applied to the comparison of

different multiplets, but Wijk\* has tried them out on the quartets and doublets of O II, a light atom in which the inter-system lines are very weak. This work roughly confirms the theoretical

3d³ 3d² 4p	4F <sub>1</sub> +	4F <sub>21</sub>	⁴F <sub>3</sub> ‡	4F <sub>41</sub>
4D <sub>↓</sub>	3161 19 (70) 72		_	_
<sup>4</sup> D <sub>1</sub>	3154 18 (28) 28	3161 76 (112) 112	_	
4D <sub>2</sub> 1	(2 0)	3152 24 (37) 35	3162 56 (171) 168	_
4D <sub>3}</sub>	_	(1,4)	3155 65 (29) 30	3168 52 (250) 249

Fig 17.8 Intensities of the 3d24p  $^4D\to 3d^3$   $^4F$  multiplet of Ti II The theoretical intensity is in brackets

quartet-doublet intensity ratio of 2 1, thus the intensities of the  $^4P \rightarrow ^4S$  and  $^2P \rightarrow ^2S$  lines were found to be as 1 6 1, and two other empirical ratios were 2 6 and 2 1

# 3 The super-multiplet

In the mercury spectrum the division into singlets and triplets has little experimental justification, and many inter-system lines are strong, moreover, the sum rule in its simple form is but poorly obeyed. Accordingly, Ornstein and Burger† suggested that when the coupling is no longer Russell-Saunders, the sum rule ought to be extended. For this there is a precedent in the laws of the Zeeman effect, which define certain sums for a single multiplet when the coupling is Russell-Saunders, but only for all terms of a configuration when the coupling is abnormal

In order to make the experimental work as significant as possible, Ornstein and Burger examined first a configuration of

<sup>\*</sup> Wıjk, ZP, 1928, 47 622

<sup>†</sup> Ornstein and Burger, ZP, 1926, 40 403

two electrons, which gives rise to a triplet and a singlet term Moreover, they were careful that one of the two combining triplet terms should be unresolved. A super-multiplet satisfying these requirements is found in some DF combinations of calcium and strontium, if the intensities of the singlet and triplet lines are

Terms	$^{1}D_{2}$	$^3\mathrm{D_1}$	$^3\mathrm{D_2}$	$^3\mathrm{D_3}$
1F	8	_		_
3F		$t_1$	$t_2$	$t_{8}$

Fig 17 9 Assumed intensities in a fundamental super-multiplet

written s and  $t_1$ ,  $t_2$  and  $t_3$  respectively, as in Fig. 17 9, the sum rule applied to the vertical columns states that

$$\frac{s}{5} = \frac{t_1}{3} = \frac{t_2}{5} = \frac{t_3}{7}$$

Thus theory suggests that the intensity of the singlet should be equal to the mean intensity of the three triplet lines, whereas the intensities actually observed\* and quoted in Fig. 17·10

	Ca		Ca	Ca		c
Transition	λ	Int	λ	Int	λ	Int
<sup>1</sup> D <sub>2</sub> - <sup>1</sup> F <sup>3</sup> D <sub>3</sub> - <sup>3</sup> F <sup>3</sup> D <sub>2</sub> - <sup>3</sup> F <sup>3</sup> D <sub>1</sub> - <sup>3</sup> F	4878 4586 4581 4579	43 70 50 25	4355 4099 4095 4093	4 7 6 9 5 0 2 8	5156 4892 4869 4855	44 68 50 34
Mean triplet intensity		48		4 9		51

Fig 17 10 Observed intensities in three fundamental super-multiplets

show that it is rather weaker But the singlet is of considerably longer wave-length than the triplet, and it has been shown\* that when the intervals are large the sum rule should be applied not to the intensity itself, but to the intensity divided by  $\nu^4$ , and, in fact, if the intensity 4 3 of the singlet line is multiplied by  $(4878/4582)^4$  the corrected intensity is 5 5, a figure which is as much larger than the mean intensity of the triplet as the first figure was too small

<sup>\*</sup> Ornstein, Coelingh and Eymers, ZP, 1927, 44 653

With this satisfactory result Ornstein and Burger\* were ready to tackle a group of lines in the mercury spectrum. The lines

Terms	$^{1}\mathrm{D}_{2}$	$^3\mathrm{D}_3$	$^3\mathrm{D_2}$	$^3\mathrm{D_1}$
<sup>1</sup> P <sub>1</sub>	8	_	<i>i</i> <sub>1</sub>	12
<sup>3</sup> P <sub>2</sub>	14	t <sub>1</sub>	$t_3$	$t_{6}$
<sup>3</sup> P <sub>1</sub>	13	_	$t_2$	$t_5$
<sup>3</sup> P <sub>0</sub>			_	t4

Fig 17 11 Assumed intensities in a diffuse super-multiplet.

which should appear are shown in Fig 17 11, and the sum rule applied to this figure leads at once to the equations

$$\frac{s+\iota_1+\iota_2}{3} = \frac{\iota_4+t_1+t_3+t_6}{5} = \frac{\iota_3+t_2+t_5}{3} = \frac{t_4}{1}$$

$$\frac{s+\iota_4+\iota_3}{5} = \frac{t_1}{7} = \frac{\iota_1+t_3+t_2}{5} = \frac{\iota_2+t_6+t_5+t_4}{3}$$

The eleven lines concerned in the relation differ so in wavelength that if all the intensities were measured close agreement with experiment could not be expected unless the  $\nu^4$  correction were applied, and at the time this work was done the  $\nu^4$  correction had not been tested out. But the intervals of the D terms are small, and as these equations require that

$$\frac{t_3 + t_6 + t_4}{t_1} = \frac{4}{21} = 19 \text{ per cent},$$

a check may be applied with measurements on only those four lines which arise from the combination of  ${}^3P_2$  with the D terms

Wave length	Combination	Intensity
3650 3655 3663 3663	t <sub>1</sub> t <sub>3</sub> t <sub>6</sub> t <sub>4</sub>	$ \begin{cases} 100 \\ 10.8 \\ 7.9 \end{cases} 18.7 $

Fig 17 12 Observed intensities in a diffuse super-multiplet of Hg I

The empirical results are shown in Fig. 17 12. The line  $t_6$  is so weak that if measured alone its intensity would certainly be less

\* Ornstein and Burger, ZP, 1926, 40 403

than 1 per cent of  $t_1$ , but it lies so close to  $i_4$  that the two may be conveniently measured together after widening the slit of the spectroscope. The figures show that when the inter-system line is included the sum rule is satisfied, whereas if it is omitted  $(t_3+t_6)$  is only 12 per cent of  $t_1$  instead of the 19 per cent predicted

These experiments clearly show that in certain spectra the sum rule is valid only if the singlet and triplet lines are treated as parts of a single whole, if this is a general phenomenon, then the intensity of successive lines in singlet and triplet series should decrease according to the same law, so that the relative intensity may be independent of the serial number, and in fact Ornstein and Burger\* have confirmed this prediction

### 4. The iron-frame elements

In the analysis of the iron frame elements at the Bureau of Standards, Russell and his co-workers have relied more on intensities than on multiplet intervals or magnetic splitting factors Indeed, if the general intensity laws were not obeyed these spectra would probably still await analysis. The strongest lines arise from transitions in which only a single electron orbit changes, and this is in agreement with the correspondence principle, which indicates that those terms between which strong combinations appear must be built up from the same state of the ion In contrast, transitions involving a change in the ion are much less probable, and the lines resulting are either absent or fainter even than the weak inter-system lines Moreover, when only one electron jumps, the intensities of related multiplets can be obtained from the formulae designed to give the intensities of related lines, Russell† suggested a law of this kind, while Kronig used theory to show that if the coupling is Russell-Saunders the figures are identical and Fig 176 can be used For this purpose S is replaced by  $_{i}L$ , L by l and J by L, where  $_{i}L$  is the orbital moment of the ionic term, l the orbital moment of the jumping electron and L their resultant

In the iron frame elements, though the relative intensities of

<sup>\*</sup> Ornstein and Burger, ZP, 1926, 40 403 7 Russell and Meggers, Bur of Standards, Sci P 1927, 22 332

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the multiplets are admirably regular, the relative intensities within the multiplets are often abnormal Russell's\* visual estimates showed that in Nii components of small J give fainter lines than they should, and later measurements amply confirm him. Not only are individual intensities irregular, but also the sums taken over all the terms of a multiplet with the same J

δG

			<del></del>				
Statistical weight	5	7	9	11	13	Sum	Quotient
	(30)				Theory	(29 7)	(9 9)
3	9 5	-	_	_	Expt	9 5	3 2
	(8)	(41)				(49 5)	(9 9)
5	11	16		_	_	27	5 4
	(0 5)	(12)	(57)			(69 2)	(9 9)
7	~1	24 5	25	_		50 5	7 2
		(0 6)	(12)	(76)		(89 0)	(9 9)
9	-	~1	29	44	_	74	8 2
	Theory		(0 3)	(8)	(100)	(108)	(9 9)
11	Expt	_	~1	41	100	142	12 9
	(38 5)	(53 8)	(69 2)	(84 6)	(100)		_
Sum	21 5	41 5	55	85	100		
	(77)	(77)	(77)	(77)	(7 7)	_	_
Quotient	43	59	61	77	7 7		

Fig 17 13 Comparison of theoretical and experimental intensities in a F $\to$ G quintet of Ni I, this quintet arises as d8s (4F) 5s  $^5F\to d^8s$  (4F) 4p  $^5G^\circ$ 

Fig 17 13 shows this, for when the sum rule is valid, the intensity sum divided by the statistical weight yields a constant, but in Nii and Coi the quotient values from one J to another

In a general way spectroscopists have long realised that the Russell-Saunders coupling, which predominates on the left-hand side of the periodic table, gives way to less regular coupling as one passes to the right, so that no one was surprised when titanium

\* Russell, PR, 1929, 34 825

was shown to obey the intensity laws more closely than nickel Nickel and cobalt indeed form the ultimate members of a series, which grows progressively less regular. In Ti ii 62 per cent of the lines obeyed the formulae to within 5 per cent, but in Ti ii, where Harrison\* measured twenty-six strong multiplets, the proportion was down to 58 per cent, in chromium† and manganese‡ still more violations were observed, while in cobalt and nickel hardly a single multiplet is regular §

Various efforts have been made to trace the cause of the irregularity In Zri many intensities are abnormal because two terms of the same configuration and the same J have also nearly the same energy, these terms share their intensities, just as they share their magnetic splitting factors In particular, the transition 4d<sup>2</sup> 5s 5p<sup>1</sup>F<sub>3</sub>° $\rightarrow$ 4d<sup>3</sup> 5s <sup>5</sup>F is observed because d<sup>2</sup> sp <sup>1</sup>F<sub>3</sub>° lies near d² sp  $^5\mathrm{D_3}^{\circ}$  , their energies being 24,387 and 23,889 cm  $^{-1}$  respectively  $\parallel$  And as the multiplet separations become greater as one passes from left to right across the table, the multiplets overlap and perturbone another more  $\P$  But adequate as this explanation may be in its place, it is necessarily unable to show why lines involving small values of J are weak compared with those in which J is larger—unless indeed many lines of lower multiplicity and therefore in general smaller J remain unidentified  $\,$  Moreover, this explanation would suggest strong correlation with departures from the interval and Zeeman rules, but in fact Frenchs,\*\* having examined selected multiplets from some elements of the iron frame, found that the correlation with the interval rule is poor, while Harrison in his detailed study of titanium found no correlation with either rule. Often those multiplets which split irregularly in the magnetic field and have irregular intervals obey the intensity laws well, while those which have regular values of g obey the intensity laws badly And an attempt to

<sup>\*</sup> Harrison, JOSA, 1928, 17 389

<sup>†</sup> Allen and Hesthal, PR, 1935, 47 926

<sup>&</sup>lt;sup>‡</sup> Seward, PR, 1931, 37 344

<sup>§</sup> Ornstein and Buoma, PR, 1930 36 679

<sup>|</sup> Kiess, C. C and Kiess, H K, BSJ, 1931, 6 621

<sup>¶</sup> Harrison and Johnson, PR, 1931, 38 773

<sup>\*\*</sup> Frenchs, AP, 1926, 81 842

attribute the abnormal weakness of certain lines to the abstraction of energy by inter-system lines was no more successful

### Alkalı doublets

In general the intensity ratio in a series of multiplets is independent of the senal number, but this is not true of the principal doublets of the alkalis nor of the similar doublets of Tli

The controversy\* about the alkalı doublets has lingered on for many years because of the great experimental difficulties, the most serious being self-absorption, which can be avoided only by working at low temperatures and low current densities, but the general features are now clear (Fig. 17.14). The diffuse and funda-

	Doublet		Doublet Intensity ratio			Intensity ratio
Ele ment	Transition	Wave length, A	Calcu- lated Fermi	Experimental		
Na K	2 <sup>2</sup> P→1 <sup>2</sup> S 2 <sup>2</sup> P→1 <sup>2</sup> S 3 <sup>2</sup> P→1 <sup>2</sup> S	5890-96 7665-99 4044-47	$ \begin{array}{c c}  & 20 \\  & 20 \\  & 216 \end{array} $	Ro <sup>1</sup> 1 98 Ra 1 91 Ra 2 10		
Rb	2 <sup>2</sup> P→1 <sup>2</sup> S 3 <sup>2</sup> P→1 <sup>2</sup> S	7800-947 4202-16	2 60	Ra 185 H 255, K H 271, Ro 2258		
Cs	1 <sup>2</sup> P -> 1 <sup>2</sup> S 3 <sup>2</sup> P -> 1 <sup>2</sup> S 1 <sup>2</sup> P -> 1 <sup>2</sup> S	3587-92 4555-93 3877-89	2 97 4 3 7 15	H 3 25, K H 3 32, Ro 2 2 90 FW 3 3, Ra 3 85 K H 8 50, Ro 2 7 40, FW 4 6, H 8 0		

Fig. 17 14 Intensity ratios of some principal doublets of the alkalis

### Observers

Fuchtbauer and Wolfi, AP 1929, 3 359 Extrapolated to allow for self F W

Hubnet, AP, 1933, 17 781 Photographic companison of lines emitted by burner at 2800° H

KH

Ra Ro 1

Kon ned Hubner, PZ, 1933, 34 278 Emission spectrum Rascetti, N Orm 1924, 1 115 Anomalous dispersion Roschdostwenski, IP, 1912, 39 307 Anomalous dispersion Roschdostwenski, T Opt I, Pehograd, 1921, 13 1 Anomalous dispersion

mental doublets give the normal ratios of 9 5 1 and 3 2 in caesium,† and presumably in all other spectra, in the principal series, on the other hand, the normal ratio of 2 1 is found only in sodium and potassium |, the deviation increases rapidly with atomic number

<sup>\*</sup> Joos, Hb d Eapt Phys 1929, 22 313

Filippov, ZP, 1927, 42 495

Fuchtbauer and Wolff, AP, 1929, 3 359

and is quite unmistakable in caesium. In the latter Rasetti\* a Roschdostwenski,† both of whom used the accurate method anomalous dispersion, found ratios of 3 85 and 7 40 in the seco and third principal doublets respectively, while Sambursk states that after rising to a maximum value of 25 1 in the fit doublet, the intensity ratio decreases to 5 1 in the eighth. the first doublet the ratio deviates very little from the norm value of 2 even in caesium.

This much was known when Fermi§ applied the quantimechanics to the problem, and showed that if certain term ordinarily neglected, are taken into account, deviations vesimilar to those observed should arise. Thus theory shows that t deviation will increase rapidly with atomic number, but shound affect the first doublet of the principal series, while the int duction of numerical values leads to intensity ratios of 4.3 a 7.15 for the second and third doublets of caesium, for the findoublets theory gives a ratio somewhat less than 2, but the difference is too small to measure. The agreement here obtain with experiment is probably as close as can be expected.

In Tl1, which like the alkalis has a single electron outside clos shells, similar deviations occur. In the  $m^2P_{1\frac{1}{2},\frac{1}{4}} \rightarrow 2^2S_{\frac{1}{2}}$  seriexperiment shows that the intensity ratios when m=4, 5, 6 are 44, 66, 60 and 52 ||

# 6 The Zeeman multiplet

As with the normal so with the Zeeman multiplet, certa simple rules have been established, but these suffice to determine the intensity ratios only in the simpler transition, in the most complex, reliance must be placed on formulae deduced with and of the quantum mechanics

Three rules are usually cited,¶ but of these the first states or the well-known fact that the Zeeman multiplet is symmetriabout the undisplaced line. The second adds that the intens

- \* Rasetti, N. Cim 1924, 1 115
- † Roschdostwenski, T Opt I, Petrograd, 1921, 13 1
- ‡ Sambursky, ZP, 1928, 49 731 § Fermi, ZP, 1930, 59 680.
- Williams and Herlihy, PR, 1932, 39 802
- ¶ Ornstein and Burger, ZP, 1924, 28 135

sum of all lines originating in one Zeeman level is equal to the intensity sum of all lines originating in any other Zeeman level, and this holds true if the word 'ending' is substituted for 'originating' This law appears at first analogous to the Burger and Dorgelo sum rule, the statistical weight of each Zeeman level being unity, but further examination shows that the relation is closer than analogy, for a term splits to (2J+1) Zeeman components, so that the normal multiplet rule is a necessary consequence of the Zeeman rule

<u>A</u>	ſ	Total intensities				
3S1	<sup>3</sup> P <sub>2</sub>	σ	π			
1 0 1 0 -1 0 -1 -1	2 1 1 0 0 0 -1 -1 -2	$egin{array}{c} a_3 \\ a_2 \\ a_1 \\ \hline a_1 \\ a_2 \\ \hline a_3 \\ \end{array}$	$ \begin{array}{c} \overline{b_1} \\ \overline{b_0} \\ \overline{b_1} \\ \overline{b_1} \\ \overline{b_1} \end{array} $			

Fig. 17 15 Assumed intensities of the Zeeman components of a  ${}^3S_1 \rightarrow {}^3P_2$  line

The third rule concerns the polarisation, and states that if the various components emitted in any direction are combined the resulting beam must be unpolarised. Thus in the normal Zeeman triplet observed transverse to the magnetic field, the sum of the intensities of the two  $\sigma$  components must be equal to the intensity of the  $\pi$  component These rules appear simple enough, but the simplicity is in part only apparent, for the intensities mentioned in the sum and polarisation rules are not the same, the sum rule applies to the total radiated intensity, while the polarisation rule applies to the intensity observed in a particular direction. Thus when a pattern is observed transverse to the field, those oscillations which produce  $\sigma$  components vibrate in a circle whose plane is perpendicular to the magnetic axis, one component of this vibration is along the line of sight and so invisible, thus only half the radiated intensity of a  $\sigma$  component is observed. On the other hand the oscillators which are producing  $\pi$  components vibrate along the magnetic axis, so that the whole of the radiated intensity reaches an eye looking transverse to the field

As an example of the way in which these three rules are applied consider the  ${}^3\mathrm{S}_1 \rightarrow {}^3\mathrm{P}_2$  transition \* Fig. 17-15 gives on the left the possible values of the magnetic quantum number M, and on the right the total intensity radiated in each transition, the  $\pi$  and  $\sigma$  components being separated for convenience. The consequences of the symmetry rule are embodied in the notation, the sum rule, applied to the components of the  ${}^3\mathrm{P}_2$  term, states that

$$b_0 + 2a_1 = b_1 + a_2 + a_3$$

while applied to the 3S1 term it shows that

$$b_0 + 2a_2 = b_1 + a_1 + a_3$$

In order to apply the polarisation rule, elect to observe the pattern transverse to the magnetic field, then the argument

Ele	Line	Intensity		σ			π			σ		Σπ	Σσ
ment		Theoretical	5	15	30	30	40	30	30	15	5	100	100
Mg Ca Zn Cd	5183 6162 4810 5085	Observed Observed Observed Observed	5 4 5 5	16 13 15 15	30 29 29 29	32 30 32 32	39 41 41 41	32 28 31 31	30 28 29 27	14 14 15 14	3 6 3 5 5	103 99 104 104	98 94 97 95

Fig 17 16 Observed intensities of the Zeeman components of a  $^3\mathrm{S}_1 \!\to\! ^3\mathrm{P}_2$  line in various spectra

given above shows that the total radiated intensity of the  $\pi$  components must be equal to half the total radiated intensity of the  $\sigma$  components, that is,

$$\begin{array}{l} b_0 + 2b_1 = \frac{1}{2} \left\{ 2a_1 + 2a_2 + 2a_3 \right\} \\ = a_1 + a_2 + a_3 \end{array}$$

The three simple rules thus determine the four unknown ratios, being satisfied by the values

$$a_1 = 1$$
,  $a_2 = 3$ ,  $a_3 = 6$ ,  $b_0 = 4$ ,  $b_1 = 3$ 

These predictions for the  ${}^3S_1 \rightarrow {}^3P_2$  line have been amply confirmed by Van Geel,† as Fig 1716 shows, moreover, similar

- \* Ornstein and Burger, ZP, 1924, 29 241
- † Van Geel, Diss Utrecht, 1928, 60



predictions for the two other lines of the triplet are equally satisfactory (Fig. 17 17)

Line	Transition	Intensity	σ		π		σ		$\Sigma_{\pi}$	Σσ
6122	<sup>3</sup> S <sub>1</sub> → <sup>3</sup> P <sub>1</sub>	Theoretical Observed	15 15 17 16		30 30	30 28	15 15	15 15	60 58	60 63
6102	$^3S_1 \rightarrow ^3P_0$	Theoretical Observed	10			80	10 10		20 20	20 19

Fig 17 17 Intensities of the Zeeman components of two calcium lines

Though these three rules suffice when the J values of the two terms concerned are small, in more complex transitions resort must be had to the correspondence principle\* or to the quantum mechanics  $\dagger$  Calculations based on these principles show that for the transitions  $J \rightarrow (J-1)$ , the intensities are given by

$$\begin{array}{lll} \sigma & \operatorname{Jump} & M \to (M-1) & & I_- = \frac{1}{2} p \left( M \right) p \left( M - 1 \right), \\ \pi & \operatorname{Jump} & M \to M & & I_0 = p \left( M \right) q \left( M \right), \\ \sigma & \operatorname{Jump} & \left( M - 1 \right) \to M & & I_+ = \frac{1}{2} q \left( M \right) q \left( M - 1 \right), \end{array}$$

while for the transitions  $J \rightarrow J$ 

$$\begin{array}{lll} \pi & \operatorname{Jump} & M \to M & I_0 = r^2(M), \\ \sigma & \operatorname{Jump} & M \to (M-1) & I \pm = p\left(M\right) q\left(M-1\right) \\ & \operatorname{or} & (M-1) \to M & \end{array}$$

In these equations the transitions considered make J and M the larger of the two quantum numbers concerned, while p,q and r are abbreviations, defined by

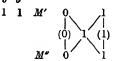
$$\begin{split} p\left(M\right) &= J + M, \\ q\left(M\right) &= J - M, \\ r\left(M\right) &= M \end{split}$$

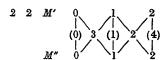
The intensities given by these formulae are the total radiated intensities. The formulae for the transition from (J-1) to J are not quoted, because the intensities are independent of the direction in which the electrons jump, so that one may consider always  $J \rightarrow (J-1)$ 

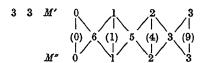
Intensities calculated from these formulae are given in Fig 17 18, as the formulae do not contain L or S the Zeeman intensities

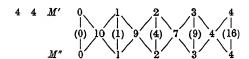
<sup>\*</sup> Honl, ZP, 1925, 31 340, AP, 1926, 79 288, Kromg, ZP, 1925, 31 885

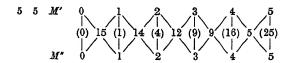
<sup>†</sup> Heisenberg and Jordan, ZP, 1926, 37 263

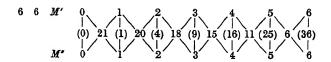












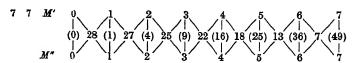
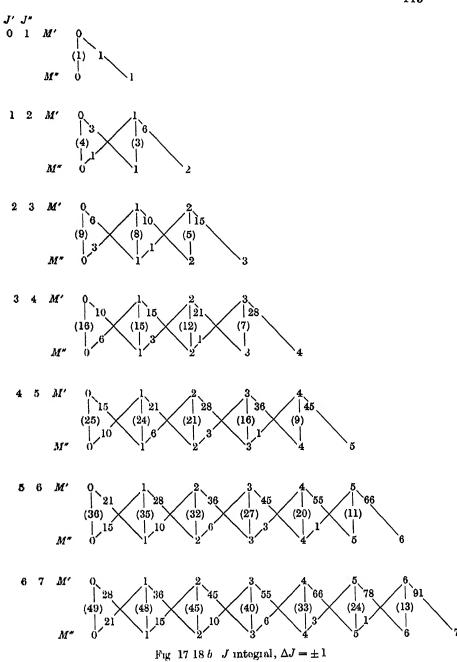
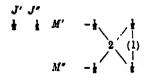


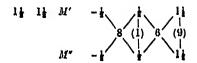
Fig. 17 18  $\alpha$  Integral,  $\Delta J = 0$ 

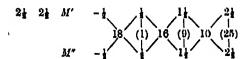
Table of Zeeman intensities. The table is divided into four sections according as J is integral or half integral, and according as  $\Delta J$  is 0 or  $\pm 1$ 

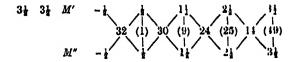


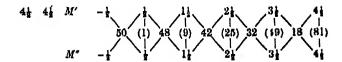
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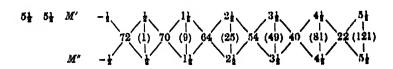












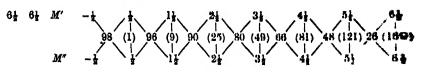


Fig 17.18 c. J half-integral;  $\Delta J = 0$ 

Fig 17 18 d J half-integral,  $\Delta J = \pm 1$ 

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sities are a function of J only, so that the components of the lines  ${}^3P_2 \rightarrow {}^3S_1$  and  ${}^7F_2 \rightarrow {}^7D_1$  have the same intensity ratios, though they do not occupy the same positions. Like the simpler rules these formulae have been confirmed by the experiments of Van Geel, who has measured lines in the octet system of MnI, and in the septet and quintet systems of CrI (Figs. 17 19–17 21), but

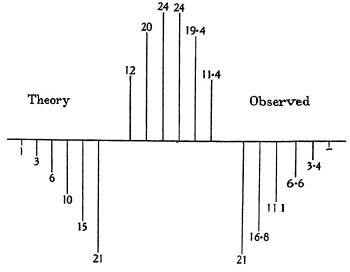


Fig 17 19 Intensities of the Zeeman components of the 4754 A line of Mn I, this line arises as  $a^8S_{3\frac{1}{2}} \rightarrow z^8P^o_{2\frac{1}{2}}$  The pattern is (1) (3) (5) 9 11 13 15 17 19/7. On the left are the theoretical, and on the right the measured intensities, the brightest  $\pi$  and  $\sigma$  components being adjusted to fit After Van Geel, Diss. Utrecht, 1928, 65

work on the iron row shows that the agreement is not always as good as that shown in the lines chosen here as illustrations

Having obtained satisfactory intensity formulae for normal multiplet lines, two extensions suggest themselves; first, one may enquire whether the formulae are applicable to inter-system lines, and second, what intensities are to be expected in the partial Paschen-Back effect. To these questions also Van Geel has offered some answer \*

As an inter-system line he chose  ${}^{1}D_{2} \rightarrow {}^{3}P_{2}$ , 3663 3 A , of Hg I,

<sup>\*</sup> Van Geel, Diss Utrecht, 1928 and ZP, 1928, 47 615

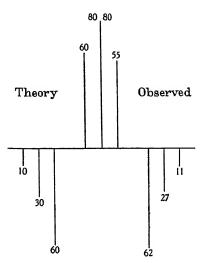


Fig 17 20 Intensities of the Zeeman components of the 5205 A line of Cr I, this line arises as z  $^5\mathrm{P}^\circ_1 \rightarrow \alpha^5\mathrm{S}_2$ , the pattern is (0) (1) 3 4 5/2 After Van Geel, Diss Utrecht, 1928, 68

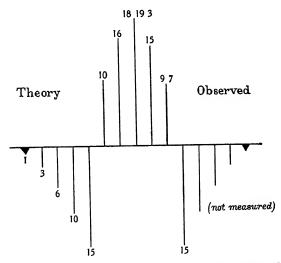


Fig 17 21 Intensities of the Zeeman components of the 5208 A line of Cr I, this line arises as  $z^5 P^\circ_{3} \rightarrow a^5 S_2$ , the pattern is (0) (1) (2) 3 4 5 6 7/3 After Van Geel, Diss Utrecht, 1928, 67

and obtained the intensity pattern shown in Fig. 17 22 This is certainly rather irregular, but then so is the pattern of the neighbouring triplet line,  ${}^{3}D_{1} \rightarrow {}^{3}P_{2}$ , 3662.9 A (Fig. 17.23), and

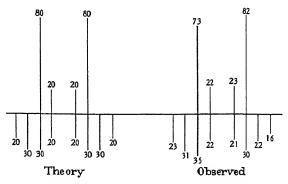


Fig. 17 22 Intensities of the Zeeman components of the 3663 3 A line of Hg I; this line arises as  $3 \, ^{1}D_{2} \rightarrow 2 \, ^{3}P_{2}$ , and the pattern is (1)(2)1234/2 After Van Geel, Diss Utrecht, 1928, 77

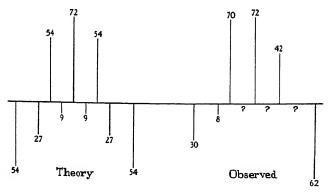


Fig. 17.23. Intensities of the Zeeman components of the 3662.9 A line of HgI, this line arises as  $3\,^3D_1 \rightarrow 2\,^3P_2$ , the pattern is  $(\theta)(2) \, 1 \, 3 \, 5/2$  After Van Geel, Diss. Utrecht, 1928, 77

as this sd configuration produces two diads instead of a singlet and a triplet, the coupling must be abnormal

For the intensities of the partial Paschen-Back effect appeal must be had to the quantum mechanics, which has been applied by Darwin\* and others to predict both the intensity and displace-

\* Darwin, C G, PRS, 1927, 115 1



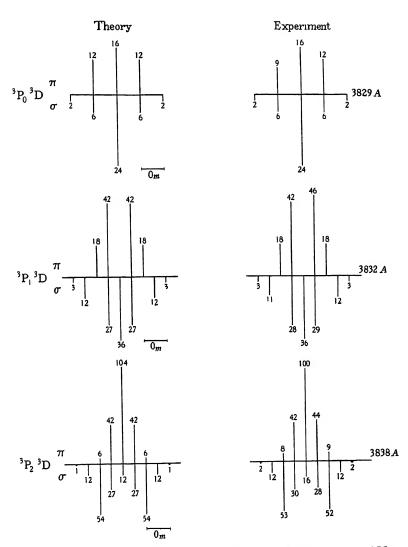


Fig 17 24 Intensities of the Zeeman components of a diffuse triplet of Mg I, the lines arise as  $3\,^3\mathrm{D}\to2\,^3\mathrm{P}_{0,\,1\,\,2}$  This is an example of the partial Paschen Back effect After Van Geel, Diss Utrecht, 1928, 84

ment of the magnetic components of any normal multiplet in any field. That this theory is valid few doubt, for it is of very general application and is known to give correct results in weak and strong fields. Further confirmation in intermediate fields is however still welcome, so that Van Geel's measurements on a Mgi triplet, which exhibits the partial Paschen-Back effect, are worth quoting (Fig. 17-24). They confirm the theory admirably \*

### 7. Raies ultimes

A common method of analysing an unknown salt is to add a little to a carbon arc,† if the powder happens to be a pure calcium salt, a great many calcium lines will appear, but as the proportion

	Arc spec	tra		Spark spectra				
Element	Wave- length	Terms	Element	Wave- length	Terms			
K Ca Sc	7665 4227 4779	$\begin{array}{c} {}^{2}P_{1} \rightarrow {}^{2}S_{1} \\ {}^{1}P_{1} \rightarrow {}^{1}S_{0} \\ {}^{2}F_{3} \rightarrow {}^{2}D_{2} \end{array}$	Ca Sc Tı	3934 3614 3349	$^{2P_{1\downarrow} \rightarrow ^{2}S_{\frac{1}{4}}}$ $^{3F_{4}} \rightarrow ^{3}D_{3}$ $^{4G_{5\downarrow} \rightarrow ^{4}F_{4\downarrow}}$			
Tr V Cr	3635 3185 4254	$^{3}G_{5} \rightarrow ^{3}F_{4}$ $^{4}G_{5\frac{1}{4}} \rightarrow ^{4}F_{4\frac{1}{4}}$ $^{7}P_{4} \rightarrow ^{7}S_{3}$	V Cr Mn	3093 2836 2576	$^{5}G_{6} \rightarrow ^{5}F_{5}$ $^{6}F_{5_{1}} \rightarrow ^{6}D_{4_{1}}$ $^{7}P_{4} \rightarrow ^{7}S_{3}$			
Mn Fe Co Nı	4031 3720 3452 3415	$^{6}P_{3\frac{1}{4}} \rightarrow ^{6}S_{2\frac{1}{4}}$ $^{5}F_{5} \rightarrow ^{5}D_{4}$ $^{4}G_{5\frac{1}{4}} \rightarrow ^{4}F_{4\frac{1}{4}}$	Fe Co Nı Cu	2382 2389 2416	${}^{6}F_{5\frac{1}{4}} \rightarrow {}^{6}D_{4\frac{1}{4}}$ ${}^{5}G_{6} \rightarrow {}^{5}F_{5}$ ${}^{4}G_{5\frac{1}{4}} \rightarrow {}^{4}F_{4\frac{1}{4}}$			

Fig 17 25 Some raies ultimes.

of calcium in the powder is diminished step by step, the weaker lines successively disappear until finally only one is left, this is known as the *raie ultime*, and is in fact the 4227 A line, arising as  ${}^{1}P_{1} \rightarrow {}^{1}S_{0}$ . This method of analysis was developed by de Gramont.‡

The raies ultimes are not necessarily the strongest lines in the spectrum as ordinarily produced, nor are they in general the lines

<sup>\*</sup> See also Back's measurements on a diffuse doublet of copper, Vol. 1, 117

<sup>†</sup> Twyman and Smith, Wavelength tables of spectrum analysis, 1931. Ryde and Jenkins, Sensitive arc lines of 50 elements, 1930 Both book and pamphlet are published by Adam Hilger

<sup>‡</sup> De Gramont, Comptes Rendus, 1920, 171 1106.

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which require the least energy to excite them, the resonance lines. Instead they are determined by four conditions, of which two are energy conditions \* The first states that the lower term is always the ground term, and the second that the higher term is of the same system. As inter-system lines are in general weaker than lines arising within a system, this condition is surprising only as excluding lines, such as the 2536 A  $^3P_1 \rightarrow ^1S_0$  line of Hg I, which are exceptionally strong for other reasons. Subject to these two conditions, and in part also to the fourth, the energy required to excite the line must be as small as possible. The fourth condition states that when the energies are nearly equal, the rare ultime will usually arise from a transition in which  $\Delta L$  is -1 in preference to one in which it is +1, but in aluminium and its homologues the  $^2D$  term lies so much higher than the  $^2S$  that the rare ultime is  $^2S_4 \rightarrow ^2P_4$ , the fourth condition notwithstanding

#### BIBLIOGRAPHY

Frerichs in the Handbuch der Physik, 1929, 21, deals with theory and its empirical justification Van Geel, Intensiteitsverhoudingen van Magnetisch Gesplitste Spectraallynen, 1928, contains a thorough study of Zeeman intensities, this is a dissertation presented to the University of Utrecht

For experimental methods

Dobson, Griffith and Harrison, Photographic photometry, 1926, Ornstein, Moll and Burger, Objektive Spektralphotometrie, 1932

\* Laporte and Meggers, JOSA, 1925, 11 459 Meggers and Scribner, how ever, have proposed a new rule 'A rare ultime originates in a simple interchange of a single electron between an s and a p state, usually preferring configurations in which only one electron occurs in these states' The rare ultime of Hf II is  $5d^2$  6p  $^4G_{5\dagger}$  5d $^2$  6s  $^4F_{4\dagger}$ , though  $^4F$  is not the ground term BSJ, 1934, 13 657, 1935, 14 629

### CHAPTER XVIII

# THE SUM RULES AND (11) COUPLING

## 1 Deviations from the Russell-Saunders coupling

The low terms of the light elements are easily divided into multiplets, and the multiplets into configurations In general the components of a multiplet differ in energy by an amount which is small compared with the height which separates one multiplet from another, and similarly the interval separating two terms of a configuration is usually small compared with the height which separates one configuration from another Each level is characterised by a certain value of J, and each multiplet by values of L and S J and L are determined primarily by selection rules and S by the number of components in a multiplet, but in the allotment of quantum numbers the interval ratios, magnetic splitting factors and intensities all have to be considered Moreover, J is the vector sum of L and S All these regularities are regarded as arising in the Russell-Saunders coupling of the electrons, and conversely any irregularity is attributed to some distortion of the coupling

Deviations from these rules occur frequently in elements of high atomic weight, and in the high terms of a spectrum, they are rather more common on the right-hand side of the periodic table than on the left. But the various rules are not equally sensitive, the interval ratios are often abnormal when the g factors and intensities are normal, while the g factors are rather more easily disturbed than the intensities. This must not be taken to mean that terms in which the interval ratio is normal and the intensities abnormal do not sometimes occur, but in the analysis of an irregular spectrum like Nii intensities usually give the surest clue to the names of the terms. There are spectra, however, such as argon, in which none of these clues are worth much, for the terms are no longer divided into multiplets but only into configurations, values of L and S cannot then be assigned. Finally, there exist

which different configurations lie at the same conturb one another

r abnormal a spectrum, the J values of each conain unchanged, and there is strong evidence that if ints, g factors and intensities are summed for terms ne values of J, then the result is the same in all uestion remains over how many terms the sum is id in this the energy seems to be crucial, in simple ich each multiplet is well separated from other rule is valid for each multiplet separately, when are intermingled, but the configurations distinct, must be taken over all terms of the configuration, a in which the sum rules are usually met But when tions overlap, then the sum must extend over both

### e of the g sum

rgies of all terms, which have the same M and one a single multiplet, is proportional to the field, nents of energy are measured in terms of the normal then their sum is independent of the field, and

$$\mathop{\Sigma Mg}_{J} = \mathop{\Sigma}_{L~S} \left( M_L + 2 M_S \right)$$

nakes possible the calculation of the weak field or without the aid of the quantum mechanics, it does, however, only to a single multiplet, it is the coupling is Russell-Saunders

nay be generalised, however, for an electron consumming over all terms of a configuration. For if lependent of the field intensity, it should not change strong that each electron vector precesses indeposit the magnetic axis, the coupling is then

$$\left\{ \left(\mathbf{l}_{1}\mathbf{H}\right)\left(\mathbf{l}_{2}\mathbf{H}\right)-\left(\mathbf{s}_{1}\mathbf{H}\right)\left(\mathbf{s}_{2}\mathbf{H}\right)-\right\}$$

rule reads

$$\Sigma Mg = \Sigma \left( m_l + 2m_s \right)$$

se  $\sum (m_l + m_s)$  As an example, consider a pd conving rise to the six terms <sup>3</sup>PDF, <sup>1</sup>PDF (Fig. 181)

Among these there are four with components in which M is 3, and in these  $\Sigma (m_l + 2m_s)$  is 14. In a weak field these components appear as parts of the  ${}^3F_4$ ,  ${}^3F_3$ ,  ${}^3D_3$  and  ${}^1F_3$  terms, whose magnetic splitting factors are  $\frac{5}{4}$ ,  $\frac{13}{2}$ ,  $\frac{4}{3}$  and 1 respectively, so that  $\Sigma g$  is  $4\frac{2}{3}$  and  $\Sigma Mg$  is 14 as theory requires

$l_1$ $l_0$	$m_{l_1}$	$m_{l_2}$	$m_{s_1}$	$m_{s}$	Ξ	$\Sigma (m_l + m_s)$		Σ	(m <sub>7</sub>	+2m	s)		$\Sigma m_l$	$m_s$		
1 2	1	2 1 0 -1 -2	士皇	土量	4 3 2 1 0	3 2 1 0 -1	3 2 1 0 -1	2 1 0 -1 -2	5 4 3 2 1	3 2 1 0 -1	3 2 1 0 -1	1 0 -1 -2 -3	1½ 1 0 -½	0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$ \begin{array}{c} -\frac{1}{2} \\ 0 \\ -\frac{1}{2} \\ -1 \\ -1\frac{1}{2} \end{array} $	$ \begin{array}{c} -1\frac{1}{2} \\ -1 \\ -\frac{1}{2} \\ 0 \\ \frac{1}{2} \end{array} $
	0	2 1 0 -1 -2	±⅓	± <del>1</del>	3 2 1 0 -1	2 1 0 -1 -2	2 1 0 -1 -2	1 0 -1 -2 -3	4 3 2 1 0	2 1 0 -1 -2	2 1 0 -1 -2	$ \begin{array}{c} 0 \\ -1 \\ -2 \\ -3 \\ -4 \end{array} $	1 0 -1 -1	$\begin{array}{c} -1 \\ -\frac{1}{2} \\ 0 \\ 1 \end{array}$	$ \begin{array}{c} 1 \\ 0 \\ -\frac{1}{2} \\ -1 \end{array} $	$-1 \\ -\frac{1}{2} \\ 0 \\ 1$
	-1	2 1 0 -1 -2	$\pm \frac{1}{2}$	土皇	2 1 0 -1 -2	1 0 -1 -2 -3	1 0 -1 -2 -3	0 -1 -2 -3 -4	3 2 1 0 -1	1 0 -1 -2 -3	1 0 -1 -2 -3	-1 -2 -3 -4 -5	$ \begin{array}{c} 0^{\frac{1}{2}} \\ -\frac{1}{2} \\ -1 \\ -1\frac{1}{2} \end{array} $	$ \begin{array}{c} -1\frac{1}{2} \\ -1 \\ -\frac{1}{2} \\ 0 \\ -\frac{1}{2} \end{array} $	$0 \\ \frac{1\frac{1}{2}}{2}$	$-\frac{1}{2}$ $0$ $\frac{1}{2}$ $1$ $1\frac{1}{2}$

Fig 18 1 Magnetic quantum numbers of a pd configuration in a field so strong that the electronic vectors precess independently

Thus far the sum has been assumed independent only of the field, but if it remains unchanged in a field so strong that all electronic vectors are uncoupled, it must surely be independent of the coupling. And a logical consequence of this hypothesis is that the sum of the splitting factors is independent of the coupling when summed over all those terms of a configuration which have the same value of J For let the sum of the g values of terms having J = a be  $\Sigma g_a$ , and when M = b let  $\Sigma Mg = \sigma_b$ , then if the highest value of J is J', when M = J',

$$J' \sum g_{J'} = \sigma_{J'}$$
$$\sum g_{J'} = \sigma_{J'}/J',$$

or

and as the right-hand side is independent of the coupling, so also is  $\Sigma g_{J'}$ . When M = (J' - 1),

$$\Sigma g_J + \Sigma g_{(J'-1)} = \sigma_{(J'-1)}/(J'-1)$$

Again, the right-hand side is independent of the coupling, and so

therefore must  $\Sigma g_{(J'-1)}$  be Clearly this argument can be extended to all values of J

The constancy of the g sum was first deduced by Pauli\* and Landé† from theory, but in the last decade experiment has amply confirmed it. In the spark spectrum of chromium‡ the  ${}^4P_{\frac{1}{2}}$  and

Term	g fa	ctor
Term	Landé	Empirical
<sup>6</sup> F <sub>†</sub> <sup>6</sup> D; <sup>4</sup> D; <sup>4</sup> P;	-0 667 3 333 0 2 667	-0 671 2 841 0 3 145
Sum ≥g	5 333	5 315

Fig 18 2 g factors of those terms of the 3d<sup>4</sup> (5D) 4p configuration of Cr II, which have  $J = \frac{1}{2}$  An example of the sum rule

Manna.	g va	alues	g sums			
Term	Landé	Empirical	Landé	Empirical		
4P <sub>2+</sub> 4P <sub>1+</sub> 2P <sub>1+</sub> 4P <sub>+</sub>	Pat 1 60 1 60 Pat 1 73 1 63	1 63	1 60	1 60 3 06		
4P <sub>1</sub>	1 33 2 67 0 67	1 43 2 53 0 81	3 34	3 34		

Fig. 18.3 g factors of the p<sup>4</sup> (<sup>3</sup>P) 5s terms of A II, showing that the sum rule is obeyed

<sup>6</sup>D<sub>‡</sub> terms of the 3d<sup>4</sup>(<sup>5</sup>D) 4p configuration show very irregular g values, but the sum for the four terms which have a J value of  $\frac{1}{2}$  agrees closely with that predicted by Landé (Fig. 18.2). Other examples of the sum rule are to be found in the spark spectra of neon, $\frac{1}{2}$  argon and krypton, in Lai, Lai \*\* and Agii † Fig. 18.3, which cites the p<sup>4</sup>(<sup>3</sup>P) 5s configuration of Aii,

- \* Pauli, ZP, 1923, 16 155
- † Landé, ZP, 1923, 19 112
- 1 Kromer, ZP, 1928, 52 542 Cr II
- § Bakker and de Brum, ZP, 1931, 69 19 Ne II
- Bakker, K Akad Amsterdam, Proc 1928, 31 1041 Am
- Bakker and de Brum, ZP, 1931, 69 36 Kr II
- \*\* Russell and Meggers, BSJ, 1932, 9 665 Lai, Lai
- †† Shenstone and Blair, PM, 1929, 8 765 Ag II

brings out also one important corollary of the sum rule,  ${}^4P_{2\frac{1}{2}}$  is the only term arising from this configuration which has a J value of  $2\frac{1}{2}$ , and so its g value must be that predicted by Landé whatever the coupling

Configurations in which the g sum is abnormal are rare, but not unknown, usually the one which deviates is known to overlap another in the energy scale. In K II\* the g sum of terms having a J value of I in the configuration  $3p^5$  ( $^2P$ ) 4s is  $257 \pm 0.02$  instead of 150, this configuration overlaps  $3p^5$  3d, but not all the 3d levels are yet known, so that the combined g sum cannot be calculated. In Rb II a similar deviation occurs, where two configurations overlap  $\dagger$ 

That the g sum rule is broken when two configurations overlap is of interest, because the quantum mechanics shows that the sum of the magnetic energies of all states having the same projection of angular momentum on the axis of the magnetic field is independent of the coupling between the vectors. As the sum has to be taken over all states of the atom, the theory in this form does not give much information, if, however, only states which have nearly the same energy influence one another, † all empirical results are seen to hang together. The rule is valid for a single multiplet in spectra whose coupling is Russell-Saunders, since a single multiplet is there isolated, it is valid for a configuration when a configuration is isolated, and when two configurations overlap it is still probably true if the sum is extended over both, though this point has not yet been tested

## 3 Invariance of the Γ sum

In the Paschen-Back effect evidence is found that the sum of the displacements of those components of a multiplet, which have the same M, remains constant when the strength of the magnetic field varies. That the similar law for the g sum remains valid for any coupling provided the sum is extended to all terms of a configuration, suggests a similar extrapolation for the  $\Gamma$  sum

Compared with the g sum, the  $\Gamma$  sum is unsatisfactory, whereas

<sup>\*</sup> Whitford, PR, 1932, 39 898

<sup>†</sup> Laporte, Miller and Sawyer, PR, 1931, 38 843.

<sup>‡</sup> Goudsmit, PR, 1931, 37 664

theory can dictate absolute g values, it can dictate displacements only relative to an undetermined centroid, and only as a multiple of an undetermined constant A Accordingly, the  $\Gamma$  sum rule is not susceptible of direct verification as the g sum rule is, and indeed had there not been some regularities which cried aloud for explanation, it seems hardly probable that Goudsmit could have pushed ahead on so flimsy a scaffolding

Parent sp	ectrum		Derived spectrum
Spectrum	Interval	Spectrum	Interval
C II Si II P III S IV Cl V Ge II	p Δ <sup>2</sup> P 64 287 560 950 1495 1768	C1 S11 P11 S111 Cl IV Ge I	(2P) ns $\Delta^3$ P  3s 60 4s 45 5s 54  4s 275 5s 283  4s 527 5s 547  4s 450 5s 924  4s 1446  5s 1661 6s 1740 7s 1765
Sn II	4253	Snī	6s 3988 7s 4201
Оп	p³ Δ²D 30 p³ Δ²P 5	01	(2D) ns Δ2D 3s 20 (2P) ns Δ2P 3s 17
Ne II Na III A II	p <sup>5</sup> Δ <sup>2</sup> P 782 1371 1431 2164	Ne 1 Na 11 A 1 K 11	( <sup>2</sup> P) ns Δ <sup>8</sup> P 3s 777 4s 780 5s 778 6s 781 3s 1357 4s 1410 5s 1397 6s 1414 7s 1433 4s 2642
K m Kr n Xe n	5371 10117	Kri Kri Xei	5s 5220 6s 9129
Nı 11 Pd 11 Pt 11	d <sup>9</sup> Δ <sup>2</sup> D 1507 3539 —	Nii Pdi Pti	(2D) ns $\Delta^3$ D 4s 1508 5s 1506 6s 1506 5s 3530 6s 3532 7s 3539 6s 10132

Fig 18.4 Comparison of doublet intervals with those of the triplets derived from them, when an s electron is added

The regularities mentioned connect the arc and spark spectra of an element. Thus in a number of spectra the triplet resulting from the addition of an s electron to a doublet ground term has the same extreme interval as the doublet. The  $^3P_{2,0}$  interval from the  $s^2$  p ( $^2P$ ) ns configuration of S11 is equal to the  $^2P$  interval of S111, and this is true also of isoelectronic spectra. Again, the ( $^2P$ ) ns  $^3P_{2,0}$  interval of the inert gas spectra is independent of the

chief quantum number n and equal to the <sup>2</sup>P interval of the ionic ground term, and the same is true of the very similar  $d^9(^2D) ns$  configuration in nickel and palladium (Fig. 184) Standing in contrast to these three groups of spectra in which the arc and spark intervals are identical stand the alkaline earth triplets whose extreme intervals obey the doublet laws, just as their spark doublets do

To account for these regularities, assume that the  $\Gamma$  sum rule, like the g sum rule, is valid in a field so strong that the electronic spin and orbital vectors precess independently round the field axis, provided the sum be then taken over all those terms of a configuration which have the same value of M. Then construct a table of all the values which  ${}_{l}M_{L}$  and  ${}_{l}M_{S}$  can assume in the  ${}^{2}\mathbf{P}$  term of an ion, and of  $m_{l}$  and  $m_{s}$  for the s electron. Then if a sufficiently strong field be postulated,

$$\Gamma = A_{i}M_{Li}M_{S}$$

$$\gamma = \alpha m_{l}m_{s},$$

and

where A and a are the interval quotients of the ground term of the ion and the electron respectively, A is thus determined by the ionic term, and a presumably by the Landé doublet formula, however, when Fig. 18.5 is made out from these equations, it shows that a vanishes provided that  $m_l$  is always zero, as it is when the electron moves in an sorbit

_	$M_L$	$m_l$	$\mathcal{M}_{S}$	$m_s$	.Γ/A	y/a	$M_L$	$M_{\mathcal{S}}$	М	$\Gamma/A$
	1 0 -1	0	1/2	1/2	$\begin{array}{c} \frac{1}{2} \\ 0 \\ -\frac{1}{2} \end{array}$	0	1 0 -1	1	2 1 0	0 -12
_	1 0 -1	0	3	-1/2	$0 \\ -\frac{1}{2}$	0	1 0 -1	0	1 0 -1	0 -1
1	1 0 -1	0	-1/2	3	$-\frac{1}{2}$ $0$ $\frac{1}{2}$	0	1 0 -1	0	1 0 -1	$-\frac{1}{2}$ 0 $\frac{1}{2}$
	1 () -1	0	-}	-1/2	-1 0 1	0	1 0 -1	-1	0 -1 -2	$ \begin{array}{c} -\frac{1}{2} \\ 0 \\ \frac{1}{2} \end{array} $

Fig. 18.5 Electronic and atomic displacements in a system consisting of an ion in a -P state and an s electron

The  $\Gamma$  sums are to be taken over terms having the same value of M, so that this table must be re-arranged in the form of Fig. 18.6

Fig. 18.6. Atomic displacements of the system of Fig. 18.5 m a strong field

But the 1' sum is independent of the coupling, so that these sums must be those found empirically in a weak field. If  $\Gamma_2$ ,  $\Gamma_1$ ,  $\Gamma_1'$  and  $\Gamma_0$  are the displacements of the  ${}^3P_2$ ,  ${}^3P_1$ ,  ${}^4P_1$  and  ${}^3P_0$  torms respectively, then arranging those by their M values we obtain Fig. 18.7

Fig. 18.7. Atomic displacements of the system of Fig. 18.5 in a weak field

Accordingly

$$\begin{array}{c|ccc}
\Gamma_{2} & \frac{1}{2}A \\
\Gamma_{1} + \Gamma_{1}' & \frac{1}{2}A \\
\Gamma_{0} & 4
\end{array}.$$

These equations show that in the atom

$${}^{3}P_{2}$$
  ${}^{3}P_{0}$   $\Gamma_{2}$   $\Gamma_{0}$   ${}^{3}A$ ,

whatever the coupling, and moreover that this is equal to the <sup>2</sup>P interval of the ion

When the addition of an s electron to a <sup>2</sup>D term is considered, a similar argument shows that

$$^{3}D_{3} - ^{3}D_{1} + ^{3}A + ^{2}D_{24} + ^{2}D_{14},$$

.1 being now the interval quotient of the ionic <sup>2</sup>D term While

when the method is applied to the alkaline earth triplets, in which a p or d electron is added to a  ${}^2S$  ground term, it shows that the extreme triplet interval should depend only on the electronic quotient a and not at all on the ionic quotient A. Thus the invariance of the displacement sum satisfactorily explains the intervals observed in three different columns of the periodic table.

But if these were the points chiefly needing explanation, they do not limit the usefulness of the theory, with its aid Slater\* has explained why the alkali doublets fit a formula developed for X-ray spin doublets, while Goudsmit† has related together the interval quotients of the numerous terms which may arise from a single configuration

As an example of an X-ray spin doublet, consider the  $L_{\rm II}$   $L_{\rm III}$  doublet which arises from a p<sup>5</sup> group of electrons. The orbital and spin vectors of this group, restricted as they are by the exclusion principle, appear in Fig. 18.8

$m_{\mathcal{I}}$	$m_s$	$M_L  M_S$ $\gamma/a$	М Г/а
1 1 0 0 -1 1 1 0 -1 -1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
1 0 0 -1 -1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

Fig 188 Electronic and atomic displacements of a p<sup>5</sup> configuration

These permitted combinations are rearranged according to their M values in Fig. 18.9, and the sum of the displacements is obtained But the only two permitted values of J are  $\frac{1}{2}$  and  $1\frac{1}{2}$ , so

$M_S$	-1½	-1	<del>1</del>	11/2
$-\frac{\frac{1}{2}}{\frac{1}{2}}$	- <u>1</u>	1 0	0	$-\frac{1}{2}$
$\Sigma\Gamma_{stia}$	$-\frac{1}{2}$	1/2	1/2	$-\frac{1}{2}$

Fig. 18.9 Atomic displacements of a p⁵ configuration in a strong field arranged by the corresponding values of M and  $M_S$ 

<sup>\*</sup> Slater, PR, 1926, 28 291

<sup>†</sup> Goudsmit, PR, 1929, 31 946

that if the displacements in zero field are  $\Gamma_{i}$  and  $\Gamma_{i}$ , the displacements in a weak field must be those shown in Fig. 18 10

J	- 1½	-1/2	1	11/2
1 <del>1</del> 1	Γ <sub>1</sub>	$\Gamma_{1\frac{1}{4}}$ $\Gamma_{\frac{1}{4}}$	$\Gamma_{1\frac{1}{4}}$ $\Gamma_{\frac{1}{4}}$	Γ <sub>1</sub> ;
$\Sigma\Gamma_w$	$\Gamma_{1\frac{1}{4}}$	$(\Gamma_{\frac{1}{4}} + \Gamma_{1\frac{1}{4}})$	$(\Gamma_{\frac{1}{4}} + \Gamma_{1\frac{1}{4}})$	Γ11

Fig 18 10 Atomic displacements of a p<sup>5</sup> configuration in a weak field

Comparison of these two tables shows that, if the  $\Gamma$  sum is independent of the coupling, then

$$\begin{array}{ccc} \Gamma_{1\frac{1}{2}} = -\frac{1}{2}a \\ \Gamma_{\frac{1}{2}} + \Gamma_{1\frac{1}{2}} = & \frac{1}{2}a \end{array},$$

$$\Gamma_{11} - \Gamma_{1} = -\frac{3}{2}a,$$

so that

showing that the interval is equal to that of an alkali P doublet

To extend this method to other groups of equivalent electrons Goudsmit had to postulate Russell-Saunders coupling of the atomic vectors. Thus the  $d^2$  configuration gives rise to the terms  ${}^3F$ ,  ${}^3P$ ,  ${}^4G$ ,  ${}^4D$  and  ${}^4S$ , or six unknowns, since  $\Gamma$  is zero in all singlet terms. Calculations based on an assumed strong field however give only five equations, one for each value of M from 0 to 4, so that the  $\Gamma$  values are indeterminate. Should we assume however that the  ${}^3F$  and  ${}^3P$  terms obey the Landé interval rule, then the

M	-4	-3	-2	-1	0	1	2	3	4
1			-11	-1	- <u>1</u>	0	1 2 2	1	11/2
0				l <del>l</del>	2	11	1 0	$-\frac{1}{2}$	0
	0	- }	1 0 -1	$-\frac{1}{2}$ $-\frac{1}{2}$	$     \begin{array}{c}       0 \\       -1 \\       -2     \end{array} $	$-\frac{1}{2}$	-1		
-1	11/2	1	1 2 1	0	-\frac{1}{2} -\frac{1}{3}	-1	-11		
$\Sigma\Gamma/a$	13	1	- }	-1	-2	-1	-1	1	11/2

Fig. 18.11 Atomic displacements of a d<sup>2</sup> configuration in a strong field, arranged by the values of M and  $M_S$ 

displacements of their components may be stated in terms of only two unknowns  $A_{\rm F}$  and  $A_{\rm P}$  This is shown in Figs. 18-11, 18-12

L $J$	-4	-3	-2	-1	0	1	2	3	4
<sup>3</sup> F <sub>4</sub> <sup>3</sup> F <sub>3</sub> <sup>3</sup> F <sub>2</sub>	$3A_{ m F}$	3AF -AF	3AF -AF -4AF	3AF -AF -4AF	$3A_{ m F} \\ -A_{ m F} \\ -4A_{ m F}$	$3A_{ m F} - A_{ m F} - 4A_{ m F}$	$3A_{ m F} - A_{ m F} - 4A_{ m F}$	$3A_{ m F} - A_{ m F}$	3 <i>A</i> F
<sup>3</sup> P <sub>2</sub> <sup>3</sup> P <sub>0</sub>			$A_{ m P}$	AP -AP	AP -AP -2AP	$A_{ m P} - A_{ m P}$	$A_{ m P}$		
$^{1}G_{4}$ $^{1}D_{2}$ $^{1}S_{0}$	0	0	0	0	0 0 0	0	0	0	0

Fig. 18 12. Atomic displacements of a  $d^2$  configuration in a weak field, arranged by the values of M and  $L_J$ 

The  $\Gamma$  sum rule shows that

$$\begin{array}{lll} \text{when } M = 4 & 3A_{\mathrm{F}} = 1\frac{1}{2}a, \\ = 3 & 2A_{\mathrm{F}} = a, \\ = 2 & -2A_{\mathrm{F}} + A_{\mathrm{P}} = -\frac{1}{2}a, \\ = 1 & -2A_{\mathrm{F}} = -a, \\ = 0 & -2A_{\mathrm{F}} - 2A_{\mathrm{P}} = -2a \end{array}$$

And these equations are satisfied if

$$A_{\mathbf{P}} = A_{\mathbf{F}} = \frac{1}{2}a$$

Proceeding in this way Goudsmit\* was able to calculate the interval quotient A of different components of many supermultiplets in terms of the interval quotients a of p or d electrons, the results are summarised in Fig. 18 13

This theory has been strikingly successful in predicting experimental facts. In the d<sup>7</sup> configuration of Ru II all the terms should be inverted except the <sup>2</sup>F term, and so in fact experiment shows that they are † While in the d<sup>3</sup> configuration of Ti II; the relative separations are in very fair agreement with theory, Fig. 18·14 shows this, the separation of the <sup>2</sup>H term having been fitted to the experimental value §

- \* Goudsmit, PR, 1928, 31 948
- † Meggers and Shenstone, PR, 1930, 35 868a
- ‡ Russell, Ast PJ 1927, 66 283
- § Pauling and Goudsmit, Structure of line spectra, 1930, 163

Con- figuration	Multiplet	Interval quotient	Extreme interval	Con- figuration
p p² p³	<sup>2</sup> P <sup>3</sup> P <sup>2</sup> D <sup>2</sup> P	$\begin{array}{c} a \\ \frac{1}{2}a \\ 0 \\ 0 \end{array}$	$ \begin{array}{c} 1\frac{1}{2}a \\ 1\frac{1}{2}a \\ 0 \\ 0 \end{array} $	- p <sup>5</sup> - p <sup>4</sup> - p <sup>3</sup>
d	2D	a	$2\frac{1}{2}a$	- d9
d²	3F 3P	$\frac{\frac{1}{2}a}{\frac{1}{2}a}$	$rac{3rac{1}{2}a}{1rac{1}{2}a}$	- d <sup>8</sup>
ď₃	<sup>4</sup> F <sup>4</sup> P <sup>2</sup> H <sup>2</sup> G <sup>2</sup> F <sup>2</sup> D <sup>2</sup> P	15 to a a to to a a a to to a a a a to a a a a	3½a ½a ½a ½¼a - ¼a - ¼a a	− d <sup>7</sup>
d <sup>4</sup>	<sup>5</sup> D <sup>3</sup> H <sup>3</sup> G <sup>3</sup> F <sup>3</sup> D <sup>3</sup> P	$ \begin{array}{c c}  & 4a \\  & 1 & 0a \\  & 1 & 0a \\  & 1 & 0a \\  & 1 & 1 & 0a \\  & 1 & 1 & 1a \\  & 1 & 1 & 1a \\  & 1 & 1 & 2a \\  & 1 & 2a \end{array} $	52a 116a 276a 275a -15a -15a	_ ds
d <sup>5</sup>	All	ō	0	- d <sup>5</sup>

Tig 18 13 Atomic interval quotients of terms arising from shells of p and d lectrons in terms of the electronic interval quotients

$J_{\frac{1}{2}}$	, <u>1</u>	1 2	1 2	$3\frac{1}{2}$ 4	1 51
			700.4	128 4	
b 4F	Observed	75 8	103 4		_
1	Calculated	74 1	103 6	133 2	_
a 4P	32 0	122 3	_	_	_
	44 4	74 1	_	<b> </b> -	
a 2H	_		_	<u> </u>	978
					(97 8)
a 2G				120 5	_
" "		1		120 0	1
b 2F		_	-599	<u> </u>	1 —
0 1			-518	i	1
b 2D		129 4	1 310	_	1 —
		_8			l —
2D	_			<u> </u>	
		$\Sigma = 74.1$	_	_	
a <sup>2</sup> P	125 0	_	i —	-	-
	889		Į.	1	

a This state has not been identified

Fig 18 14 Term intervals in the  $d^3$  configuration of Ti II, to obtain the calculated values the  $^2H$  term has been fitted to the experimental value

Nevertheless, in spite of its successes the theory has its difficulties, of these one example will suffice. In the  $p^5$  ns terms of neon, theory shows that  $\Gamma_0$ ,  $(\Gamma_1 + \Gamma_1')$  and  $\Gamma_2$  are independent of the coupling and therefore of the chief quantum number. Now  $\Gamma$ has always been interpreted as the displacement of a term from the centroid of the multiplet, so that for the  ${}^1\!P$  term  $\Gamma_1'$  should be zero, indeed  $\Gamma$  has been assumed zero for all singlet terms in some of the above calculations. But if this assumption is made  $(\Gamma_1 - \Gamma_0)$ 

Term	${}^{1}P_{1}$ $ms_{2}$	<sup>3</sup> P <sub>0</sub> ms <sub>3</sub>	<sup>8</sup> P <sub>1</sub> ms <sub>4</sub>	<sup>3</sup> P <sub>2</sub> ms <sub>5</sub>		
Interval	Γ1'-	$\Gamma_0$ $\Gamma_0$ –	$\Gamma_1$ $\Gamma_1-1$	Γ2	$\Gamma_0 - \Gamma_2$	$\Gamma_1' + \Gamma_1 - 2\Gamma_0$
1		39110 8 0 1 359			776 8	7107
2	(14506 5) ( <i>148</i>	(14651 9) 5 4) (489	(15141 5) 6) (290	(15 <b>4</b> 32 2) 7)	(780 3)	(-3442)
3	7272 9 50	7323 1 9 2 693	8016 7 6 84	8101 3 6	778 2	-6
4	4201 8 2	4223 5 1 7 7 <b>3</b> 8	4962 1 6 42	5004 8 7	781 3	- 7169
5	1.	2616 6 1 2 755	8 24	3	780 1	- 7446
6		1675 1 7-4 764	8 16	2	781 0	- 757 4
7	1072 4	1077 3 1-9 771	1848 5 2 9 6	1858 1	780 8	- 766 3

Figures in brackets have been intrapolated from the series formula

Fig 18 15 Energies and intervals of the s terms of neon; the term values are measured down from the series limit

should be independent of n just as  $\Gamma_2 - \Gamma_0$  is; a prediction which experiment does not support. Moreover, the most obvious way of dodging the difficulty is blocked, for if one suggests plausibly enough that when the coupling is no longer Russell-Saunders one may not rightly speak of a singlet term, still though  $\Gamma_1$  need not be zero, yet  $(\Gamma_1 + \Gamma_1)$  must be constant. And if this be admitted, theory predicts that

$$(\Gamma_1 + \Gamma_1') - 2\Gamma_0 = (\Gamma_1 - \Gamma_0) + (\Gamma_1' - \Gamma_0)$$

should be constant, a prediction quite at variance with experiment (Fig. 18 15)

### 4 The intensity sum

That the intensity sum is proportional to the statistical weight (2J+1) is a thesis, which has been developed by successive stages from the SP combination, in which it is true of a single line, through the general multiplet, PD, to the super-multiplet or configuration in which the sum must be taken over all lines which originate in terms having the same value of J\*

This development is so closely analogous to the development of the g and  $\Gamma$  sums, that one expects similar deviations to occur when configurations overlap. And in fact abnormal intensities in Bai have been ascribed to this cause  $\dagger$ 

## 5 General coupling of two electrons

The coupling of electron vectors postulated by Russell and Saunders explains that division of levels into multiplets which is characteristic of light atoms. It explains, for example, why in the s<sup>2</sup> p s configuration of Ci the four levels are divided into a triplet below and a singlet above, it even explains the 2-1 interval ratio, but when in Pb i these four levels divide into two diads, the Russell-Saunders coupling fails. What then is to be put in its place?

In the model the interaction of ion and electron is represented as the coupling of four vectors. This means that there are six interactions, but these belong to only four different types, since  $(\mathbf{l_1s_1})$  and  $(\mathbf{l_2s_2})$  are identical and so are  $(\mathbf{l_1s_2})$  and  $(\mathbf{l_2s_1})$ , of these four types,  $(\mathbf{s_1s_2})$ ,  $(\mathbf{l_1l_2})$ ,  $(\mathbf{l_1s_1})$  and  $(\mathbf{l_1s_2})$ , the quantum mechanics states that the fourth may be neglected, unless the atom is extremely light, but the other three are all important. In spectra which conform to the Russell-Saunders type, the spin coupling  $(\mathbf{s_1s_2})$  determines the separation of terms of different multiplicity, the orbital coupling  $(\mathbf{l_1l_2})$  that of terms of different name, and the orbit-spin coupling  $(\mathbf{l_1s_1})$  the multiplet intervals. As the separation of the terms is a measure of the coupling, and in Russell-Saunders spectra terms of different multiplicity are

<sup>\*</sup> Harrison and Johnson, PR, 1931, 38 758, give the full theory and compare it with experiment

<sup>†</sup> Langstroth, PRS, 1933, 142 286

widely separated, the  $(s_1s_2)$  coupling must be strong. The  $(l_1l_2)$  coupling is weaker than the  $(s_1s_2)$  but stronger than the  $(l_1s_1)$ , for terms with different names but the same multiplicity are less widely separated than terms of different multiplicity but more widely than different components of the same multiplet \*

If the evidence of the quantum mechanics is to be accepted, and the  $(\mathbf{l_1} \mathbf{s_2})$  coupling ignored, there are still three alternatives to the coupling postulated by Russell and Saunders If the latter is written

(A) 
$$\{(\mathbf{l}_1\mathbf{l}_2)(\mathbf{s}_1\mathbf{s}_2)\} = \{\mathbf{LS}\} = \mathbf{J},$$

the other three are

(B) 
$$\{(l_1s_1)(l_2s_2)\} = \{j_1j_2\} = J,$$

(C) 
$$\{[(l_1s_1)s_2]l_2\} = \{[j_1s_2]l_2\} = \{j'l_2\} = J,$$

$$(D) \qquad \qquad \{[(\mathbf{l_1}\mathbf{s_1})\,\mathbf{l_2}]\,\mathbf{s_2}\} \!=\! \{[\mathbf{j_1}\mathbf{l_2}]\,\mathbf{s_2}\} \!=\! \{\mathbf{j''}\,\mathbf{s_2}\} \!=\! \mathbf{J}$$

These three all show an ion, whose orbital and spin vectors are not at once unlinked when a second electron is added, but differ in the influence the ion has on the coupling of the series electron. Thus in (B) the coupling  $(\mathbf{l_2s_2})$  is preserved and the atomic resultant  $\mathbf{J}$  appears as the sum of two electronic vectors  $\mathbf{l_1l_2}$ . In (C) the ion shows a special attraction for the spin vector  $\mathbf{s_2}$  of the second electron, and so breaks the  $(\mathbf{l_2s_2})$  coupling, while in (D) the ion attracts particularly the  $\mathbf{l_2}$  vector

All three coupling types have been considered by those who have tried to interpret abnormal spectra, in particular, the magnetic g factors have been calculated and compared with experiment in more than one spectrum,† but the result of this work has so far been to show that types (C) and (D) have no advantage over the simpler (11) coupling of type (B) Incidentally, too, the three are identical when the electron added occupies an s orbit

The further discussion of abnormal spectra will therefore be simplified by treating the (JJ) coupling as though it were the only alternative to that postulated by Russell and Saunders

<sup>\*</sup> Hund, Linienspektren, 1927, 91 f

<sup>†</sup> For g factors of all four coupling types, see p 145

## 6 (jj) coupling

In the change from weak to strong magnetic field, while the energies change, the number of states and their magnetic quantum numbers, M, do not, similarly, in the change from (**LS**) to (11) coupling, while the relative energies change, the J values do not Accordingly, in the complex spectrum of a heavy metal, such as platinum, values of J can be assigned to the empirical terms, but the Russell-Saunders notation, depending as it does on L and S, is of little use

$l_1$	$l_2$	$\jmath_1$	J <sub>2</sub>	J	Names if coupling is R S
0	0	1/2	1/2	0	<sup>1</sup> S <sub>0</sub> <sup>3</sup> S <sub>1</sub>
0	1	1/2	1 1 1	0 1 1 2	<sup>3</sup> P <sub>0</sub> <sup>3</sup> P <sub>1</sub> <sup>1</sup> P <sub>1</sub> <sup>3</sup> P <sub>2</sub>
1	1	12 12 12 12	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0 1 1 2 1 2 0 1 2 3	$^{1}S_{0}  ^{3}P_{0}$ $^{1}P_{1}  ^{3}S_{1}  ^{3}P_{1}  ^{3}D_{1}$ $^{1}D_{2}  ^{3}P_{2}  ^{3}D_{2}$ $^{3}D_{3}$

Fig. 18 16. Terms arising from the  $\eta$  coupling of two unlike electrons in s. s, sp and p. p states, the J values are the same as those of the corresponding Russell-Saunders terms.

To illustrate the invariance of J, consider the terms arising from the (jj) coupling of two electrons. The values of j permitted a single electron are  $(l\pm\frac{1}{2})$ , and the terms arising from the combination of two electrons can be deduced by combining the two j vectors. When the electrons are not equivalent, J is simply the vectorial sum of  $j_1$  and  $j_2$ , and there are no restrictions, thus two electrons having j values of  $1\frac{1}{2}$  and  $2\frac{1}{2}$  produce four states having j values of  $j_1$ ,  $j_2$ ,  $j_3$ ,  $j_4$ . Other examples are given in Fig. 18.16. On the other hand, when the two electrons are equivalent, the Pauli exclusion principle does not allow two electrons with the same

values of n, l, j and m, but when this condition is introduced, as it is in the derivation of Figs 18 17, 18 18, the resulting J values are still identical to those developed by the (**LS**) coupling The J

$l_1$	$l_2$	J <sub>1</sub>	J 2	$m_1$	$m_2$	М	J	Names with R S coupling
1	1	12	1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1	$\frac{1}{2}$ $1\frac{1}{2}$ $\frac{1}{2}$ $-\frac{1}{2}$	-12 -121-121-121-121-121-121-121-121-121	0 2 1 0 0 -1 -2	0 1 2 0 2	<sup>1</sup> S <sub>0</sub> <sup>3</sup> P <sub>0</sub> <sup>3</sup> P <sub>1</sub> <sup>1</sup> D <sub>2</sub> <sup>3</sup> P <sub>2</sub>

Fig 1817 Terms arising from the jj coupling of two equivalent p electrons

$l_1$	$l_2$	$l_{3}$	11	J2	Ĵз	$m_1$	$m_2$	$m_3$	М	J	Na R S	mes wit	h ng
1	1	1	1/2	1/2	11/2	1/2	$-\frac{1}{2}$	1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1	1 1/21 1/21 1/21 1/21 1/21 1/21 1/21 1/	11/2			
			1/2	11/2	11/2	$-\frac{1}{2}$	$   \begin{array}{c}     1\frac{1}{2} \\     \hline     2 \\     -\frac{1}{2} \\     1\frac{1}{2} \\     -\frac{1}{2}   \end{array} $	- 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	211112 12 12 12 12 12 12 12 12 12 12 12	2½ 1½	<sup>2</sup> P <sub>1‡</sub>	<sup>2</sup> P <sub>‡</sub> <sup>2</sup> D <sub>1‡</sub> <sup>2</sup> D <sub>2‡</sub>	4S <sub>1‡</sub>
			11/2	11/2	11/2	1½	$-\frac{1}{2}$ $-\frac{1}{2}$ $-\frac{1}{2}$	$ \begin{array}{r} -\frac{1}{2} \\ -\frac{1}{2} \\ -\frac{1}{2} \\ -\frac{1}{2} \end{array} $	$ \begin{array}{c c} 1\frac{1}{2} \\ -\frac{1}{2} \\ -1\frac{1}{2} \end{array} $	11/2			

Fig 18 18 Terms arising from the 11 coupling of three equivalent p electrons

values to be expected from more complex configurations are shown in Fig 18 19

Turning from the states themselves to their energies, consider first the addition of an s electron to an ion in the <sup>2</sup>P state, this actually occurs in columns IV and VIII, and much is known of the

resulting terms The two ionic levels are defined by  $j_1$ , which here assumes the values  $1\frac{1}{2}$  and  $\frac{1}{2}$  The addition of the second electron splits each of the levels in two, for  $j_2$  can orient itself parallel or anti-parallel to  $j_1$   $j_2$  is here identical with  $s_2$ , since  $l_2$  is zero. Thus the atomic level scheme consists of two 'diads', and the

Con- figura		ber of					evels 11			
tion	1/2	$1\frac{1}{2}$	$2\frac{1}{2}$	0	1	2	3	4	5	6
p²	2	1 2		1	1	1 1				
d²		2 1	1 2	1 1	1	1 1 1	1	1		
d⁴		4 3 2 1	1 2 3 4	1 2 1 1	1 1 2	1 4 2 1	1 2 3	1 3 2 1	1 1	1 1
Con figura- tion	1/2	$j$ $1\frac{1}{2}$	21	1/2	$1\frac{1}{2}$	$2\frac{1}{2}$	$J$ $3\frac{1}{2}$	41/2	5½	6 <del>1</del>
p <sup>3</sup>	2	1 2 3		1	1 1 1	1				
d <sup>3</sup>		3 2 1	1 2 3	1 1	1 1 2 1	2 2 1	1 2	1 1 1	1	
d <sup>5</sup>		4 3 2 1	1 2 3 4 5	1 2 1	2 3 2	1 2 4 2 1	2 3 2	1 3 1	1 1 1	1

Fig. 18 19 Terms arising from various numbers of equivalent p and d electrons

distance between the diads, being due to the coupling  $(l_1s_1)$ , must be greater than the interval of either diad, for the latter is due to  $(l_1l_2)$  Further, the relative positions of the two terms can be foretold, for the energy is due primarily to the interaction of  $l_1$  and  $s_1$  and secondarily to the interaction of  $s_1$  and  $s_2$  Hund's rule states that the energy of interaction of  $s_1$  and  $s_2$  is small

when the angle between them is small, so that in the lower level of each dad s<sub>1</sub> and s<sub>2</sub> will be parallel. The levels constructed on this principle are shown in Figs. 18 20 and 18 22, the former

1	ome levels	Vector coupling	Atomic levels	J
Jı	1, +8,	$ \begin{array}{ccc} \mathbf{l_1} & \mathbf{s_1} \\ \hline \mathbf{s_2} & \neg \end{array} $	$\mathbf{J} = \mathbf{J_1} - \mathbf{s_2} - \mathbf{m}$	1,
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$J = j_1 + s_2 - \cdots$	1,+1
31	l <sub>1</sub> - s <sub>1</sub>	$ \frac{l_1}{s_1 \leftarrow s_2 \rightarrow} $	$J = J_1 + s_2$	1,
•	, -1	$ \begin{array}{c} 1_{1} \\$	$\mathbf{J} = \mathbf{j_1} - \mathbf{s_2} - \cdots$	1,-1

Fig. 18.20 Energy levels resulting when an s electron is added to an ion in an erect doublet state, in coupling is assumed

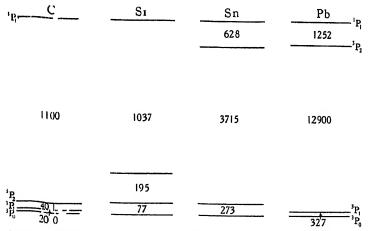


Fig. 18 21 Intervals of low  $s^2p$  s terms in four elements of column IV, the scale is adjusted so as to make the  ${}^1P_1 - {}^3P_0$  interval the same in all elements. Note the change from LS coupling in C i to jj in Pb i

representing an erect and the latter an inverted parent term, the first agrees well with the empirical  $s^2p$  ns terms of tin and lead (Fig. 18.21), and the second with the  $p^5$  ( $^2P$ ) ns terms of the mert gases (Fig. 18.23)

But one may ask, why does the addition of an s electron to a <sup>2</sup>P ground term produce two diads in columns IV and VIII, when the addition of a p electron to a <sup>2</sup>S ground term produces triplets and singlets in column II The couplings which have to be contrasted are

$$\begin{aligned} \{s_1(l_2s_2)\} &= \{s_1J_2\} & \text{ in the alkaline earths,} \\ \text{and} & \{(l_1s_1)s_2\} &= \{j_1s_2\} & \text{ in column IV} \end{aligned}$$

In both the coupling of the electronic vector  $\mathbf{j}$  with the isolated spin vector will decrease rapidly in strength with increase of the chief quantum number, the coupling energy being roughly proportional to  $n^{\star-3}$  But the interaction of the orbital vector with its own spin vector differs in the two columns, in the alkaline earths the orbital vector concerned is the orbital vector of the series electron, so that the coupling  $(\mathbf{l_2s_2})$  will decrease in strength with increase of the chief quantum number just as the  $\{\mathbf{js}\}$  coupling does, in column IV, on the other hand, the orbital vector concerned is the orbital vector of the ion, and the coupling of this with its own spin vector remains unchanged throughout the series, being determined by the doublet interval of the ion \*

In the addition of an selectron to a  $^2\mathrm{P}$  term, the energy sequence of J values happens to be identical with that produced by (LS) coupling, but the two will not always agree. In the  $5\mathrm{s}^2$   $5\mathrm{p}^4$  ( $^3\mathrm{P}$ ) 6s configuration of Ir† the five levels can be named  $^4\mathrm{P}_{2\frac{1}{2},1\frac{1}{2},\frac{1}{2}}$ ,  $^2\mathrm{P}_{1\frac{1}{2},\frac{1}{2}}$ , for the J values occur in that order from below upwards, but the intervals are 1459, 4803, 924 and 4530 cm  $^{-1}$ , and so are actually more consistent with a (11) coupling, for they divide the terms into a lower diad, which we interpret as  $(^3\mathrm{P}_2$   $^2\mathrm{fs})_{2\frac{1}{2},1\frac{1}{2}}$ , a middle diad  $(^3\mathrm{P}_1$   $^3\mathrm{fs})_{\frac{1}{2},1\frac{1}{2}}$  and an upper monad  $(^3\mathrm{P}_0$   $^3\mathrm{fs})_{\frac{1}{2}}$ , the critical will not fail to observe, however, that if the (11) coupling was rigid, the J values of the middle diad would be interchanged

But in fact even in those spectra in which the terms arising from different ionic states are most widely separated, spectra such as RnI, CsII, XeI and XeII, the individual terms of a configuration are arranged in no consistent order. In RnI the four

<sup>\*</sup> Pauling and Goudsmit, Structure of line spectra, 1930, 104

<sup>†</sup> Evans, S F, PRS, 1931, 133 417

terms ( ${}^{2}P_{1\frac{1}{2}}$   $p_{1\frac{1}{2}}$ ) might lie consistently below the two terms ( ${}^{2}P_{1\frac{1}{2}}$   $p_{\frac{1}{2}}$ ), but in fact the six empirical terms cannot be separated into two groups

# 7. Calculation of g for any coupling

Less important than the sum rule at the moment because data is scanty, but destined perhaps to be equally useful, is the calculation of g for any coupling Following Landé, Goudsmit and Uhlenbeck\* have shown that if any vector  $\mathbf{Z}$  is the resultant of two other vectors  $\mathbf{X}$  and  $\mathbf{Y}$ , so that the permissible values of  $\mathbf{Z}$  are determined by

then 
$$|X+Y| \ge Z \ge |X-Y|,$$

$$g(Z) = \frac{Z(Z+1) + X(X+1) - Y(Y+1)}{2Z(Z+1)} g(X)$$

$$+ \frac{Z(Z+1) + Y(Y+1) - X(X+1)}{2Z(Z+1)} g(Y)$$

With this assumption consider the four coupling types of an earlier section

(A) 
$$\{(\mathbf{l_1l_2})(\mathbf{s_1s_2})\} = \{\mathbf{LS}\} = J$$

J is the sum of the L and S, so

$$\begin{split} g\left( J \right) \! = \! \frac{J\left( {J + 1} \right) \! + \! L\left( {L + 1} \right) \! - \! S\left( {S + 1} \right)}{2J\left( {J + 1} \right)} g\left( L \right) \\ + \frac{J\left( {J + 1} \right) \! + \! S\left( {S + 1} \right) \! - \! L\left( {L + 1} \right)}{2J\left( {J + 1} \right)} g\left( S \right) \! . \end{split}$$

Now L is the sum of the vectors  $l_1$  and  $l_2$ , so

$$\begin{split} g\left(L\right) \! = \! \frac{L\left(L\!+\!1\right) \! + \! l_{1}\left(l_{1}\!+\!1\right) \! - \! l_{2}\left(l_{2}\!+\!1\right)}{2L\left(L\!+\!1\right)} \, g\left(l_{1}\right) \\ + \! \frac{L\left(L\!+\!1\right) \! + \! l_{2}\left(l_{2}\!+\!1\right) \! - \! l_{1}\left(l_{1}\!+\!1\right)}{2L\left(L\!+\!1\right)} \, g\left(l_{2}\right) \end{split}$$

= 1, if 
$$g(l) = 1$$
 for all values of  $l$ 

And similarly g(S) = 2, if g(s) = 2 for all values of s Substituting these values in the expression for g(J) gives at once the usual Landé formula

$$g = 1 + \frac{J(J+1) + S(S+1) - L(L+1)}{2J(J+1)}$$

\* Goudsmit and Uhlenbeck, ZP, 1926, 35 618

This analysis brings out, perhaps more clearly than any other, the cause of the whole anomalous Zeeman effect, which is nothing else than the double magnetism of the electron

If there are more than two elections active one may assume that the binding of  $s_1$  and  $s_2$  is tighter than that of their resultant  $s_{1,2}$  with  $s_3$ , then one may first work out  $g(s_{1,2})$  and then combine  $s_{1,2}$  with  $s_3$  But for the Russell-Saunders coupling g(L) is always 1 and g(S) always 2

(B) 
$$\{(\mathbf{l_1}\mathbf{s_1})(\mathbf{l_2}\mathbf{s_2})\} = (\mathbf{J_1}\mathbf{J_2}\} - \mathbf{J}$$

**J** is compounded of  $j_1$  and  $j_2$ , so

$$\begin{split} g\left(J\right) &= \frac{J\left(J+1\right) + \jmath_{1}\left(\jmath_{1}+1\right) - \jmath_{2}\left(\jmath_{2}+1\right)}{2J\left(J+1\right)} g\left(\jmath_{1}\right) \\ &+ \frac{J\left(J+1\right) + \jmath_{2}\left(\jmath_{2}+1\right) - \jmath_{1}\left(\jmath_{1}+1\right)}{2J\left(J+1\right)} g\left(\jmath_{2}\right) \end{split}$$

The  $g(j_1)$  of this expression appears in Landé's table simply as the g factor of some doublet term, for  $j_1$  is the sum of  $l_1$  and  $s_1$ , only one electron being active

Very similar to this (jj) coupling for two electrons is the binding of the series electron near the limit of a term sequence, indeed the equation is unaltered, save that the ground term of the ion is not necessarily a doublet

(C) In the coupling

$$\{[(\mathbf{l_1s_1})\mathbf{s_2}]\mathbf{l_2}\} = \{[\mathbf{j_1s_2}]\mathbf{l_2}\} = \{\mathbf{j'l_2}\} = \mathbf{J},$$

**J** is the resultant of 1' and  $1_2$ , so

$$\begin{split} g\left( J \right) \! = \! \frac{J\left( J + 1 \right) \! + \! \jmath'\left( \jmath' + 1 \right) \! - \! l_{2}\left( l_{2} \! + \! \frac{1}{2} \right)}{2J\left( J \! + \! 1 \right)} g\left( \jmath' \right) \\ + \frac{J\left( J \! + \! 1 \right) \! + \! l_{2}\left( l_{2} \! + \! 1 \right) \! - \! \jmath'\left( \jmath' \! + \! 1 \right)}{2J\left( J \! + \! 1 \right)} g\left( l_{2} \right) \end{split}$$

In this equation  $g(l_2) = 1$ , and j' is the resultant of  $j_1$  and  $s_2$ , so that

$$\begin{split} g\left(j'\right) = & \frac{\jmath'\left(j'+1\right) + \jmath_{1}\left(\jmath_{1}+1\right) - s_{2}}{2\jmath'\left(j'+1\right)} g\left(\jmath_{1}\right) \\ & + \frac{\jmath'\left(j'+1\right) + s_{2}\left(s_{2}+1\right) - \jmath_{1}\left(\jmath_{1}+1\right)}{2\jmath'\left(j'+1\right)} g\left(s_{2}\right) \end{split}$$

Here  $g(j_1)$  may be taken from Landé's doublet table, while  $g(s_2)$  is 2, as always for a single electron

(D) The coupling  $\{[(\mathbf{l_1s_1})\mathbf{l_2}]\mathbf{s_2}\}$  is so similar to (C) that it need not be worked out in detail

The values to be predicted by each of these four coupling types have been worked out for certain spectra whose Zeeman splitting is irregular, but no close agreement with experiment has ever been found Coupling types (B), (C) and (D) often give better

J		Co	uplir	ıg sch	eme				g	values			J
	A	$\jmath_1$	B J <sub>2</sub>	y' C	$l_2$	ງ″່	D 82	A	В	С	D I	Em- pirical	
3½ 2½ 2½	<sup>4</sup> D <sub>31</sub> <sup>4</sup> P <sub>21</sub> <sup>4</sup> D <sub>21</sub> <sup>2</sup> D <sub>21</sub>	2 2 1 2		$2\frac{1}{2}$ $2\frac{1}{2}$ $1\frac{1}{2}$	1 1 1	3 2 2 3	12 12 12 12 12 12 12 12 12 12 12 12 12 1	1 43 1 60 1 37 1 20	1 43 1 44 1 40 1 33	1 43 1 53 1 40 1 24	1 43 1 53 1 40 1 24	1 43 1 60 1 33 1 24	3 <del>1</del> 2 <del>1</del>
11	<sup>4</sup> P <sub>1</sub> ; <sup>4</sup> D <sub>1</sub> ; <sup>4</sup> S <sub>1</sub> ; <sup>2</sup> D <sub>1</sub> ; <sup>2</sup> P <sub>1</sub> ;	2 0 2 1 1		1	1 1 1 1	1 2 1 2 1		≥g 4 17 1 73 1 20 2 00 0 80 1 33	4 17 1 47 1 33 1 67 1 22 1 38	4 17 1 49 1 29 1 84 1 11 1 33	4 17 1 50 1 30 1 83 1 10 1 33	4 17 1 73 1 20 2 00 0 90 1 23	11
ł	<sup>4</sup> P <sub>1</sub> <sup>4</sup> D <sub>1</sub> <sup>2</sup> P <sub>1</sub> <sup>2</sup> S <sub>2</sub>	1 0 1 2	121212	11/2	1 1 1 1	0 1 1 1	-cu-for-for-for	$\Sigma g 7 06$ $\begin{array}{c} 2 67 \\ 0 00 \\ 0 67 \\ 2 00 \\ \hline \Sigma g \overline{5 33} \end{array}$	7 06 1 78 0 67 1 22 1 67 5 33	7 06 2 11 0 67 0 89 1 67 5 33	7 06 2 00 0 67 1 00 1 67 5 33	7 06 2 67 0 00 0 99 1 68 5 34	1

Fig 18 24 g factors of the p4 (3P) 4p terms of A 11 compared with values calculated for four different couplings. The sum rule is valid although the g factors are abnormal (Bakker, K Ahad Amsterdam, 1928, 31 1041)

agreement for certain terms, but none of them has been found to give close agreement even for one configuration in one element A good example of results obtained is afforded by the (3P)4p configuration of A II (Fig. 18 24)

As there is evidence that departures from the interval rule and Landé's g formula are both signs of a break from the Russell-Saunders coupling, a study of the variation of g in a series or in a sequence of homologous spectra has been a long felt want Recently Pogány\* has supplied the need by studying the change in g in the  $p^5$  ( $^2P$ ) is terms of the inert gases. This configuration produces two terms having a J value of I, and in neon both in-

<sup>\*</sup> Pogány, ZP, 1935, 93 376

tensity laws and magnetic splitting factors show that the lower is  ${}^3P_1$  and the higher  ${}^1P_1*$  Of these  ${}^3P_1$  approaches the lower limit of the ion, and must therefore flow to the (JJ) coupling term of ( ${}^2P_{1\frac{1}{2}}$  s), with a g value of 7/6, while the higher term approaches the higher limit and must flow to ( ${}^2P_1$  s)<sub>1</sub> with a g value of 4/3 Thus as the coupling changes the magnetic splitting factor of

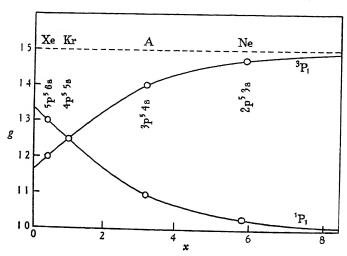


Fig 18 25 g factors of the s terms of the mert gases, showing the transition from LS to 11 coupling (After Pogany, ZP, 1935, 93 376)

the  $^{8}P_{1}$  term flows from 1 5 to 1 17, while the g factor of the  $^{1}P_{1}$  term flows from 1 0 to 1 33, this shows that the g values cross and that for some particular coupling the two g values must be equal Experiment has not yet revealed the steps in this transition in the series of neon, but the low terms of all inert gases are readily accessible and Pogány has shown five steps in the analogous transition from the (LS) coupling characteristic of light to the (jj) characteristic of heavy atoms, in neon the g values approach the ideal values of 1 5 and 1 0, being 1 47 and 1 03, whereas in krypton they are equal, and in xenon become 1 20 and 1 30 (Fig. 18 25). A similar transition can be detected in the g terms (Fig. 18 26).

	(LS) Neon coupling (2P) 3p		Argon (2P) 4p		Krypton ( <sup>2</sup> P) 5p 6p			Xenon (2P) 6p		(jj) coupling			
Term	g	Term	g	Term	g	Term	g	g	Term	g	$\jmath_1$	$\jmath_2$	g
<sup>3</sup> P <sub>0</sub> <sup>1</sup> S <sub>0</sub>	0	p <sub>1</sub> p <sub>3</sub>	0	P <sub>1</sub> P <sub>5</sub>	0	$\begin{array}{c} \mathbf{p_1} \\ \mathbf{p_5} \end{array}$	0	0	p <sub>1</sub> p <sub>5</sub>	0	$1\frac{1}{2}$	$1\frac{\frac{1}{2}}{2}$	0
<sup>3</sup> P <sub>1</sub> <sup>1</sup> P <sub>1</sub> <sup>3</sup> D <sub>1</sub> <sup>3</sup> S <sub>1</sub>	15 10 05 20	P <sub>2</sub> P <sub>5</sub> P <sub>7</sub> P <sub>10</sub>	1 340 0 999 0 699 1 984	P <sub>2</sub> P <sub>4</sub> P <sub>7</sub> P <sub>10</sub>	1 379 0 819 0 840 1 962	P <sub>3</sub> P <sub>4</sub> P <sub>7</sub> P <sub>10</sub>	1 425 0 619 1 028 1 891	1 384 0 635 1 046 1 820	P <sub>2</sub> P <sub>4</sub> P <sub>7</sub> P <sub>10</sub>	1 02			1 5 0 67 1 33 1 5
$^{\mathrm{3}\mathrm{D}^{2}}_{\mathrm{3}\mathrm{D}^{2}_{2}}$	1 5 1 17 1 0	P <sub>4</sub> p <sub>6</sub> p <sub>8</sub>	1 301 1 229 1 137	p <sub>3</sub> p <sub>6</sub> p <sub>8</sub>	1 248 1 302 1 121	$egin{array}{c} \mathbf{p_2} \\ \mathbf{p_6} \\ \mathbf{p_8} \end{array}$	1 163 1 400 1 116	1 406 1 110	P <sub>3</sub> P <sub>6</sub> P <sub>9</sub>	1 183 1 402 1 113	$1\frac{1}{2}$ $1\frac{1}{2}$ $1\frac{1}{2}$	$1\frac{1}{2}$ $1\frac{1}{2}$	1 17 1 33 1 17
$^3\mathrm{D}_3$	1 33	P <sub>9</sub>	1 329	$p_{9}$	1 333	$\mathbf{p_9}$	1 333	1 333	p <sub>8</sub>		11/2	11/2	1 33

Fig 18 26 g factors of the p terms of the mert gases, showing the transition from LS to jj coupling These terms arise as  $p^5$  (<sup>2</sup>P) np

Sources Ne Back, AP, 1925, 76 330, which is in good agreement with Murakawa and Iwama, Inst Phys and Chem Tokyo, 1930, 13 289 A Pogany, ZP, 1935, 93 364, which agrees well with Terrien and Dijkstra, J de Phys 1934, 5 443 Kr and Xe Pogány, ZP, 1935, 93 376

### 8 Electronic displacements

In an earlier chapter, while trying to explain why terms are inverted if they arise from a shell more than half full, resort was had to the theory that the atomic displacement  $\Gamma$  may be regarded as the sum of electronic displacements  $\gamma_1$  and  $\gamma_2$ , and it was shown that provided the coupling is Russell-Saunders, the relation between the two is

$$\begin{split} \Gamma = & \gamma_1 + \gamma_2 = \cos\left(\mathbf{LS}\right) \Sigma a_1 l_1 \cos\left(l_1 \mathbf{L}\right) s_1 (\mathbf{s_1 S}) \\ = & LS \cos\left(\mathbf{LS}\right) \Sigma a_1 \frac{l_1}{L} \cos\left(l_1 \mathbf{L}\right) \frac{s_1}{S} \cos\left(\mathbf{s_1 S}\right). \end{split} \tag{13 2}$$

The quantity summed in this expression is commonly abbreviated as the interval quotient A, so that

$$A = \sum a_1 \frac{l_1}{L} \cos(\mathbf{l_1 L}) \frac{s_1}{S} \cos(\mathbf{s_1 S})$$
 (18 1)

If this equation is applied to the addition of an electron to an ion, the expression for the interval quotient A will in general contain two interval quotients  $a_1$  and  $a_2$ , and no method is known

separating these. But under certain conditions the expression simplifies, thus if either the ion or the electron is in an sistate, or if the ion is in a singlet state, one of the interval quotients vanishes, while if the two electrons are equivalent  $a_1$  and  $a_2$  are equal. The method cannot be extended to the combination of three electrons, unless two are assumed so tightly linked that they are quite undisturbed by the third electron

Thus consider the addition of an electron  $(l_2s_2)$  to an ionic S term defined by  $(l_1s_1)$ , then since  $l_1$  is zero,  $a_1$  vanishes from the expression for A, and there is left simply

$$A = a_2 \frac{l_2}{L} \cos(l_2 \mathbf{L}) \frac{s_2}{S} \cos(\mathbf{s}_2 \mathbf{S})$$
 (18 2)

In this equation

$$\begin{split} \frac{l_2}{\bar{L}}\cos{(\mathbf{l_2L})} &= \frac{l_2(l_2+1) + L(L+1) - l_1(l_1+1)}{2L(L+1)} \\ &= 1, \text{ when } l_1 = 0 \text{ and } L = l_2. \end{split}$$

so that the expression for A simplifies to

$$A = a_2 \frac{s_2(s_2+1) + S(S+1) - s_1(s_1+1)}{2S(S+1)}$$
 (18 3)

Now when an electron is added to a term with spin vector  $s_1$ , two terms will be produced with spin moments  $(s_1 + \frac{1}{2})$  and  $(s_1 - \frac{1}{2})$ , if these have interval quotients  $A_+$  and  $A_-$ ,

$$\begin{split} A_{+} \! = \! a_{2} \frac{\frac{3}{4} + (s_{1} \! + \! \frac{1}{2}) \left(s_{1} \! + \! \frac{3}{2}\right) \! - \! s_{1} \left(s_{1} \! + \! 1\right)}{2 \left(s_{1} \! + \! \frac{1}{2}\right) \left(s_{1} \! + \! \frac{3}{2}\right)} \\ = \! a_{2} \! / \! \left(2s_{1} \! + \! 1\right) \end{split}$$

And similarly it may be shown that

$$A_{-} = \frac{-a_2}{(2s_1 + 1)}$$

Applied to the alkaline earth spectra the expression for  $A_+$  leads directly to the results already obtained by the sum rule, but applied to the  ${\rm d}^5({}^6{\rm S})\,n{\rm p}$  configuration of Cri and Moi, the formulae lead to results which are new, thus the 7P term should be erect and the 5P term inverted, while both should have the same interval quotient. In Cri the two terms obey the interval rule well, and the 5P term is inverted, but the interval quotients



where

instead of being equal bear a ratio of 9  $\,^{1}$  (Fig. 18 27) In Mo I the terms do not obey the interval rule and both are erect, while if the theory is applied to the  $p^3$  ( $^{4}$ S)  $^{n}$ p configuration of column VI the results are even more unsatisfactory

Agreement, however, is only to be expected if the p<sup>3</sup> and d<sup>5</sup> groups are so firmly bound in an S state that the addition of the

Terms		Cı	r I	Мог		
Terms		Δν	A	Δν	A	
3d <sup>5</sup> ( <sup>6</sup> S) 4p for Cr 1 and	710		27 1 28 1	257 449	86 112	
4d <sup>5</sup> ( <sup>6</sup> S) 5p for Mo 1	<sup>5</sup> P <sub>1</sub> <sup>5</sup> P <sub>2</sub> <sup>5</sup> P <sub>3</sub>	-57 -88	-29 -29	121 87	61 29	

Fig 18 27 Intervals of the d<sup>5</sup> (<sup>6</sup>S) p configuration in Cr I and Mo I

p electron does not disturb them, and if the coupling of the ion and electron is Russell-Saunders. That experiment does not here support theory shows only that these assumptions are invalid, for a very valuable application of the same theory has been made to the displaced terms of beryllium, magnesium and isoelectronic spectra. The 3s 3p 3P° and 3p 2 P° of the magnesium-like spectra have many of them identical intervals as Fig. 18 28 shows. Now according to the above theory the intervals should be determined by

$$\Gamma = ALS \cos (\mathbf{LS}),$$

$$A = a_1 \frac{l_1}{L} \cos (\mathbf{l_1 L}) \frac{s_1}{S} \cos (\mathbf{s_1 S})$$

$$+ a_2 \frac{l_2}{L} \cos (\mathbf{l_2 L}) \frac{s_2}{S} \cos (\mathbf{s_2 S}) \qquad (18.4)$$

For the 3s 3p configuration the first term of this equation is zero, and there remains simply  $A=\frac{1}{2}a_2$  For the 3p² configuration, on the other hand, the two terms of this equation are equal, and since  $L=S=l_1=l_2=1$  and  $s_1=s_2=\frac{1}{2}$ , there results again  $A=\frac{1}{2}a_2$  Thus the interval quotients are equal, and since both are <sup>3</sup>P terms their displacements and intervals are also equal

Bechert\* has advanced even further than this and has been able to apply a theory of Goudsmit's† to account for the discrepancies from the 2-1 interval ratio, but the theory involves the use of the quantum mechanics and is beyond the scope of this book

		3s 3p <sup>s</sup> P°		3p <sup>2</sup> <sup>3</sup> P			
	Δ <sup>8</sup> P° <sub>1 2</sub>	Δ3P° <sub>0 1</sub>	$\Delta^3 P_1^0 / \Delta^3 P_0^0$	$\Delta^3 P_{1}$	Δ <sup>8</sup> P <sub>0 1</sub>	$\Delta^3 P_{1/2}/\Delta^3 P_{0/1}$	
Mg 1 Al II Si III P IV S V Cl VI	40 6 122 6 261 3 469 1 767 1 1183 7	20 1 64 1 130 7 227 1 360 4 521 3	2 02 1 91 2 00 2 07 2 13 2 27	40 6 122 6 261 3 469 1 767 1 1183 7	20 5 59 7 130 1 234 7 412 4 668 0	1 98 2 05 2 01 2 00 1 86 1 77	

Fig 18 28 sp 3P° and p2 3P intervals in spectra isoelectronic with Mg I

## 9. Abnormal Intensities

Kronig has shown that the intensity tables given in the previous chapter may be applied to configurations in which the coupling is (ij), if S is replaced by  $j_1$  and L by  $j_2$ , where  $j_1$  is taken to be the quantum number which does not change in the transition  $\ddagger$ 

Abnormal intensities due to (jj) coupling must be distinguished from those due to the overlapping of multiplets and configurations, to obtain clear evidence of the validity of this formula, one would wish to measure the intensities of lines arising in a configuration well separated from all others and exhibiting the intervals characteristic of (jj) coupling

## 10 Perturbed terms

There is one factor producing abnormal series, interval ratios, g factors and intensities, which has only recently received the attention it deserves. It is known as perturbation, and is best introduced by a study of a perturbed series.

Of perturbed series, the diffuse series of calcium affords a clear

- \* Bechert, ZP, 1931, 69 735
- † Goudsmit, PR, 1930, 35 1325
- † White and Eliason, PR, 1933, 44 753 Bartlett, PR, 1929, 34 1247, derived formulae for (11) coupling

example The first four members of the <sup>3</sup>D term sequence contract in the usual way, but the next three expand anomalously, the expansion reaches a maximum at the seventh term, the succeeding triplets contracting again as they approach the series limit. This may be shown in two ways, by plotting the displacement of

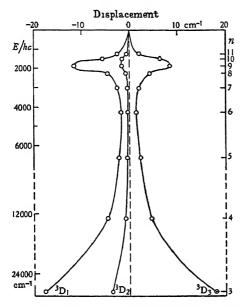


Fig 18 29 The 4s nd <sup>3</sup>D term series of calcium showing perturbation The abscissae are the displacements from the centroid, which is shown dotted

each term from the centroid against the energy (Fig 18 29) and by plotting the effective quantum number against the energy (Fig 18 30)

Similar abnormalities have been noticed in the <sup>3</sup>F series of Al II\* and the <sup>2</sup>P series of Cu I,† and their cause has been elucidated by Russell and Shenstone ‡ They show that these anomalous series only occur when a term of another series intrudes, thus between the sixth and seventh terms of the 4s nd <sup>3</sup>D sequence of

<sup>\*</sup> Sawyer and Paschen, AP, 1927, 84 1

<sup>†</sup> Shenstone, PR, 1929, 34 1623

<sup>‡</sup> Russell and Shenstone, PR, 1932, 39 415 White, Introduction to atomic spectra, 1934, gives a clear and full account of this work.

calcium there hes the  $3d\ 5s\ ^3D$  term, a term be it noted with the same values of L, S and J, but with an interval much greater than that to be expected at this height in the 4s nd series (Fig  $18\ 32$ ) When this intruding term is excluded from the sequence, all succeeding values of the quantum defect are reduced by one, and the graph of the defect against the energy comes to resemble an anomalous dispersion curve (Fig  $18\ 31$ ) Moreover, if a formula

#### Quantum defect

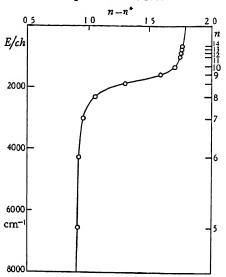


Fig 18 30 The quantum defect  $(n-n^*)$  for the <sup>3</sup>D term sequence of Ca I with the intruding term included

is developed on anomalous dispersion lines,\* very good agreement with experiment can be obtained

Clearly all spectroscopic terms do not perturb one another, analysis alone does not reveal what conditions are essential, but the quantum mechanics provides an answer to this important question. If two levels have the same characteristic quantum numbers and he close together, the eigenfunction of each level contains some components of the eigenfunction of the other, so that both levels belong in part to both configurations. Stated in other words this means that when two states perturb one another,

<sup>\*</sup> Langer, PR, 1930, 35 649a

there is a certain probability that the atom will jump back and forth between the two without energy being radiated. The assignment of a given level to a definite electron coupling is therefore indefinite, it becomes more definite the further the levels are apart. More precisely two levels perturb one another when both have the same J and both are odd or both even, the two terms

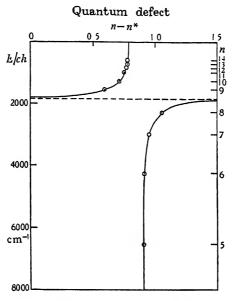


Fig 18 31 The quantum defect  $(n-n^*)$  for the <sup>3</sup>D term sequence of Ca I with the intruding term removed. Note how similar this graph is to that characteristic of anomalous dispersion

need not belong to the same configuration, or be derived from the same state of the ion, but experiment shows that the perturbation is greater when the two terms have the same values of L and S if the coupling is (LS) or the same values of  $J_1$  and  $J_2$  if the coupling is (I)

Since the assignment of electron coupling is indefinite, each perturbed level is likely to have some of the properties of the other, and in fact much evidence has accumulated to show that the perturbing levels share their interval factors, their magnetic splitting factors and their intensities

The quantum mechanics shows that in terms of energy perturbation manifests itself essentially as a repulsion, but it is not difficult to show that repulsion leads logically to a sharing of intervals. Consider for example a narrow triplet lying close below a wide one, if one of these is odd and the other even, they will not perturb one another, and if the coupling is (**LS**) they will appear as shown on the left of Fig. 18 33. If however both terms are

Observed term value cm -1	Configura tion	n	n*	$n-n^*$	Calculated term value cm -1	T (obs )– $T$ (calc )
28969 1 11556 4 6561 4 4255 5 3002 4 2268 3 1848 9 1551 3 1273 1 1045 6 869 8 734 0 628 0	4s 3d 4s 4d 4s 5d 4s 6d 4s 7d 4s 8d 3s 5d 4s 9d 4s 10d 4s 11d 4s 12d 4s 13d 4s 14d	3 4 5 6 7 8 9 10 11 12 13 14	1 946 3 081 4 090 5 078 6 045 6 955 7 702 8 410 9 284 10 244 11 232 12 227 13 219	1 054 0 919 0 910 0 922 0 955 1 045 0 590 0 716 0 756 0 768 0 773 0 781	26465 11556 6562 4252 3002 2287 Foreign term 1551 1276 1048 873 737 630	2504 0 - 1 + 3 0 - 19 0 - 19 0 - 3 - 2 - 3 - 3 - 2

Fig 18 32 Series calculations of the anomalous 4s nd  $^8D_1$  series of calcium. The calculated term values are obtained from a formula designed on the lines of those used to explain anomalous dispersion. (After Russell and Shenstone, PR, 1932, 39 415)

even, the levels with the same J will repel one another, and as the repulsion is greater the nearer the levels are to one another, the  $^3P_0$  terms which are nearest undergo the greatest displacement, thus the narrow triplet is widened and the wide triplet is narrowed, this is shown on the right side of the figure. Moreover, if the narrow term lies above the wide, the same sharing of the intervals results

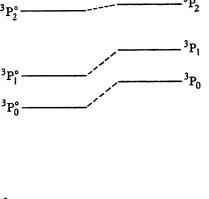
Of the sharing of magnetic splitting factors much evidence has accumulated Thus is Zri the  $^3P_2$  and  $^1D_2$  terms of the  $4d^2$   $5s^2$  configuration should have g values of 1 5 and 1 0, whereas in fact both have the same g value, 1 25, these terms are separated by 915 cm  $^{-1}*$  Further examples from Zri are shown in Fig. 18 34,

<sup>\*</sup> Kless, C C and Kless, H K, BSJ, 1931, 6 660

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while the phenomenon has been observed in Tii, Cui, Niii\* and Laii In all these spectra the two perturbing terms belong to the same configuration, but the deviating g sums of Kii, Rbii and Pniii make it probable that this is not an essential condition. In Pbiii† the g value of the 6s 6p  $^3$ P<sub>2</sub> term, which



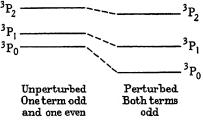


Fig 18 33 Changes produced by perturbation in wide and narrow triplets when these he close to one another

should be 1 50 whatever the coupling, is in fact 1 35 This can be most reasonably explained if the term is perturbed, but what unidentified configuration is likely to lie near enough is not clear

Short of complete sharing, the g factors may be more or less distorted A method of calculating the precise change in g caused by neighbouring states was first developed by Houston‡ for the

<sup>\*</sup> Shenstone, PR, 1927, 30 264

<sup>†</sup> Green and Loring, PR, 1932, 41 389a

<sup>‡</sup> Houston, PR, 1929, 33 297

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ps configuration, Goudsmit\* later extended the method to the ds, and Laporte and Inglis† to the p<sup>5</sup> s and d<sup>9</sup> s configurations. The only empirical constant which these formulae contain is one easily determined from the energies of the terms

Though perturbed terms share their magnetic splitting factors, one must not too readily assume the converse, that when two terms share their splitting factors they are perturbing one another The  $^3P_1$  and  $^1P_1$  terms of the  $4p^5(^2P)$  5s configuration

Configuration	Term	E/hc	g theory	g observed
4d <sup>2</sup> 5s <sup>2</sup>	<sup>3</sup> P <sub>2</sub> <sup>1</sup> D <sub>2</sub>	4,186 5,101	1 500 1 000	1 25
4d³ 5s	³F₄ ³G₄	12,342 12,761	1 250 1 050	1 15
4d² 5s 5p	¹G₄ ³F₄	26,931 26,938	1 000 1 250	1 13
4d³ 5p	$^{5}P_{2}$ $^{1}D_{2}$	34,761 34,850	1 833 1 000	1 42
4d3 5p	¹F₃ ³G₃	36,760 36,942	1 000 0 750	0 87

Fig 18 34 Sharing of magnetic splitting factors in Zr I

of KrI both have g factors of 1 25, but they are separated by  $4930 \,\mathrm{cm}^{-1}$ , and in fact their g factors have been explained as due to a particular coupling intermediate between (LS) and (j]) (Fig. 18 25)

The sharing of intensities is also well established. In Zri singlet terms have been found combining with quintets, but only when the singlet has a quintet neighbour or the quintet a singlet and the two perturbing terms have the same J; Moreover, in barium Langstroth  $\S$  has identified the terms which perturb the first three multiplets of the diffuse and fundamental series, and has shown that the experimental intensity sums are those required for (LS) coupling. In this comparison an uncalculable parameter appears connecting the intensities of two multiplets

<sup>\*</sup> Goudsmit, PR, 1930, 35 1325

<sup>†</sup> Laporte and Inglis, PR, 1930, 35 1337 Pogány, ZP, 1933, 86 729, confirms the predicted values in Kr i

<sup>‡</sup> Details on p 106

<sup>§</sup> Langstroth, PRS, 1933, 142 286

arising in different configurations, but this may be determined experimentally provided some lines occur in each multiplet which are only slightly perturbed. A study of perturbed terms leads naturally to the identification of lines previously regarded as anomalous, for a weak multiplet may have one or more of its lines intensified by perturbation until they become strong enough to stand out in the spectrum. Several fragments of multiplets, whose other components are so weak that they escape observation, have in fact been found.

In barium no attempt was made to calculate the precise intensities of individual lines, for this is only possible when the parent configurations of all perturbing terms are known, and as yet the analysis of Ba ii is insufficiently advanced. Indeed individual perturbed intensities seem to have been calculated and compared with experiment only once, by Kast\* working on Sr i He found satisfactory agreement, but the perturbation in the two terms considered was not as large as one could wish considering the magnitude of the experimental error

#### BIBLIOGRAPHY

Pauling and Goudsmit, The structure of line spectra, 1930

\* Kast, ZP, 1932, 79 731

#### CHAPTER XIX

### SERIES LIMIT

### 1 J values

Evidence has already been adduced to show that in the spectra of N, A II and Ne where the limit is a multiplet, some series converge to one component and some to another. To recall the point at issue consider the displaced terms of calcium, five terms of the

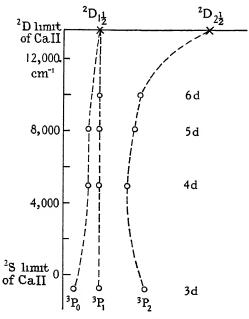


Fig 19 1 Splitting of the 3d  $\,\it nd$   $^3P$  terms of Ca I showing that all three do not tend to the same limit

d np  $^3P$  series are known and the separations are plotted in Fig 19 l, showing quite clearly that  $^3P_2$  converges to an upper limit, while  $^3P_1$  and  $^3P_0$  converge to a lower, these limits are naturally interpreted as the  $^2D_{24}$  and  $^2D_{14}$  terms of Ca  $_{11}$ 

All these terms have been named because they approximate to the Russell-Saunders ideal, but there are other terms such as the  $(^2P)$  p and  $(^2P)$  d terms of neon which cannot be named though their series have been worked out, and the limits they approach Naturally then the question arises cannot theory predict which terms will approach each limit? This was the problem which Hund set himself, and his solution will be considered in due course, but in that J is more easily determined than the orbital and spin vectors, it must take precedence

Empirically the J values of unknown terms are always more easily determined than the multiplet structure. And theoretically the J values retain their significance even when the coupling is most irregular and L and S have no meaning. In particular, if both the series limit and the orbital vector of the series electron

J Limit	O	1	l	ž	2	3
${}^{2}\mathbf{P}_{\underline{1}}$	p <sub>1</sub>	$\mathbf{p_2}$	$P_5$	<b>P</b> <sub>4</sub>		
${}^{2}P_{1}$	$\mathbf{p_3}$	p,	P <sub>10</sub>	P <sub>6</sub>	P <sub>8</sub>	P9

Fig 19 2 Paschen's p series in neon and the limits to which they tend

are known, then the J values of the terms approaching that limit are readily determined

Ask, for example, which of the p terms of neon approach the lower  ${}^2P_{1\frac{1}{4}}$  limit of Ne II When the chief quantum number of the series electron is sufficiently large the coupling is roughly (jj) and the problem is simply to find what J values can result from a term having  $j_1 = 1\frac{1}{2}$  and a p electron having  $j_2 = \frac{1}{2}$  or  $1\frac{1}{2}$  When  $j_2 = \frac{1}{2}$  the permitted values of J are 1 and 2, while when  $j_2 = 1\frac{1}{2}$ , J will assume the values 0, 1, 2 or 3 Thus the J values of the terms approaching the lower limit should be 0, 1, 1, 2, 2, 3, while those approaching the upper  ${}^2P_{\frac{1}{4}}$  limit will have J values of 0, 1, 1, 2, and this is in fact the division actually observed

And these facts may be simply summarised in a cell diagram, constructed to show the limits from top to bottom and the J values from left to right

This diagram shows that the structure of certain terms is determined uniquely, thus the empirical p<sub>1</sub> term is the only term

arising by the addition of a p electron to a  ${}^{2}P_{\frac{1}{2}}$  limit and having J=0, and it is thus the only term whose structure can be expressed symbolically as  $({}^{2}P_{\frac{1}{2}}$  p)<sub>0</sub> But unfortunately no method is known of distinguishing two terms which have the same limit and the same value of J, though theory shows clearly that the one arises when the p electron has  $j_{2}=\frac{1}{2}$  and the other when  $j_{2}=1\frac{1}{2}$  p<sub>6</sub> and p<sub>8</sub> must both be written  $({}^{2}P_{1\frac{1}{2}}$  p)<sub>2</sub>, for they cannot be distinguished as  $({}^{2}P_{1\frac{1}{2}}$  p<sub>4</sub>)<sub>2</sub> and  $({}^{2}P_{1\frac{1}{2}}$  p<sub>1+</sub>)<sub>2</sub>

The same method when applied to the (2P)d terms of neon or

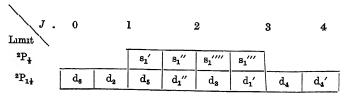


Fig 193 Limits of the (2P)nd terms of neon and argon

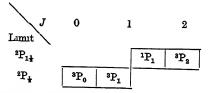


Fig 194 Limits of the (2P)ns terms of silicon

argon gives Fig 19 3, while applied to the 3p ns configuration of silicon it gives Fig 19 4

The J values of all known series fit in with these requirements, and the agreement is equally satisfactory whether the low terms are roughly Russell-Saunders as they are in nitrogen and the s terms of neon, or whether a large gap separates the terms tending to the upper and lower limits as in the p and d terms of argon

### 2. Hund's theories

The real problem, however, is not to account for the empirical terms by assuming a (jj) coupling, but to name them with the Russell-Saunders symbols

Towards the solution of this problem Hund has made two

pronouncements In the first\* he fixed the limit towards which a term series must converge, and fixed it given only the ion, the series electron and the symbol of the term, but though this theory is successful enough when both terms and limit are erect it fails badly when the limit is inverted as it is in neon † Thus the  $(^2P)n$ s configuration yields two terms having J=1,  $^3P_1$  and  $^1P_1$ , Hund's early theory states that of these  $^3P_1$  will always approach the  $^2P_{\frac{1}{2}}$  limit, and  $^1P_1$  the  $^2P_{\frac{1}{2}}$  limit, but though this prediction is correct in silicon it is incorrect in neon

Hund's revised prediction; is less precise and therefore less useful, it has usually been taken to mean that terms arising from

Term	n=5	$n=5$ $\Delta \nu$ $n=6$		$\Delta \nu$	Limit
<sup>3</sup> D <sub>3</sub> <sup>3</sup> D <sub>2</sub> <sup>3</sup> D <sub>1</sub> <sup>1</sup> D <sub>2</sub>	19533 2 18802 5 18398 6 16122 5	730 7 403 9 2276 1	108313 0 107817 0 107309 3 107631 5	496 0 507 7 - 322 2	195,195 194,824 194,268 195,978

Fig 19 5 Values of the limits to which the four terms of the 4d  $\,$  ns configuration of Zr III tend

the same configuration and having the same J do not cross as they approach the limit, and in this form the theory is certainly in closer agreement with experiment. Thus in silicon the  ${}^3P_1$  term lies below the  ${}^4P_1$  term and accordingly  ${}^3P_1$  will approach the lower limit, namely  ${}^2P_{\frac{1}{2}}$  of Si II, in neon  ${}^3P_1$ , being s<sub>4</sub> in Paschen's notation, again lies below  ${}^4P_1$  or s<sub>2</sub>, so that again  ${}^3P_1$  approaches the lower limit, but this time the limit is inverted and the lower component is  ${}^2P_{1\frac{1}{2}}$ 

These seem to show that <sup>1</sup>D<sub>2</sub>, though below <sup>3</sup>D<sub>2</sub> in the low

<sup>\*</sup> Hund, Linienspektren, 1927, 184 f

<sup>†</sup> Shenstone, N, 1928, 121 619, 122 727

<sup>†</sup> Hund, ZP, 1929, 52 601

<sup>§</sup> Kiess, C C and Lang, BSJ, 1930, 5 321

terms, yet tends to a higher limit, for the separation of the limits of  $^{1}D_{2}$  and  $^{3}D_{2}$  works out as 1154 cm  $^{-1}$ , which compares well with the interval of the  $^{2}D$  term of Zriv, which is 1250 cm  $^{-1}$  That the  $^{1}D_{2}$  sequence should converge to the upper limit is in accord with Hund's early theory, but contrary to the usual interpretation of his later pronouncement

A letter, however, written by Hund to Mack\* shows that his statement has been interpreted too rigidly, for he specifically limited his prediction to terms which showed no symmetry property, and the letter states that any experimental evidence of crossing is to be taken as evidence of a symmetry property of the system Accordingly the crossing of levels having the same J can never be in disagreement with Hund's conjecture, and the latter is in fact only a convention for naming levels where experiment does not distinguish between them Mack pointed this out

But even in this very limited form one may question whether the convention is useful, for if the Russell-Saunders notation is not to have any of its usual implications, it is surely better abandoned, and one which has no implications at all adopted in its place. And in fact Russell has advised that terms whose configuration and coupling are still undetermined shall be specified simply by numbers.

Present theory thus appears unable to make any general pronouncements, but it is not therefore valueless, experiment shows that in a large number of spectra, terms having the same J do not cross, and accordingly the consequences of this hypothesis are worthy of study, if only as an ideal with which the empirical may be compared. This ideal is the more useful in that if all terms obeyed Hund's energy rules only two types of convergence would be found, one when the limit is erect, the other when the limit is inverted. The erect type of convergence is identical with that dictated by Hund's first theory

Take as an example the convergence of the terms of a (3P) nd configuration when the limit is first erect and then inverted (Figs. 196, 197) When the limit is inverted all components of a multiplet tend to approach the same limit, but when the limit is

<sup>\*</sup> Mack, PR, 1929, 34 34

erect they tend to approach different limits, and in this the (<sup>3</sup>P)d terms are only one example of a general trend

A word should be added on the filling up of these figures, the number of cells in each row and their J values have been con-

Limit	<del>1</del>		11/2		$2\frac{1}{2}$		3 <del>1</del>		41/2	
$^3P_2$	<sup>2</sup> P <sub>i</sub>	<sup>4</sup> P <sub>‡</sub>	<sup>2</sup> P <sub>1</sub>	<sup>2</sup> D <sub>1<sup>1</sup>/<sub>2</sub></sub>	<sup>2</sup> D <sub>2</sub>	<sup>2</sup> F <sub>2</sub>	²F₃.	4D <sub>81</sub>	4F4+	]
$^3P_1$		<sup>4</sup> D <sub>1</sub>	4P <sub>1+</sub>	4D <sub>1</sub>	4P21	<sup>4</sup> D <sub>2</sub>	4F <sub>81</sub>			'
$^{8}P_{0}$				4F <sub>1+</sub>	4F <sub>2+</sub>			•		

Fig 19 6 Convergence of ( $^3$ P) $^{nd}$  terms when the limit is erect, the low terms are assumed to obey Hund's energy rules and terms with the same J do not cross as they tend to the limit

J Limit	;	2	1	<u> </u>	2	3	ŧ	3 <u>1</u>	4 <u>1</u>
$^{8}P_{0}$				<sup>2</sup> D <sub>1</sub>	<sup>2</sup> D <sub>2</sub>				
$^{8}P_{1}$		$^{2}P_{\frac{1}{4}}$	<sup>2</sup> P <sub>1</sub>	4P <sub>11</sub>	<sup>2</sup> F <sub>2</sub> 1	4P <sub>21</sub>	2F <sub>81</sub>		
$^3P_2$	4P.	<sup>4</sup> D <sub>1</sub>	4D <sub>1</sub>	4F <sub>1</sub>	<sup>4</sup> D <sub>2</sub>	4F <sub>2±</sub>	4D <sub>3+</sub>	4F34	4F4+

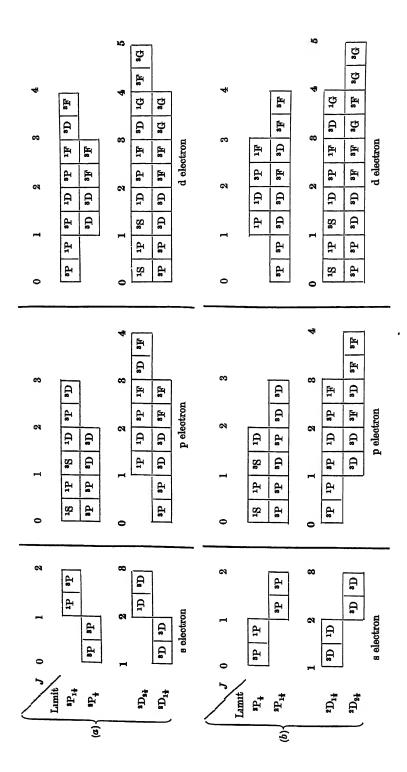
Fig 19 7 Convergence of (<sup>3</sup>P)nd terms when the limit is inverted, the assumptions being the same as in the previous figure

sidered earlier, the terms arising from ( $^3P$ )d are  $^4F$ ,  $^4P$ ,  $^2F$ ,  $^2D$ ,  $^2P$  in that order from below upwards, accordingly, starting with  $^4F$ , insert each of the four components in the lowest cell which its J value permits, having finished  $^4F$  continue to  $^4D$  and so through  $^4P$  and  $^2(FDP)$  until all seventeen cells are full

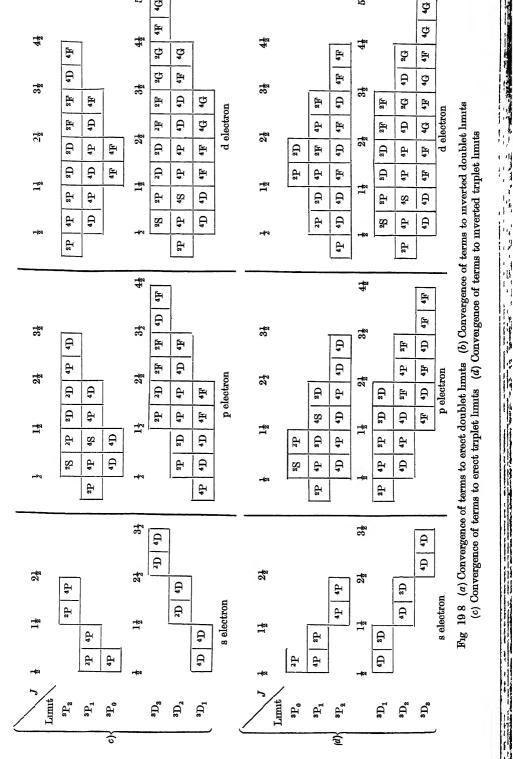
A number of these convergence types are given in Fig 198

#### BIBLIOGRAPHY

Chapter XIX of White's Introduction to atomic spectra may be usefully read, though its subject "Series Perturbations" is parallel to rather than a development of series limits



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#### CHAPTER XX

## HYPERFINE STRUCTURE

# 1 Empirical

When the interferometers of Michelson, Fabry-Perot and Lummer-Gehrcke are applied to spectral lines, which appear single in a prism spectroscope, many are found to exhibit a complex structure with component intervals of 0 1 to 10 cm<sup>-1</sup> This much has been known since these high resolving instruments were first invented, the structure being commonly referred to as hyperfine

The small intervals alone might suggest that the hyperfine levels can hardly be attributed to the same electron spin which produces the normal multiplet, and this suspicion gains support from the difficulty in fitting them into Hund's term scheme Caesium, for example, must surely have a doublet structure, yet if a spectroscope of high resolving power is applied to certain lines, which should be simple, they appear as doublets with an interval of about 0.3 cm<sup>-1</sup> Time and again Hund's scheme has predicted how many terms an element should possess, and when the analysis has been completed, these and only these have been found. Yet when an element exhibits hyperfine structure, the extra levels cannot be fitted in

Clearly then some new explanation must be sought In 1924 Pauli\* drew attention to the nucleus as a possible influence, but it was not until the following year that Schuler† brought forward the first experimental evidence in his work on the hyperfine structure of the 5485 A line of Liu This line arises from the  $2p^3P_{0,1,2}\rightarrow 2s^3S_1$  transition, and should therefore be similar to the 7065 A. line of He i, for the latter arises from  $3s^3S\rightarrow 2p^3P$ , but whereas the helium line is a triplet, Schuler showed that the 5485 A line of lithium has at least 14 components

As both the helium atom and lithium ion have two orbital electrons, they differ only in their nuclei, and so to the nuclei

<sup>\*</sup> Pauli, Nw, 1924, 12 741

<sup>†</sup> Schüler, AP, 1925, 76 292, ZP, 1927, 42 487

must be attributed the hyperfine structure Further, lithium has only two isotopes, Li<sup>6</sup> and Li<sup>7</sup>, so that even if these did produce separate triplets they would account for only 6 out of the 14 components, the nuclear property responsible must therefore be something other than a simple mass effect

#### 2 Influence of nuclear mass

In both hydrogen and ionised helium, the series are governed by the relation

 $v = Z^2 R \left\{ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right\},$ 

but the Rydberg constant, R, has a slightly different value in the two spectra, 109,678 in hydrogen and 109,722 in helium. This small difference Bohr explained as due to the different mass of the two nuclei, for if the mass is infinite

$$R = \frac{2\pi^2 e^4 m_e}{ch^3} \tag{2.9}$$

But when the mass of the nucleus is finite, the electron and nucleus both revolve about the common centre of gravity, to correct for this one substitutes for the mass of the electron,  $m_e$ , the quantity

$$\frac{M}{M+m_e}m_e$$

This theory clearly shows that the spectral lines of the heavy isotope of hydrogen will be displaced, each line of the Balmer's series having a weak component on its short wave-length side, moreover, as the mass of the isotope is 2, the intervals of the first four lines,  $H_{\alpha}$  to  $H_{\delta}$ , should be 4 16, 5 61, 6 29 and 6 65 cm <sup>-1\*</sup> Photographs show that in fact a weak satellite does occur in this position, and that the satellite is stronger when the concentration of  $H^2$  is increased

When there is more than one electron, the theory is much more complicated, but Hughes and Eckart† have provided a solution for systems of two and three electrons. The separations of the

<sup>\*</sup> Urey, Brickwedde and Murphy, PR, 1932, 40 1

<sup>†</sup> Hughes and Eckart, PR, 1930, 36 694

lithium isotopes, Li<sup>6</sup> and Li<sup>7</sup>, is in reasonable agreement with theory \* The measured intervals are

Lin 
$$2p^{3}P \rightarrow 2s^{3}S$$
 5485 A 1 06 cm<sup>-1</sup>  
Lii  $2p^{2}P \rightarrow 2s^{2}S$  6708 A 0 345 cm<sup>-1</sup>  
 $3p^{2}P \rightarrow 2s^{2}S$  3233 A 0 56 cm<sup>-1</sup>

For atoms with more than three electrons, no theory has been evolved, and in fact a displacement due to mass alone seems to have been demonstrated only in neon. Each arc line of this element is accompanied by a faint companion of shorter wavelength. If the single electron theory was not invalid, it would suggest that the intervals should be given by  $\frac{\delta \nu}{\nu} = 247 \cdot 10^{-8}$ , while experiment shows that this ratio assumes the values 437  $\cdot 10^{-8}$  in the lines  $2p_m \rightarrow 1s_2$ , and 368  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ , and  $\cdot 10^{-8}$  in the lines  $\cdot 2p_m \rightarrow 1s_3$ .

### 3. The extended vector model

The first theory put forward to explain hyperfine structure; assigned to the nucleus an angular momentum  $\mathbf{I}$ , and made this combine with the electronic moment  $\mathbf{J}$  to form a resultant atomic moment commonly written  $\mathbf{F}$  Then  $\mathbf{F}$  must be quantised as well as  $\mathbf{I}$ , and  $\mathbf{J} + \mathbf{I} = \mathbf{F}$ 

Previous experience with the similar linking of  $\mathbf{L}$  and  $\mathbf{S}$  to form  $\mathbf{J}$  suggests that possibly F will change only by  $\pm 1$  or 0, and that the transition from F=0 to F=0 will be forbidden, further, one may hope that the multiplet intervals will satisfy the Landé interval rule. This hypothesis was at first only a guess, but evidence drawn both from experiment and from the calculations of the wave mechanics shows that the guess is fortunate

Evidence will be adduced first in support of the interval and selection rules, thus certain lines of the bismuth spectrum were

<sup>\*</sup> Hughes, PR, 1931, 38 857 Cf Granath, PR, 1932, 42 44

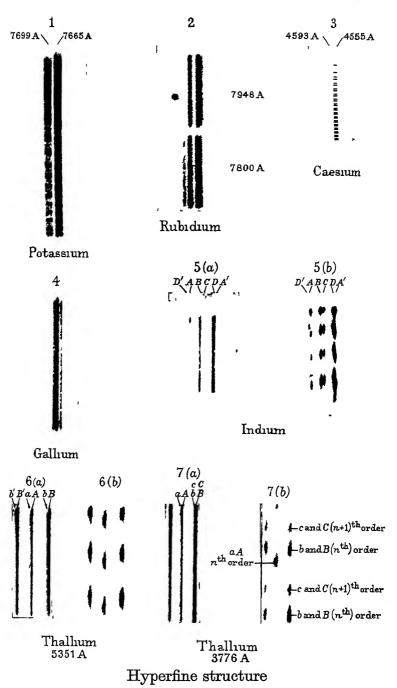
<sup>†</sup> Hansen, N, 1927, 119 237, Nagaoka and Mishima, Imp Acad Tokyo, Proc. 1929, 5 200, 1930, 6 143, Thomas and Evans, E. J., PM, 1930, 10 128

<sup>‡</sup> Pauli, Nw, 1924, 12 721

#### PLATE VII HYPERFINE STRUCTURE

- 1 Potassium resonance lines, 7699 and 7665A,  $^2\mathrm{P} \rightarrow ^2\mathrm{S}$  Light from a potassium lamp was examined with a Fabry-Perot étalon, after passing through a beam of potassium travelling at right angles to the line of sight, the absorption pattern possesses a fine doublet structure, the Doppler width in absorption being much less than in emission
- 2 Rubidium resonance lines, 7800 and 7948 A,  $^{2}P \rightarrow ^{2}S$  Photographed with a reflection échelon, each line consists of four components, the weak outer components are due to Rb<sub>87</sub>, and the strong inner components to Rb<sub>85</sub> As the hfs is the same for both lines, it arises in the common level  $^{2}S$
- 3 Caesium line, 4555 A,  $^2P_{12} \rightarrow ^2S$  The hfs revealed by a Lummer-Gehrcke plate consists of doublets, arising in the  $^2S$  level, the intensity ratio of 1 27 1 shows that  $I=3\frac{1}{2}$  The fringes of 4593 A,  $^2P_{\frac{1}{2}} \rightarrow ^2S$ , appear very faint
- 4 Gallium resonance line, 4033 A,  ${}^2S \rightarrow {}^2P_{\frac{1}{2}}$  A reflecting échelon grating reveals three lines with intensity ratio of 4 9 6 1 5 The  ${}^2S$  and  ${}^2P$  terms have nearly the same interval so that two of the four components overlap, the theoretical patterns are the same for  $I=\frac{1}{2}$  and  $I=1\frac{1}{2}$ , but the intensity ratios are 1 2 1, and 5 6 5 respectively, thus I=1.
- 5 Induum lune,  $4101\,\mathrm{A}$ ,  $^2\mathrm{S} \to ^2\mathrm{P}_{1}$  The photograph on the left is taken with a reflecting échelon grating, while on the right this has been crossed with a Fabry-Perot étalon. Since the four streaks A,B,C,D lie on a diagonal, the pattern consists of these and not of D',A,B,C as the left-hand figure might suggest. The intensity ratio of 2.72 1.82, 1.00 2.74 shows that  $\mathrm{I}=4\frac{1}{2}$
- 6 Thallrum line,  $5351 \, \mathrm{A}$ ,  $^2\mathrm{S} \to ^2\mathrm{P}_{11}$  The left-hand photograph was taken with a reflecting échelon, in the right hand this has been crossed with a Fabry-Perot étalon. The line consists of two close doublets, for the components b' and B' can only be b and B appearing in the next order, since on the right the étalon fringes appear at the same height. The small interval is due to isotope displacement, a and b being due to  $\mathrm{Tl}_{208}$  and A and B to  $\mathrm{Tl}_{206}$ , the larger interval is due to the hfs of the  $^2\mathrm{S}$  term
- 7 Thallrum line,  $3776 \, \text{A}$ ,  $^2\text{S} \rightarrow ^2\text{P}_{\frac{1}{4}}$  The six components are arranged in three close doublets, but the pair B and b in the  $n^{\text{th}}$  order overlap the pair C and c in the  $(n+1)^{\text{th}}$  order, for when the échelon is crossed with a Fabry-Perot étalon, the fringes in these lines are double

All photographs were lent by Dr D A Jackson



early analysed\* and the 4722 A line, arising from the p² sl<sub>½</sub>  $\rightarrow$  p³  $^2D_{1½}$  transition may be quoted as an example. The observed pattern is shown in Fig. 20 1 and analysis of this shows that the lower term,  $^2D_{1½}$ , has intervals of 0 152, 0 198, and 0 255, these best satisfy the interval rule if F is assigned the values 3 to 6, and the vector model allows just these values if I is 4½, moreover, the model predicts always (2J+1) or (2I+1) components, according as I or J is the larger, and in fact the 1½, 81½ and  $2D_{2½}$  terms do

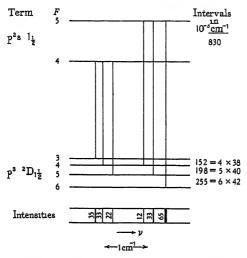


Fig 20 1 Level diagram showing the structure of the 4722 A line of Bii, the intervals given are empirical, the intensities theortical (After Goudsmit and Back, ZP, 1927, 43 321)

split into 2, 4 and 6 levels respectively. Of these terms the two last obey the interval rule even better than the  $^2D_{11}$  term cited above (Fig. 20.2)

The analysis of bismuth by the interval rule has been followed up by work on Mn, Pr, La and Cs That bismuth was the first element successfully analysed was not due only to chance, but to the existence of only one isotope. For where several isotopes occur, each may have a different nuclear spin, and each spin then produces its own hyperfine pattern.

<sup>\*</sup> Goudsmit and Back, ZP, 1927, 43 321 Zeeman, Back and Goudsmit, ZP, 1930 66 1

Thus cadmium possesses six isotopes and these manifest themselves in the structure of the triplet 4678, 4800, 5086 A, which arises from the transition  $2\,^3\mathrm{S}_1 \to 2\,^3\mathrm{P}_{0,1,2}$  \* The three hyperfine patterns have only one interval in common, namely 0 396 cm  $^{-1}$ , and the  $2\,^3\mathrm{S}_1$  term must split therefore to two and only two components, but as the number of components is always (2J+1) or (2I+1), I must be  $\frac{1}{2}$ , and since this value must hold for all three P levels the term scheme and line pattern should be those shown in Fig 20 3 All the lines required by this scheme are in fact observed and have their theoretical intensities, but in

Term	F	2	3	4	5	6	7
6p³ 2D1+	Interval	=	-0 152 -0 038	-0 198 -0 040	-0 255 -0 042	_	
6p <sup>3 2</sup> D <sub>2</sub>	$_{A}^{\rm Interval}$	0 256 0 085	0 312 0 078	0 385 0 077	0 491 0 082	0 563 0 080	
6p <sup>2</sup> 7s 8 <sub>11</sub>	Interval A	=	0 379 0 095	0 473 0 095	0 563 0 094	_	

Fig 202 Examples of the interval rule in bismuth

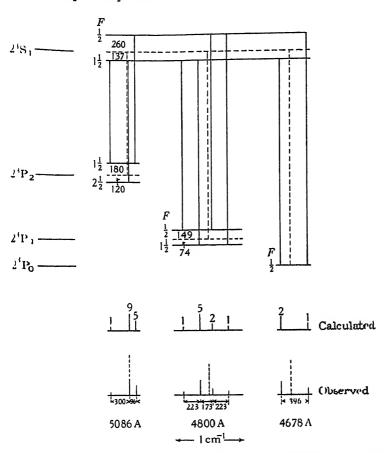
addition each gross line has a strong component shown by the dotted line A at the foot. This strong component has been attributed to isotopes of cadmium having no nuclear moment and hence no hyperfine structure. Of the six isotopes of cadmium which Aston has identified therefore some have a nuclear moment of  $\frac{1}{2}$  and some of zero, and the intensity of A relative to the other components makes it necessary to allocate the value  $\frac{1}{2}$  to the odd isotopes 111 and 113, while all the even isotopes 110, 112, 114 and 116 have I=0

Cadmium is peculiar in that the hyperfine levels are inverted, the levels with the largest values of F lying lowest, this arrangement is rather rare among hyperfine structures thus far analysed, though the  $^2\mathrm{D}_{11}$  level of bismuth examined above happens also to be inverted

The results thus far cited may be taken to prove that the hyperfine intervals satisfy the interval rule and that the selection rule is  $\Delta F = \pm 1$  or 0, but no evidence has been adduced to show

<sup>\*</sup> Schuler and Bruck, ZP, 1929, 56 291, 58 735

ther the transition from F=0 to F=0 is specifically forbidden. sider therefore the 3776 A line of Tli, a line which arises from tump  $2^2S_{\frac{1}{2}} \rightarrow 2^2P_{\frac{1}{2}}$ , examined for hyperfine structure this line



ig 20 3 Level diagram showing the structure of three cadmium lines

sals an unsymmetrical triplet (Fig. 20.4)\* As the initial and I terms have the same value of J, this structure can be exned only if I is  $\frac{1}{2}$ , and if the jump from F=0 to F=0 is initially forbidden, any other value of I would give use to

Schuler and Bruck, ZP, 1929, 55 575 Schuler and Keyston, ZP, 1931,

four components, and should two of these coincide then the triplet would be symmetrical

That the same selection and interval rules are valid for both

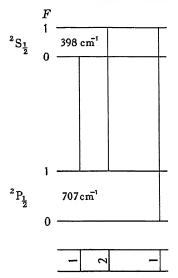


Fig 20 4 Level diagram of the 3776A,  ${}^2S_{\frac{1}{2}} \rightarrow {}^2P_{\frac{1}{2}}$ , line of thallium

Gross structure			Hyperfine structure
Resultant of spin moments Resultant of orbital moments Vector sum of S and L	S L J	I J F	Nuclear spin Electronic moment Vector sum of I and J
Magnetic moment of spin Magnetic moment of orbital vector	g (S) S $g$ (L) L	g (I) I $g$ (J) J	Magnetic moment of nucleus Magnetic moment of electronic vector
Projection on magnetic axis of S of L of J	M <sub>S</sub> M <sub>L</sub> M <sub>J</sub>	M <sub>I</sub> M <sub>J</sub> M <sub>F</sub>	Projection on magnetic axis of I of J of F

Fig 20.5 Comparison of vectors used to explain gross and hyperfine structures

gross and hyperfine structures suggests a far-reaching analogy, which is summarised and extended in Fig. 20.5, so as to suggest rules for the Zeeman and Paschen-Back splitting. The angular momenta are given in units  $h/2\pi$  and the magnetic moments in Bohr magnetons

 $\frac{h}{2\pi} \frac{e}{2m.c}$ 

That the interval rule is valid shows that if the interaction energy of I and J is E, then

$$E/ch = AIJ\cos(\mathbf{IJ})$$
  
=  $\frac{1}{2}A \{F(F+1) - J(J+1) - I(I+1)\}$  (20 1)

The separation of the two levels F and (F-1) is then

$$\frac{1}{2}A \{F(F+1)-(F-1)F\}=AF$$

so that successive intervals in a multiplet term are proportional to the greater of the adjacent quantum numbers

Hyperfine multiplets usually obey the interval rule so well that exceptions attract an attention, which similarly deviating gross multiplets never obtain. These irregularities are to-day recognised as arising from at least two distinct causes, perturbation and absence of spherical symmetry in the electric field of the nucleus. As perturbation, however, produces also abnormal isotope displacements, and isotope displacements have not yet been considered, these inregularities are better postponed to a later section.

## 4 Zeeman and Paschen-Back effects

In work on the splitting of lines in the magnetic field, theory has long travelled ahead of experiment, so consider what splitting the vector model predicts \*

In a weak field **J** and **I** combine to form **F**, and the projection of **F** on the magnetic axis **H** is quantised. According to the theory of the Zeeman effect, the increment of energy will be  $\Delta E$ , where

$$\Delta E/ch = M_{F}g(F)o_{m} \qquad (20 2)$$

 $o_m$  is here an abbreviation for the Lorentz unit

$$\frac{eH}{4\pi m_e c^2}$$
 = 4 698 10<sup>-5</sup> $H$  cm <sup>-1</sup>,

H being measured in gauss, while  $M_F$  is restricted by the condition  $F\geqslant M_F\geqslant -F$ 

This energy equation gives the displacement of a level from the position it occupies when the magnetic field is zero, to obtain the

<sup>\*</sup> Goudsmit and Bacher, ZP, 1930, 66 13

displacement from the centroid a second term must be added so that the energy becomes

$$E/ch = \frac{1}{2}A \left\{ F\left(F+1\right) - I\left(I+1\right) - J\left(J+1\right) \right\} + M_F g\left(F\right) o_m \quad . \quad (20\ 3)$$

A is here the hyperfine interval quotient

In an earlier chapter g(J) was derived on the assumption that if two vectors X and Y combine to form a third vector Z, then

$$g\left(Z\right)\!=\!g\left(X\right)\!\frac{X}{Z}\!\cos\left(\mathbf{X}\mathbf{Z}\right)\!+\!g\left(Y\right)\frac{Y}{Z}\!\cos\left(\mathbf{Y}\mathbf{Z}\right)\!,$$

this expression being itself derived from the wave mechanics Now  $\mathbf{F} = \mathbf{J} + \mathbf{I}$ , so that

$$g(F) = g(J)\frac{J}{F}\cos(\mathbf{JF}) + g(I)\frac{I}{F}\cos(\mathbf{IF}).$$
(20 4)

The magnitude of the hyperfine splitting itself and the theory of its cause both suggest that g(I) will be very small, about 1/2000 say, so that in all fields which can be applied to the atom g(I) will be negligible, and g(F) may be written as

$$g\left(F\right)\!=\!g\left(J\right)\frac{F\left(F+1\right)\!+\!J\left(J+1\right)\!-\!I\left(I+1\right)}{2F\left(F+1\right)}\tag{20 5}$$

This completes the description of the weak field. In a strong field **J** and **I** are no longer linked together, but precess independently round the magnetic axis, so that their projections on the magnetic axis have to be quantised separately. As in the theory of the Paschen-Back effect, so here

$$E/ch = AM_{I}M_{J} + M_{J}g(J)o_{m},$$
 (20 6)

where g(I) has been treated as negligibly small

This simple theory should give good agreement in fields so weak that  $o_m \ll A$ , and in fields so strong that  $o_m \gg A$ , but in intermediate fields resort must be had to the quantum mechanics. Moreover, in all fields the quantum mechanics should give more accurate numerical values

A complex theory such as this is most satisfactorily tested, if applied, first to a transition producing a simple pattern, and afterwards to patterns of growing complexity. Accordingly,

Green and Wulff first examined the 3092 A line of Tln, which arises from 6s  $7s^1S_0 \rightarrow 6s$   $6p^1P_1$ ,\* and then turned to more complex lines in thallium and bismuth † They worked with the first and second spark spectra, because hyperfine intervals are there larger than in the arc, and they examined each line in three

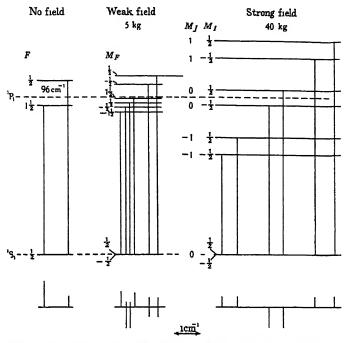


Fig 20 6 Level diagram showing the splitting of the  $3092\,\mathrm{A}$ ,  $^1\mathrm{S}_0 \! \to \! ^1\mathrm{P}_1$ , line of Tl II in weak and strong magnetic fields. The displacements shown are calculated from the vector model

fields In these heavy elements, the Doppler effect does not produce so wide a line as when the atom is light, moreover, thallium and bismuth provide a convenient contrast, for their nuclear moments are  $\frac{1}{2}$  and  $4\frac{1}{2}$  respectively, so that in a strong field the thallium lines split to two components while the bismuth split to ten

Consider then the 3092 A line of Tl  $\pi$ , of the two terms,  ${}^{1}\!S_{0}$  and

- \* Green and Wulff, ZP, 1931, 71 593
- † Green and Wulff, PR, 1931, 38 2176, 2186

 $^1\mathrm{P}_1$  (Fig 20 6), from which it arises, the first does not split but the second has a hyperfine interval of -0.96 cm  $^{-1}$ , so that the interval quotient A is -0.64 cm  $^{-1}$ , while in the weakest field used, namely 14,700 gauss, the Lorentz unit  $o_m$  is 0.69 cm  $^{-1}$  In this field then  $o_m$  is not 'much smaller' than  $\Delta \nu$  and the splitting is likely to be characteristic of an intermediate rather than of a weak field, but in fact the simple Zeeman theory does give good qualitative agreement. For the  $F=1\frac{1}{2}$  and  $\frac{1}{2}$  components of the  $^1\mathrm{P}_1$  term g(F) works out at  $\frac{2}{3}$  and  $\frac{4}{3}$  respectively, so that the patterns predicted are  $\pm (1)$  1 3/3 and  $\pm (2)$  2/3, while the dis-

Field strength	14,	700 g	43,350 g		
M <sub>F</sub>	Vector model	Quantum mechanics	Vector model	Quantum mechanics	
11/2	0 37	0 37	1 51	1 51	
1/2	1 10 - 0 09	1 06 -0 05	2 15 0 32	2 17 - 0 025	
-1	0 18 - 0 55	0 11 -0 48	$-032 \\ -151$	0 005 -1 50	
-11/2	-101	-101	-2 15	-2 15	

Fig 20.7 Displacements of the  $^1P_1$  term of Tl  $\pi$  in weak and strong magnetic fields

placements calculated by equation (20 3) work out as 0 37, -0.09, -0.55 and -1.01 for  $F=1\frac{1}{2}$ , and 1 10 and 0 18 for  $F=\frac{1}{2}$ . Fig. 20 7 shows how these calculations compare with the more accurate predictions of the quantum mechanics

In contrast a field of 43,350 gauss produces a Lorentz unit of 2 02 cm  $^{-1}$ , so that splitting characteristic of a strong field is to be expected. In fact theory shows that the 3092 A line splits to six components, whose displacements are  $\pm$  (0 32), 0 32, 1 51, 2 15. The pattern thus consists of three pairs of lines, one at the centroid of the hyperfine doublet and the other two arranged symmetrically on either side, and in general terms this is what experiment reveals, though the numerical agreement is not close

Better numerical agreement is, however, obtained if the more precise theory of the wave mechanics is substituted for the

1.025 instead of 1 since the coupling is not pure (LS), but shows some signs of the (jj) type so that the g factor of the  $^{1}\mathrm{P}_{1}$  term is influenced by other terms which he near; the numerical value of the correction is obtained by the method of Houston \*

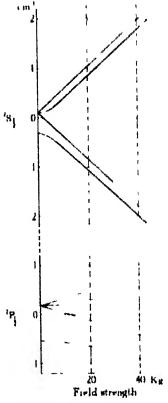


Fig. 20-10. Displacements of the hyperline components of the  $lambda_4$  and  $rac{11}{4}$  levels of Tl 1 in various fields. The displacements are calculated by equations (20 8) of the quantum mechanics.

Thus theory interprets this simple pattern with great success; nor is it less successful with the more complex patterns of Th. Back and Wulff† photographed the 3776 A., <sup>2</sup>S<sub>4</sub> - <sup>2</sup>I<sup>\*</sup><sub>4</sub>, line in fields of 17,050, 29,700 and 43,350 gauss. In these fields the Lorentz unit assumes the values 0-80, 1-40 and 2-08 cm. <sup>3</sup>, while

<sup>\*</sup> Houston, PR, 1929, 38 297.

<sup>†</sup> Back and Wulff, ZP, 1930, 66 31

the hyperfine intervals of the  $^2\mathrm{S}_{\frac{1}{2}}$  and  $^2\mathrm{P}_{\frac{1}{2}}$  terms are 0 40 and 0 71 respectively, so that all three fields are technically 'strong' The magnetic field and nuclear moment would thus separately split each term in two, the Zeeman components being determined by  $M_J=\pm\frac{1}{2}$ , and the hyperfine components by  $M_I=\pm\frac{1}{2}$  According to the wave mechanics the displacements of these four levels from the centroid are given by the equations

and shown graphically in Fig. 20 10. As previously g is here an abbreviation for g(J)

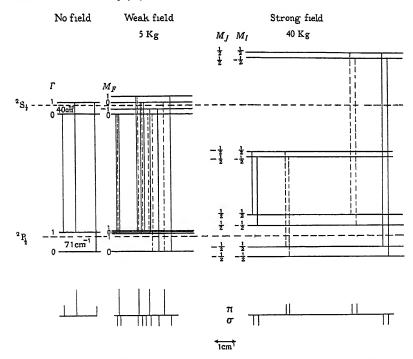


Fig. 20 11 Level diagram to show the structure of the 3776 A,  $^2S_{\frac{1}{2}} \rightarrow ^2P_{\frac{1}{2}}$ , line of Tl I in weak and strong magnetic fields. The diagram assumes that the laws of the vector model are valid

When the four levels of each gross term combine, they would give rise to six  $\pi$  and eight  $\sigma$  components in a weak field, but in a strong field two  $\pi$  and four  $\sigma$  components fade, for in a strong field transitions in which  $M_I$  changes its value are no longer allowed (Fig. 20-11). The empirical displacements are compared with this theory in Fig. 20-12, the centroid of the empirical pattern being adjusted so that the line of lowest frequency has the value dictated by theory. The empirical intensities are estimated, not

Field	Par	allel comp	llel components			Perpendicular components			
in gauss -	Position (cm <sup>-1</sup> )		Intensity		Position (cm <sup>-1</sup> )		Intensity		
gatass	Calc	Obs	Calc	Obs	Calc	Obs	Calc	Obs	
17,050	1 344 0 456 \ 0 455 \ -0 302 -0 609 -1 190	1 39 0 50 - 0 24 - 0 57 - 1 19	3 1 6 9 1 10 0 5 6 9 10 3 1	3 10 8 10 3	1 521 0 810 0 633 0 278 -0 075 -0 863 -0 963 -1 368	1 62 0 93 0 76 0 34 -0 05  -0 94 -1 368	8 0 9 85 2 0 0 15 2 0 0 15 8 0 9 85	9 9 1 0 5 3 6 10	
43,350	2 89 1 36 1 28 -1 20 -1 44 -2 74	2 91 1 50 1 17 -1 06 (1 19) -1 32 (1 43) -1 55 -2 74	0 8 9 2 10 9 2 10 0 8	6 7 9 2 7 10 6	3 08 2 45 1 55 1 09 -1 00 -1 65 -2 52 -3 00	3 11 2 46 1 59 	9 4 10 0 0 6 0 02 0 6 0 02 9 4 10 0	10 10 1 - 1 - 10 10	

Fig 20 12 Splitting of the 3776 A line of Tl I compared with the predictions of the quantum mechanics in two magnetic fields

measured To prove that the vector model gives a reasonable approximation to these results is left to the reader

In bismuth the theory is of course unchanged, but one line may be cited to show how the nuclear moment was first determined by the use of a magnetic field \* The 4722 A line arises from the  $l_{\frac{1}{2}} \rightarrow {}^2D_{1\frac{1}{2}}$  transition, so that in the absence of hyperfine structure it should split to two  $\pi$  and four  $\sigma$  components. When the line was examined in a field of 43,340 gauss, these components were found,

<sup>\*</sup> Back and Goudsmit, ZP, 1928, 47 174 Zeeman, Back and Goudsmit, ZP, 1930, 66 1.

\*×]

but all were exceptionally wide, and four were clearly resolved into ten components (Fig. 20 13) Now the energy of a magnetic level is  $E/ch = AM_IM_I + M_Ig(J)o_m$ ,

Where the second term determines the gross Zeeman level and the first term its hyperfine structure, as  $M_I$  can assume (2I+1)

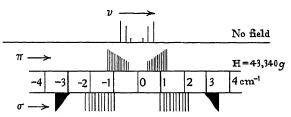


Fig. 2013 Empirical structure of the 4722 A,  $l_1 \rightarrow ^2D_{12}^\circ$ , line of Bi iin a strong magnetic field (After Back and Goudsmit, ZP, 1928, 47 179)

Values, each gross term will have (2I+1) components (Fig 20 14) Moreover, as  $M_I$  is not allowed to change in a transition the gross Zeeman lines will also split to (2I+1) components, the interval being  $A'M_{J}' - A''M_{J}''$  (Fig 20 15) Thus, if in fact the lines split to ten components the nuclear moment must be  $4\frac{1}{2}$  And it is of some interest to note that the value of the interval was also confirmed, the hyperfine interval quotients of the  $^2D_{1\frac{1}{2}}$  and  $1\frac{1}{4}$  terms are known to be -0.0403 and 0.166 cm  $^{-1}$  respectively, so that the interval of the  $\pi$  components should be

$$A'M_{J}' - A''M_{J}'' = -0.0403(-\frac{1}{2}) - 0.166(-\frac{1}{2})$$
  
= 0.1031 cm<sup>-1</sup>,

and of the outer  $\sigma$  components

$$A'M_{J}' - A''M_{J}'' = -0.0403 \times \frac{1}{2} - 0.166 (-\frac{1}{2})$$
  
= 0.0628 cm<sup>-1</sup>

Now the width of the  $\pi$  components was measured as 0 880 cm<sup>-1</sup>, so that the interval between successive components must be 0.880/9 or 0 0977 cm<sup>-1</sup> The width of the outer  $\sigma$  components is 0.520 cm<sup>-1</sup>, and the interval accordingly 0 0577 cm.<sup>-1</sup> Both are satisfactory agreement with theory

In Figs 20 16–17 evidence is presented for two still more complex lines, 2298 A,  $2^3S_1 \rightarrow 2^3P_2$  of Tlu and 5719 A,  $^3P_0 \rightarrow ^3P_1^{\circ}$  of

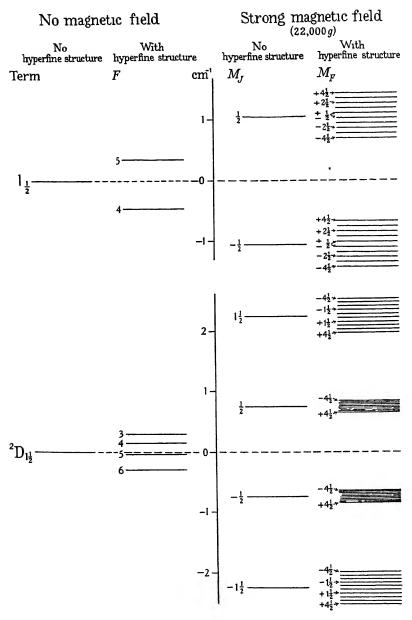
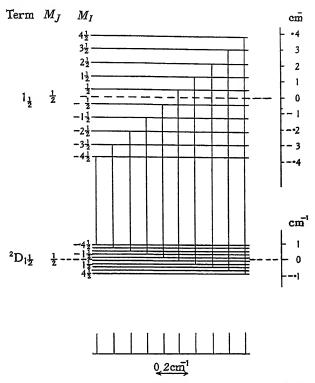


Fig 20 14 Structure of the  $l_{\frac{1}{2}}$  and  ${}^2D^{\circ}_{1\frac{1}{2}}$  levels, which produce the 4722 A line of Bi I The laws of the vector model are assumed, and the field strength has been reduced to half that actually used to keep the figure within reasonable limits, the g factors are abnormal being 1 225 and 2 088 in the two terms

Bi  $\Pi$ ,\* in each figure the photometer curve appears above and the theoretical pattern below, and in both the agreement is all that can be desired

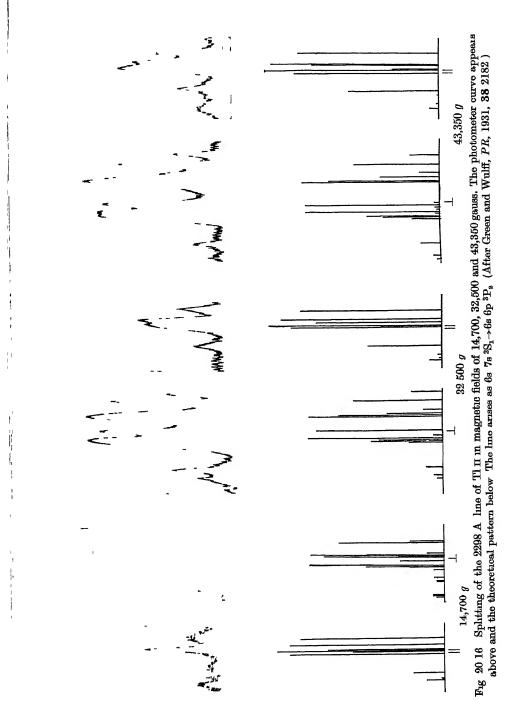


 $F_{1g}$  20 15 Level diagram to show the hyperfine structure of one gross  $\sigma$  component of the 4722 A line of Bi i

#### 5. Intensities

No absolute measurements of intensity seem to have been made, but the photometric curves obtained by Zeeman, Back and Goudsmit in 1930 showed that the intensity formulae deduced from the wave mechanics are qualitatively correct, while more recently these rules have been so widely applied to the analysis of the complex structures described in the next section and the results have been so satisfactory, that few serious deviations can exist

<sup>\*</sup> Green and Wulff, PR, 1931, 38 2182, 2186



In order that the hyperfine components of a line may be observed with their theoretical intensities, however, the exciting source must fulfil certain conditions. Thus the temperature of the source must be as low as possible so as to reduce the Doppler broadening of the lines, the source is therefore worked in liquid air or liquid hydrogen. And secondly, the vapour pressure of the

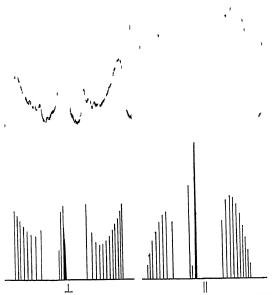


Fig 20 17a Splitting of the 5719 A line of Bi II in a magnetic field of 14,700 gauss, again the photometer curve is above and theory below. The line arises as 6p 7p  $^3P_0 \rightarrow 6p$  7s  $^3P_1$  (After Green and Wulff, PR, 1931, 38 2186)

element in the source must be kept low, for high pressure leads to self-absorption, besides hyperfine intensities seem in some way disturbed by inter-atomic fields, though why they should be is not yet clear \*

The intensity formulae, deduced from the wave mechanics by Hill,† correspond to the multiplet intensity formulae with the transformation (Fig. 20 5) already used in the interval rule

<sup>\*</sup> Schuler and Keyston, ZP, 1931, 71 413

<sup>†</sup> Hill, Nat Acad Scr., Proc 1929, 15 779

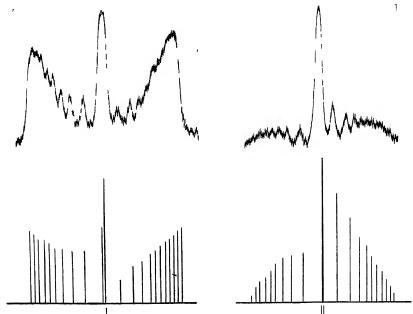


Fig 20 17b Splitting of the 5719 A line of Bi  $\pi$  in a field of 32,500 gauss

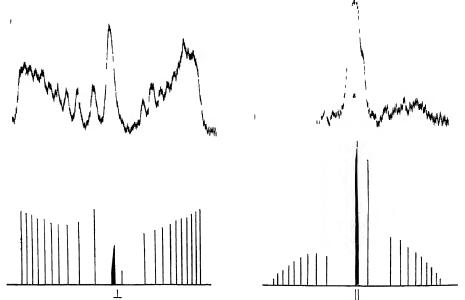


Fig 20 17c Splitting of the 5719 A line of Bi  $\pi$  in a field of 43,350 gauss

where

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In the jump  $J \rightarrow (J-1)$  and

$$\begin{split} F \to (F-1) & I_- = \frac{1}{F} \, P(F) \ P(F-1), \\ F \to F & I_0 = \frac{(2F+1)}{F(F+1)} \ P(F) \ Q(F), \\ (F-1) \to F & I_+ = \frac{1}{F} \ Q(F) \ Q(F-1), \end{split}$$

while in the jump  $J \rightarrow J$ , and

$$F \to F \qquad I_0 = \frac{(2F+1)}{F(F+1)} \ R^2(F),$$
 
$$F \to (F-1) \qquad I_{\pm} = \frac{1}{F} P(F) \ Q(F-1),$$
 
$$P(F) = (F+J) (F+J+1) - I(I+1),$$
 
$$Q(F) = I (I+1) - (F-J) (F-J+1),$$

In all these formulae the transitions are so chosen that J and F are the larger of the two quantum numbers involved. Moreover, a term containing only J and I has been dropped since in fact the formulae are applied to the components of a single gross line

R(F) = F(F+1) + J(J+1) - I(I+1)

The Zeeman intensity formulae may be transformed in the same way and compared with the visual estimates of Back and Wulff \*

# 6. Isotope displacement

The vector model, based on the hypothesis of nuclear spin, solves many of the problems of hyperfine structure, but there is clear evidence that when several isotopes exist, the vector model does not suffice

Consider, for example, the Tl I line, 5351 A ,† which arises as  $7s^2S_{\frac{1}{2}} \rightarrow 6p^2P_{1\frac{1}{2}}$ , work on the 3776 A line of Tl has already been adduced to show that the nuclear moment of Tl is  $\frac{1}{2}$ , so that the 5351 A line might be expected to split to three components with an intensity ratio of 5–2–1 as shown in Fig. 20–18, but in fact the

<sup>\*</sup> Back and Wulff, ZP, 1930, 66 31 † Schuler and Keyston, ZP, 1931, 70 1

line splits to four components, and these have intensities roughly in the ratio of 6 9 3 2 3 1, that is two pairs with an intensity ratio of 3 1, now the three lines of theory can be reduced to two with an intensity ratio of 3 1 if the two components of the  ${}^{2}P_{1\frac{1}{2}}$  term are not resolved Accordingly, the empirical facts can be explained if there are two isotopes of Tl with an abundance ratio of 2 3 1, and if the term schemes of these two isotopes are displaced slightly relative to one another, in short that is if the term

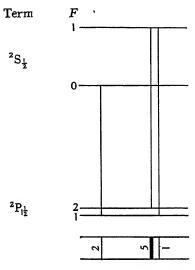


Fig 20 18 Structure of a normal  ${}^2S_{\frac{1}{2}} \rightarrow {}^2P_{1\frac{1}{2}}$  line

scheme of Fig. 20 19 is postulated. In this diagram the energy of the  ${}^2\!S_{\frac{1}{4}}$  term is supposed the same in both isotopes, though in fact only the displacements of the one term relative to the other can be measured, experiment then shows that the  ${}^2\!P_{1\frac{1}{4}}$  term is displaced through 55 X in one of the isotopes 203 and 205. The existence of the isotopes 203 and 205 in the abundance ratio of 1–2 3 has been confirmed by the analysis of many Tl II lines, while more recently Aston\* has found a ratio of 1–2 40

Isotopes have been observed displaced in the lines of many elements, but of all mercury is the most complex, for it consists of

<sup>\*</sup> Aston, PRS, 1932, 134 571.

six isotopes,\* of these the four of even atomic weight have zero moment, but the two odd isotopes have different nuclear moments, namely  $\frac{1}{2}$  and  $1\frac{1}{2}$ , and to make confusion worse confounded the terms of one are inverted

To illustrate the methods by which such a complicated line

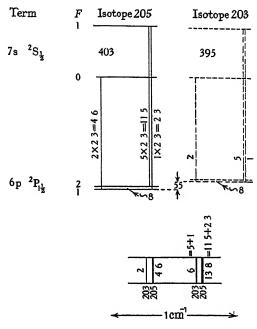


Fig 20 19 Structure of the 5351 A ,  $^2\!S_{\frac{1}{4}}\!\to\!{}^2\!P_{1\frac{1}{2}},$  line of Tl 1 (After Schuler and Keyston, ZP, 1931, 70 3 )

structure can be analysed, consider two mercury arc lines, 2536 and 4078 A ,† which arise as  $2\,^3P_1 \rightarrow 1\,^1S_0$  and  $2\,^1S_0 \rightarrow 2\,^3P_1$ , these lines are in fact particularly simple, for in one term J is zero

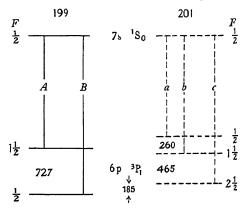
In the analyses described heretofore, three criteria have been used first, the picking of a common hyperfine interval from lines with a common gross structure level, second, the interval rule, and third the intensity rules. Of these the first two suffice for the

<sup>\*</sup> Recent work has revealed more than six isotopes, but in work on hyperfine structure only those present in a proportion of more than 1 per cent need usually be considered

<sup>|</sup> Schuler and Keyston, ZP, 1931, 72 423

analysis, when the structure is simple, but the last is the most valuable when the structure is complex. That the method has been so successful is perhaps the best evidence of the wide validity of the intensity formulae.

To obtain the theoretical intensities of the components of a line, the intensity ratios of the components due to a single isotope must first be calculated, and these must then be weighted with the



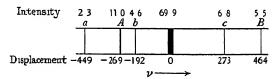
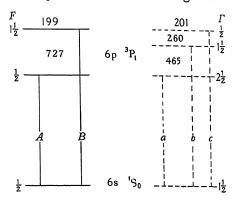


Fig. 20 20 Structure of the 4078 A, 2  $^1S_0 \rightarrow 2$   $^3P_1$ , line of Hg I The displacements are given in  $10^{-3}$  cm. $^{-1}$  (After Schuler and Keyston, ZP, 1931, 72 428)

isotope abundance. Thus the even isotopes produce only one component each, but the isotopes 199 and 201, having nuclear moments of  $\frac{1}{2}$  and  $1\frac{1}{2}$ , produce two and three components respectively. These are shown as A, B and a, b, c in Figs. 20 20–21, and the theoretical intensity ratios are calculated as 2–1 and 1–2–3. But the mass spectrograph has shown that mercury contains 16-44 per cent of isotope 199, so that the absolute intensity of the A component should be  $\frac{2}{3}$  of 16 44 or 10 96, and similarly since isotope 201 occurs to the extent of 13 68 per cent, the line b

should be of absolute intensity  $\frac{1}{3}$  of 13 68 or 4 56. The intensities calculated in this way are summarised in Fig. 20 22.



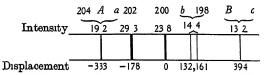


Fig 20 21 Structure of the 2536 A,  $2^3P_1 \rightarrow 1^1S_0$ , line of Hg I The displacements are again in  $10^{-3}$  cm<sup>-1</sup> (After Schuler and Keyston, ZP, 1931, 72 434)

Isotope	Abundance ratio	Component	Relative intensity	Absolute intensity
199	16 44	A B	2	10 96 5 48
201	13 68	a b c	1 2 3	2 28 4 56 6 84
198 200 202 204	9 89 23 77 29 27 6 85 99 90	No hyperfir	l ne structure	9 89 23 77 29 27 6 85 99 90

Fig 20 22 Intensities in a  ${}^{3}P_{1} \rightarrow {}^{1}S_{0}$  or  ${}^{1}S_{0} \rightarrow {}^{3}P_{1}$  line of Hg i

With these predictions in mind, the analysis of the structures shown in Figs 20 20 and 21 presents no great difficulty, provided one understands that components separated by less than 0 030 cm $^{-1}$  are not resolved

This somewhat complicated analysis of the 2536 A. line has

been beautifully confirmed by Mrozowski,\* who has shown that when separately excited the various isotopes behave like a mixture of independent gases. If light from a mercury arc is sent through mercury vapour in a magnetic field, various hyperfine components can be filtered out. By varying the field strength Mrozowski in this way isolated three groups of lines, (a) the  $394\ 10^{-3}$  cm<sup>-1</sup> component, (b) the +161 and -333 components, (c) the 0.0 and -178 components. No matter which of these groups is used to excite cold mercury vapour, the resonance radiation contains only that group, when only the +161 and -333 components are incident, only these two components are emitted. Thus each hyperfine line is itself a resonance line and there is no fluorescence.

Fluorescence appears, however, when a little helium is added to the tube,† for the increased pressure means inelastic collisions for the mercury atoms. If the cold vapour mixed with helium is excited by the +394 line, the three lines +394, +161 and -333 are emitted, for the +394 line excites both the 199 and 201 isotopes and these after losing a little energy in colliding with a helium atom can return to the ground state while emitting the +161 or -333 line. The details are easily followed in Fig. 20.21. On the other hand, irradiate the vapour with the 0.0 and -178 lines, and only these lines are emitted, for these lines excite only the 200 and 202 isotopes, and as these have only one upper level they must radiate what they absorbed

The analysis of a single line (Fig. 20 23) does not determine the absolute isotope displacements of either term, it determines only the displacements of the isotopes in one term relative to their displacements in the other, and what is true of the analysis of a single line is true of the analysis of any number of lines, so that apparently the absolute displacements can never be determined Many lines, however, which arise between high levels of the mercury atom show no hyperfine structure at all, so that all the terms concerned must have identical isotope displacements, and

<sup>\*</sup> Mrozowski, Sci Bull Acad Pol 1930, 464, 1931, 489 The lines with displacements of 132 and 161  $10^{-3}$  cm $^{-1}$  in Fig 2021 were not resolved in these experiments, they are referred to on this page as the 161 line

<sup>†</sup> Mrozowski, ZP, 1932, 78 826

this is extremely improbable unless the displacements of all are zero. In support of this thesis, theory and experiment show that isotope displacements must and do decrease, as the chief quantum number increases (Figs. 20.24—26)

The hyperfine levels thus obtained may be simplified by substituting for the odd components a single level at the centroid of the isotope, and when this is done an interesting regularity

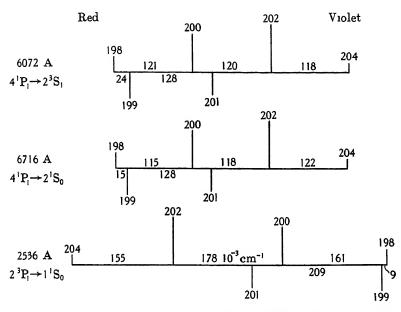


Fig 20 23 Centroids of the isotopes in three lines of Hg  $\scriptstyle\rm I$  (After Schuler and Keyston, ZP, 1931, 72 423)

emerges, the interval separating each even isotope from its neighbour is roughly constant and equal to the interval separating the odd isotopes, but the odd isotopes are not spaced mid-way between the even isotopes, this is clearly shown in Fig 20 23 and is true not only in Hg I, but also in Pb I and Pb II. As the isotopes are not displaced in the upper levels of many lines, this property may well be demonstrated in a single line

The relative energies of the isotopes also need to be related to their masses, for there has never been any doubt that the sequence of the isotopes is the sequence of their masses, nor that in the arc and spark spectra of mercury the isotope of lowest atomic

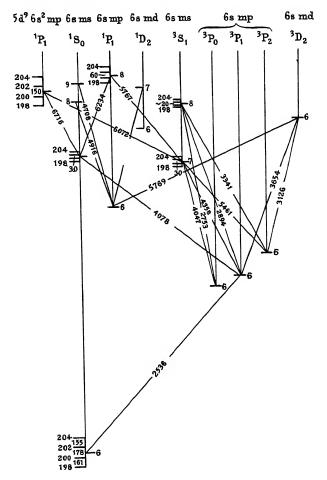


Fig 20 24 Isotope displacements in Hg  $\scriptstyle\rm I$  The wide splitting of the 8p  $^{\rm 1}P_{\rm 1}$  term is anomalous (After Kallmann and Schuler, EEN, 1931, 11 165)

weight lies lowest In the light of recent theory this order seems to be general, but several spectra have been a little difficult to bring into line, thus the displacements in thallium seemed to be in different directions in the arc and spark spectra, but Breit\* has

<sup>\*</sup> Breit, PR, 1932, 42 348

since shown that this was due to a misinterpretation of certain lines of Tl  $\pi$  and that in fact the isotopes of thallium are arranged like the isotopes of mercury, the smallest at the bottom. The

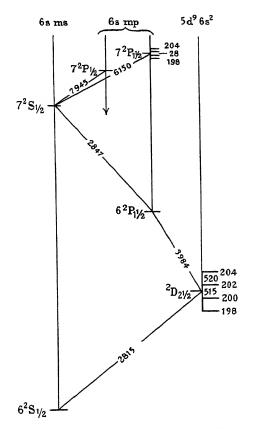


Fig 20 25 Isotope displacements in Hg II (After Kallmann and Schuler,  $\it EEN, \, 1932, \, 11 \, 167$  )

theoretical explanation is interesting, isotope displacements are due to the increase in the volume of the nucleus resulting on the addition of a neutron,\* this causes the same charge to occupy a larger volume and so reduces the electrostatic energy of the system, as the electrostatic energy of a condenser is negative,

<sup>\*</sup> Schuler and Schmidt, ZP, 1935, 94 463

this means that the terms of the larger isotope lie higher than the smaller

Turning to the quantitative side, the displacement of one isotope relative to another seems to be the same for all terms of a

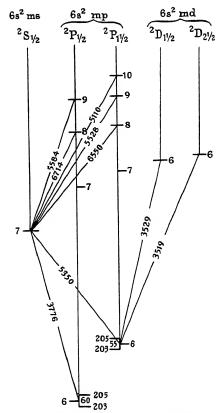


Fig 20 26 Isotope displacements in Tl I (After Kallmann and Schuler, EEN, 1932, 11 167)

configuration, Fig 20 27 shows this regularity in the 6s<sup>2</sup> 6p<sup>2</sup> configuration of Pb 1 Attempts actually to calculate the displacement have not yet met with complete success, because large corrections have to be made for the screening of one configuration by another, and these cannot be accurately estimated. Of partial solutions the most important is that produced by Breit,\* who has

<sup>\*</sup> Breit, PR, 1932, 42 348

related the displacement to the nuclear radius, the latter being assumed proportional to the cube root of the mass, but there is little doubt that other influences contribute \*

204	<sup>1</sup> S <sub>0</sub>	$^{1}\mathrm{D_{2}}$	<sup>3</sup> P <sub>2</sub>	<sup>8</sup> P <sub>1</sub>	<sup>3</sup> P <sub>0</sub>	904
206	65	84	?	?	?	204
208	72	88	90	85	83	206 208

Fig 20 27 Isotope displacements in the 6s2 6p2 configuration of Pb I

### 7 Deviations from the interval rules

In general hyperfine multiplets obey the interval rule better than gross multiplets, but this very regularity makes exceptions the more striking. When two gross levels lie near one another and satisfy certain conditions they perturb one another, one may expect the same phenomenon among hyperfine levels, and in fact Schuler and Jones | have shown that when in HgI the 6d 1D. and 6d 3D, levels lie at a distance apart comparable with their hyperfine intervals, the interval rule is no longer valid and the isotope displacements are anomalous. In the Hg<sup>201</sup> isotope the hyperfine intervals of the  $6d \, ^{1}D_{2}$  term are 181, 301 and 313  $\, ^{10^{-3}}$ cm<sup>-1</sup>, numbers which are in the ratio of 3 0 5 0 5 2 instead of in the normal ratio of 3 5 7 Moreover, in these terms the even isotopes are all coincident, showing that there is no isotope displacement, but the centroids of the odd isotopes instead of coinciding with the even isotopes he farther apart. This suggests at once that the reason why both intervals and isotope displacements are abnormal, is that the two terms perturb one another, for the characteristic sign of perturbation is repulsion Among gross multiplets two components can perturb one another only If they have the same J, and so among hyperfine multiplets we may expect components to perturb one another only if they have the same F, if this is true the even isotopes will not be displaced, for in them I is zero, and the two levels will have different values

<sup>\*</sup> Breit, PR, 1933, 44 418 $\alpha$ , Bartlett and Gibbons, PR, 1933, 44 538, Grace and More, PR, 1934, 45 169

Schuler and Jones, ZP, 1932, 77 801

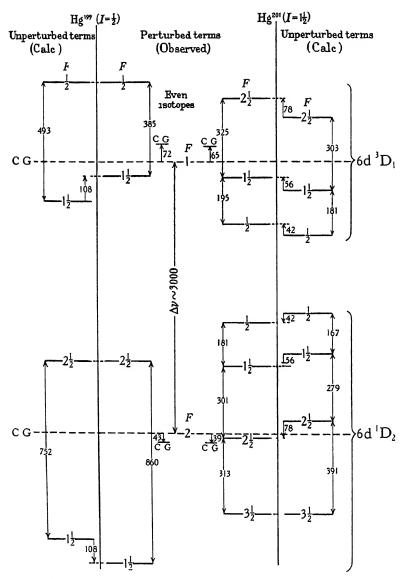


Fig 20 28 Two perturbed terms of mercury In the middle between the two uprights is the observed term system, while to left and right the terms are shown in the positions they would occupy if they were not perturbed The argument by which the various displacements are obtained is fully given by Schuler and Jones, ZP, 1932, 77 806

of F, namely 1 and 2. This makes the investigation much simpler than the analogous investigation of two gross multiplets, for the even isotopes provide a fixed scale of reference

A bird's eye view of the changes produced by perturbation is provided by Fig. 20.28, in the 199 isotope system, the levels in which F is  $1\frac{1}{2}$  perturb one another, while the levels in which F is  $\frac{1}{2}$  above and  $2\frac{1}{2}$  below remain undisturbed. As the two levels in which F is  $1\frac{1}{2}$  repel one another, the  ${}^1D_2$  term has an enlarged and the  ${}^3D_1$  a reduced interval. In the isotope 201 on the other hand three components wander, for there are levels with F values of  $\frac{1}{2}$ ,  $1\frac{1}{2}$  and  $2\frac{1}{2}$  in both gross terms, only the  $F=3\frac{1}{2}$  level of the  ${}^1D_2$  term remains undisturbed. The repulsion of the levels with  $F=\frac{1}{2}$ ,  $1\frac{1}{2}$  and  $2\frac{1}{2}$  leads to a great reduction of the  $2\frac{1}{2}-3\frac{1}{2}$  interval, and a consequent departure from Landé's interval rule

When the interval rule is not obeyed the interaction between the nucleus and the electron shells is no longer proportional to the scalar product of the two vectors, and the vector model fails,\* the quantum mechanics shows, however, that two states lying close to one another perturb one another and gives a satisfactory account of the displacements †

As perturbation is a phenomenon well known when two gross multiplets lie close to one another, physicists have naturally tried to use it to explain all deviations from the interval rule. But whereas two gross levels may perturb one another when 2000 cm<sup>-1</sup> apart, two hyperfine levels must lie within a few units of one another, and so it is much less probable that an unknown level lies close enough to produce the observed distortion. And in fact Schuler and Schmidt have shown that some multiplets in Eu<sup>151</sup>, Eu<sup>153</sup>, Lu<sup>175</sup>§ and Hg<sup>201</sup>|| do not satisfy the interval rule, and that perturbation is an inadequate explanation. Instead of the displacements of the levels from the centroid being proportional simply to  $\cos(\mathbf{IJ})$ , a second term proportional to  $\cos^2(\mathbf{IJ})$ 

<sup>\*</sup> Casımır, ZP, 1932, 77 811

<sup>†</sup> Goudsmit and Bacher, ZP, 1933, 43 894

<sup>|</sup> Schuler and Schmidt, ZP, 1935, 94 457

<sup>§</sup> Schuler and Schmidt, ZP, 1935, 95 265

<sup>||</sup> Schuler and Schmidt, ZP, 1935, 98 239.

appears, this second term has a coefficient small compared with that of the normal  $\cos{(\mathbf{IJ})}$  term, but though the deviations are small, they are greater than the experimental error. Whether this second term affects the extreme interval is doubtful, its obvious result is to make the levels crowd towards the levels of large or small F, the one when the term is positive the other when it is negative

The appearance of a cos<sup>2</sup> term means that the interaction of the nucleus and electrons cannot be wholly explained as due to the action of a magnetic nuclear dipole on the electrons, the form the deviation takes suggests that the new force is electrostatic in origin, and is due to a lack of spherical symmetry in the electric field of the nucleus \*

# 8. The spin of the nucleus

The spin of an atomic nucleus may be obtained from the hyperfine structure of a line, from the deflection of an atomic ray in a magnetic field and from the alternating intensities of band spectra. All three methods have been applied to sodium, and all give the same nuclear spin, and more generally where two methods have been used the results are consistent. Besides these three methods there are others which are permissible in theory, but which do not seem to have been used as yet, these are the specific heat at low temperatures; and scattering; ‡

An atomic ray can be used only if the resolution is increased by including a magnetic velocity selector, this consists of an inhomogeneous magnetic field, which spreads the beam out into a velocity spectrum. A movable slit selects a part of the beam homogeneous in velocity to about 10 per cent, and this then passes through a weak inhomogeneous field of the Stern-Gerlach type, thereafter a third magnetic field is used to focus the beam on the detector wire. This technique has only recently been perfected, but already in Rabi's hands it has disclosed the spin of

<sup>\*</sup> The equations for the interaction of such a core with the nucleus have been given by Casimir, *Physica*, 1935, 2 719

<sup>†</sup> Dennison, PRS, 1927, 115 483

<sup>‡</sup> Sexl, Nw, 1934, 22 205

 $<sup>\</sup>S$  Rabi and Cohen, PR, 1933, 43 582a

potassium and in Stern's the magnetic moments of the proton and deuton,\* important quantities which could not have been easily measured by other methods. When applied to sodium the

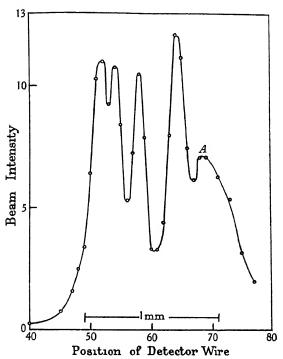


Fig 20 29 An atomic ray of sodium split into four components in passing through a magnetic field. The high resolution is obtained by using an inhomogeneous magnetic field and a slit to select a beam homogeneous in velocity to 10 per cent. The figure shows the points obtained in one particular run. The peak marked A is due to atoms other than those selected. (After Rabi and Cohen, PR, 1933, 43 582.)

beam splits into four components as shown in Fig 20 29, the spin of sodium is therefore  $1\frac{1}{2}$  †

In the application of band spectra; to this purpose, the relative intensities of the alternating bands of symmetrical molecules

- \* References to particular elements appear in the bibliography of h f s
- † Broit and Rabi, PR, 1931, 38 2082 a, Rabi and Cohen, PR, 1933, 43 582 a, Rabi, Kellogg and Zacharias, PR, 1934, 46 157, Dickinson, PR, 1934, 46 598
  - Jevons, Band spectra of diatomic molecules, 1932, 140

are measured,  $Cl^{35}Cl^{35}$  is a symmetrical molecule,  $Cl^{35}Cl^{37}$  is not, there are no alternating intensities in the bands of unsymmetrical molecules. The rotational levels of a symmetrical molecule divide into two systems, known as symmetrical or (s) and antisymmetrical or (a), a level of one system never combines with a level of the other, (s) combines only with (s) and (a) only with (a). An (s) line defined by J lies between two (a) lines defined by (J-1) and (J+1), but its intensity is not a mean of its neighbours, the symmetrical lines are strong and the anti-symmetrical lines are weak. Theory ascribes this alternating intensity to the nuclear spin of the atoms, and shows that if the intensities are as  $I_s$  to  $I_a$ , then

$$\frac{I_s}{I_a} = \frac{I+1}{I}$$
,

or in tabular form

When I is zero, the alternate lines are missing, so that the appearance of the anti-symmetrical lines is quite definite proof that I is not zero, but as intensities are not easily measured accurately, this method is not well adapted to measuring large nuclear moments, any estimate greater than  $1\frac{1}{2}$  is certainly dubious. The method has been applied to show that the nuclein He<sup>4</sup>, C<sup>12</sup>, O<sup>16</sup>, S<sup>32</sup> and Se<sup>80</sup> have no nuclear spin, and to estimate the nuclear spin of ten other elements, in the table of values these are indicated by a B

An examination of the spins obtained by hyperfine structure and band spectra (Figs 20 30–32) shows that they divide nuclei into two groups, in one of which the mass is odd and in the other even Other evidence suggests that nuclei should be further divided according as the charge is odd or even When the mass and charge are both even, the spin is always zero, this statement is supported by measurements on more than 30 nuclei. When mass is even and the charge odd, the spin is certainly 1 in H<sup>2</sup> and N<sup>14</sup>, of this the alternating intensities of band spectra leave no doubt, in Li<sup>6</sup> the absence of hyperfine structure has been taken to indicate zero spin, but a narrow hyperfine structure can easily be

missed Nuclei of this type are so unstable that only four examples are known. When the mass is odd, the spin is always half an odd integer, from time to time, zero moment has been ascribed, to a nucleus of this type, but in view of the 42 nuclei which conform and the fact that hyperfine structure can always be missed if the lines are too blurred or the resolving power too low, they need not be further considered, no exception has been established

How these regularities are related to be the structure of the nucleus can be most profitably considered after the magnetic moments have been discussed

## 9 The magnetic moment of the nucleus

The simplest theory of hyperfine structure ascribes a magnetic moment to the nucleus, and argues that when this acts upon an electron in its orbit, the electronic term splits. If the coupling of the nucleus and electron obeys a cosine law, this hypothesis can be shown to predict the doublet formulae, the interval rule and the usual magnetic splitting \*

In particular the displacement of a particular level from the centroid will be given by the formula

$$\begin{split} \nu - \nu_G &= A \, I \, J \, \cos \left( I \, J \right) \\ &= \frac{1}{2} A \, \{ F \, (F+1) - J \, (J+1) - I \, (I+1) \}, \end{split}$$

where A is the hyperfine interval quotient \* When only one electron is active A is identical with a, the electronic interval quotient, which is determined by the formula

$$a = \frac{R\alpha^2 Z^3}{n^3 (l + \frac{1}{2}) j (j + 1)} \frac{g(I)}{1838}$$
 cm  $^{-1}$ 

for a hydrogen-like orbit, or by

$$a = \frac{R\alpha^2 Z_i^2 Z_a^2}{n^{*3} (l + \frac{1}{2}) j(j+1)} \frac{g(I)}{1838} \text{cm}^{-1}$$

for a penetrating orbit. The latter is considered as composed of two parts, an inner in which the electron moves as if under the influence of a charge  $Z_i$ , and an outer where the effective charge is  $Z_a$   $n^*$  is the effective quantum number. In theory these

<sup>\*</sup> Goudsmit, PR, 1931, 37 663, Fermi and Segrè, ZP, 1933, 82 729

1701	lon.	-	T	
Element	Charge	Mass	Spin	Magnetic moments
Ĥ	1	1	1 B	
<u>L</u> u	3	7	$1\frac{1}{2}H, B, R$	3 29 S, G, 3 20 F, 3 20
B	5	11	• • •	, , , , , , , , , , , , , , , , , , , ,
N	7	15		i
F	9	19	1177	ا ا
Na	11	23	$\frac{1}{2}H, B$	3
Al			$1\frac{1}{2}H, B, R$	2 14 S, 2 09 F, 2 08
	13	27	$\frac{1}{2}H$	193S, 21G, 24
P	15	31	$\frac{1}{2}B$	
Cl	17	35	$2\frac{7}{2}B$	
	1	37		
K	19	39	$1\frac{1}{2}R$	0 38, 0 43, 397
		41		0 30, 0 23, 301
Sc	21		$> \frac{1}{2}$ and $\leq 2\frac{1}{2}R$	
Ÿ		45	$3\frac{1}{2}H$	3 6
	23	51	$3\frac{1}{2}H$	1
Mn	25	55	$2\frac{1}{2}H$	
Co	27	59	3 <del>1</del> H	25?
Cu	29	63	$1\frac{1}{4}H$	2 74 S
		65		
Ga	31	69	1177	2748
	•-		$1\frac{1}{2}H$	2 14 S, F, 2 01 G
۸	99	71	$1\frac{1}{2}H$	274S, 149 F, 255 G
As	33	75	$1\frac{1}{2}H$	0 90 S, G
Br	35	79	$1\frac{1}{2}H, B$ ?	
		81	$1\frac{7}{2}H, B^{9}$	ļ
Rb	37	85	$2\frac{1}{2}H$	149 S, 136 F, 13 G
	ĺ	87		
Y	39	89	$1_{\frac{1}{2}}H$	3 06 S, 2 79 F, 2 7 G
Ĉъ	41		4	
Ma.		93	4	37
	43	_		
Rh	45	_		- 1
Ag	47	107		1)
		109		} <0 24 S
In	49	115	$4\frac{1}{2}H$	, E 0 E 0 E 0 E 0 E 4 C
Sb	51	121		5 25 S, 5 3 F, 5 4 G
	-	123	2 <del>1</del> H	2 70 S, 2 7 G, 2 75
I	59		$2\frac{1}{2}H$	2 10 S, 2 1 G, 2 0
Св	53	127	$4\frac{7}{2}H, B$ ?	
	55	133	$3\frac{1}{2}H$	2 91 S, 2 63 F, 2 50
La	57	139	$3\frac{7}{2}H$	25
Pr	59	141	$2\frac{7}{4}H$	· · · - <del>-</del>
II	61		4	
Eu	63	1		
Tb	65			1
Ho	67	185		1
Tu		165		
Lu	69	169	[	
	71	175	$3\frac{1}{2}H$	2 5
Ta	73	181	$3\frac{1}{2}H$	
Re	75	185	$2\frac{1}{2}H$	
		187	$2\frac{1}{2}H$	j
Ir	77	19i	2 H	ļ
		193	19 17	i
Au	79		1 ? H	
Ti		197	1 H	0 23 S, 1 67 F
**	81	203	<u>∓</u> H	147 S, 142 F, 18 G
ъ.	00	205	$\frac{1}{2}H$	147 S. 142 F. 18 G
Bı	83	209	$4\frac{1}{2}H$	1 47 S, 1 42 F, 1 8 G 3 60 S, 3 54 F, 4 0 G
			<u> </u>	0 00 D, 0 0 tr F, 4 U C

1

Fig 20 30 Protonic nuclei with charge and mass both odd. In the spin column, the letters H, B, and R show the method used, hyperfine structure, band spectra or atomic rays. In the column of magnetic moments the letters denote the authority, S for Schuler, ZP, 1933, 88 324, F for Fermi and Segrè, ZP, 1933, 82 748, and G for Goudsmit, PR, 1933, 48 638 Figures given without a letter are from recent papers which can be traced in the bibliography

Element	Charge	Mass	Spin	Magnetic moments
H Lı B	1 3 5	2 6 10	$ \begin{array}{c c} 1 & B \\ 0 & H, \geqslant 1 & R \end{array} $	0 7-0 8 R 0 7-0 8 R
Ñ	7	14	1 B	≤0 2 <i>H</i>

Fig. 20 31  $\,$  Deutonic nuclei with charge odd and mass even  $\,$  For key to letters see Fig. 20 30  $\,$ 

Element	Charge	Mass	Spin	Magnetic moments
Be C O	4 6 8	9 13 17	1/2 ° H	
Ne	10	21		
Mg	12	25		
Sı	14	29		
S	16	33		
Cr	24 30	53 67	11 27	
Zn Ge	32	73	$1\frac{1}{2}H$	
Se	34	77		
Кr	36	83	$\geqslant 3\frac{1}{2}H$	
Sr	38	87	$\geqslant 1\frac{7}{2}H$	-086S
Mo	42	95	_	
_		97		
Ru	44	99 101		
Pd	46	101		
Cd	48	111	$\downarrow H$	-063S, -053F, -067G
-	1	113	$\frac{1}{2}H$	$-0.63\mathrm{S}$ , $-0.53\mathrm{F}$ , $-0.67\mathrm{G}$
$\mathbf{Sn}$	50	115	_	
		117	$\frac{1}{2}\frac{H}{II}$	-095S, -089
		119	$\frac{1}{2}H$	-095S, -089
m.		121 123		
$\mathbf{T}\mathbf{e}$	52	125		
Хe	54	129	$\frac{1}{2}H$	-VA)
220	02	131	$1\frac{3}{4}\widehat{H}$	$ \begin{vmatrix} -\text{ve} \\ +\text{ve} \end{vmatrix} \mu_{129}/\mu_{181} = -1 \ 1 $
Ba	56	135	$2\frac{1}{8}H$	1
		137	$2\frac{1}{2}H$	094S,105F
$\mathbf{Sm}$	62	?		
$\widetilde{\mathbf{G}}\mathbf{q}$	64	?	İ	
Dy	66	161 163		
$\mathbf{Er}$	68	167		
$\mathbf{\tilde{Y}}\mathbf{b}$	70	171		
	'	173	1	
$\mathbf{H}\mathbf{f}$	72	9		
W	74	183		
Os	76	187		
m,	70	189	1 77	
Pt Ha	78 80	195 199	$\frac{1}{2}H$ $\frac{1}{2}H$	055S,046F,055G
Hg	00	201	1½ H	-0 62 S, -0 51 F, -0 62 G
Pb	82	207		0 60 S, 0 67 F, 0 60 G
	-	209	2	

Fig. 20 32  $\,$  Neutronic nuclei with charge even and mass odd. For key to letters see Fig. 20 30  $\,$ 

equations offer a simple method of determining the magnetic splitting factor g(I), and hence the magnetic moment of the nucleus, but in practice a large relativity correction has to be made before these formulae can be applied \* A more general formula is thus of greater value

When several electrons are active the interval quotient can be shown to have the value  $A = \frac{\mu H}{I I},$ 

where  $\mu$  is the magnetic moment of the nucleus, and H is the magnetic field produced by the electrons at the nucleus. When the eigenfunctions of the electrons are known, the field H can be calculated, and then the experimental values of the interval quotient determine the magnetic moment of the nucleus

Whether this theory can be considered satisfactory depends on how well nuclear moments agree when calculated from different terms of the same spectrum, and from different spectra with the same nucleus. That 20 terms distributed among the first three spectra of thallium do all give the same magnetic moment is therefore encouraging.

The magnetic moments thus obtained are summarised in Figs 20 30–32. In these figures the nuclear moment is given in nuclear magnetons,  $\mu_N$ , where

$$\mu_N = \frac{eh}{4\pi Mc} = \frac{\mu_B}{1838},$$

M is the mass of the nucleus and  $\mu_B$  is the Bohr magneton

Of the isotopes of even mass only two magnetic moments are known, H<sup>2</sup> and N<sup>14</sup>, in all the other isotopes the mechanical moment is zero, so that there is no hyperfine structure and therefore no evidence. An inspection of the table of isotopes of odd mass, however, shows a clear division between those of even and odd charge, among the former positive and negative moments are equally frequent, the latter being shown empirically by inverted hyperfine terms, moreover, the moment is always less

<sup>\*</sup> Goudsmit, PR, 1933, 43 636 The precise form the formulae should take seems also in doubt Pauling and Goudsmit, Structure of line spectra, 1930, 60 and 209, note 1

than 1, on the other hand, when the charge is odd, the moment is always positive, and with two or three exceptions it is greater than 1 \*

Though this last statement certainly indicates a tendency, it must not be taken quite at its face value, for there are many spectra in which spectroscopists have commonly failed to find any structure at all, among these are N I, P II, Cl II, K II, K II, Ag I and  $\operatorname{Cd}\Pi$  Band spectra dispose of the hypothesis that the mechanical moments of these atoms are all zero, nitrogen, phosphorus and potassium all spin A second alternative is that the magnetic field produced by the electrons at the nucleus is very weak, but as some of the atoms possess a penetrating s electron such as usually produces wide hyperfine intervals, this explanation is improbable Better is the suggestion that the magnetic moments of these nuclei are small, in two elements certainly recent work supports this, thus Jones | has shown that in Cd II, though 12 out of the 13 lines which he examined have no structure, the thirteenth reveals the ground, 2S, term as double and indicates a nuclear magnetic moment of 0 625  $\mu_N$  In KI too Jackson and Kuhn‡ have recently shown that if sufficient care is taken, the resonance lines may be resolved to a narrow doublet, the lines were obtained from a discharge tube containing neon at a pressure of a few mm and potassium at a pressure of less than one two-thousandth of a mm  $\,$ , before entering the spectrograph, the light passed through a ray of potassium atoms travelling at right angles across its path This atomic ray passed through a cool tube whose length was twenty times its diameter, so that the Doppler width of absorption lines was only 1/20 of that obtained with a random distribution of velocities Resolved with a Fabry-Perot étalon, the lines appeared as a doublet with an interval of 0 015 cm  $^{-1}$ 

<sup>\*</sup> The magnetic moments have been tabulated by Fermi and Segrè, ZP 1933, 82 748, Goudsmit, PR, 1933, 43 638, Schuler, ZP, 1933, 88 324 Schuler gives a critical survey of the data and recalculates the values

<sup>†</sup> Jones, Phys Soc Proc 1933, 45 625

Jackson and Kuhn, PRS, 1934, 148 335

### 10. The structure of the nucleus

At the present day the evidence of hyperfine structure suffices to divide the nuclei into four types, though history relates that Aston\* recognised these types long before hyperfine structure had advanced far enough to be of much service. The nuclear type is most simply determined by the mass and charge, the crucial question being whether each of these is odd or even (Fig. 20 33).

Nuclear mass	Even	Even	Odd	Odd
Nuclear charge	Even	Odd	Odd Even	
No of isotopes known	114	4	44	45
No of nuclear moments known	>30	3	12	30
Value of $I$	0	1 or 9 0	Half integral	Half integral
No of magnetic moments known	0	2	10	20
Values and sign of $\mu$	No evidence, probably 0		As often $-ve$ as $+ve$ , $\mu < 1$	Always +ve, in all but 4, $\mu > 1$
Structure of nu- cleus suggested		Core + 1 deuton	Core + l neutron	Core + 1 proton

Fig 20 33 Frequency of occurrence of the four nuclear types and their properties

When both mass and charge are even, the nuclear moment is always zero, nothing is then known of the magnetic moment, though it is commonly assumed zero. This structure is particularly stable, Aston's figures showing that more than half the known isotopes are built to this plan.

When the mass is even and the charge is odd, the nucleus is usually unstable, though four light isotopes do occur, the heaviest of these is N<sup>14</sup>. Of the known mechanical moments, two are of magnitude 1 and a third is possibly zero

When the mass is odd and the charge even, the mechanical moment is half an odd integer, the magnetic moment is as often negative as positive, and is always less than one. In terms of the number of isotopes known, this nuclear type is less than half as stable as the even-even type

<sup>\*</sup> Aston, Mass spectra and isotopes, 1933, 175

Finally, when the mass and charge are both odd, the mechanical moment is again half an odd integer, but the magnetic moment is always positive and usually greater than 1. This type of nucleus is about as stable as the preceding type. Further, of ten of these elements, which have two isotopes, nine pairs have the same spin, the one exception, rubidium, is exceptional also in being radioactive. When two isotopes are of even charge, they do not obey this law \*

These facts are independent of any theory of the structure of the nucleus, but to proceed further some simplifying assumptions are necessary A very few years ago, the nucleus was supposed constructed of protons and electrons,† and there seemed no alternative to allotting the proton a spin of  $\frac{1}{2}h/2\pi$  and depriving the electron of the spin it has outside the nucleus But to-day this awkward trick of giving the electron different properties in different places can be avoided by introducing the neutron, and supposing the nucleus built of three bricks only, the proton, the neutron and the a-particle The odd-even rule of mechanical moments is then easily explained if both the proton and neutron have a spin of  $\frac{1}{2}h/2\pi$ , while the  $\alpha$ -particle has no spin at all The band spectra of  $\mathrm{H}^1$  and  $\mathrm{He}^4$  confirm this assignment for they show that these nuclei have respectively moments of  $\frac{1}{2}$  and 0, while the moment assigned to the neutron is that suggested by the quantum mechanics  $\ddagger$  Becoming still more definite, if a nucleus of mass Mand charge Z is composed of N neutrons, P protons and Aα-particles, then obviously

$$M = 4A + N + P,$$
$$Z = 2A + P$$

As these equations are indeterminate, there are current at the present time two simplifying assumptions, the first due to Heisenberg $\S$  eliminates the  $\alpha$ -particles altogether and leaves the

<sup>\*</sup> Schuler and Schmidt, ZP, 1935, 94 460

<sup>1</sup> Bryden, PR, 1931, 38 1989, White, PR, 1931, 38 2073 a

<sup>[</sup> Temple, PRS, 1934, 145 344

<sup>§</sup> Heisenberg, ZP, 1932, 78 156 This theory has been developed by Eastman, PR, 1934, 46 1

nucleus composed of neutrons and protons only, the econd proposed by Iwanenko and used by lande\* does not allow the presence of more than one proton, this one bear present when ever the charge is odd.

For the present purpose, however, the respective ment of these two hypotheses are of little account, for both are consistent with the assumption that the even even nucleus is the core from which the other three types are formed by the addition of a proton, a neutron or a deuton. For convenience we may then describe a nucleus with odd mass and odd charge as protone, one with odd mass and even charge as 'neutronic', and one with even mass and odd charge as 'deutonic'. This hypothese in its simplest form has not thus far been stretched to cover all the facts of hyperfine structure, but it has succeeded so well that secent papers have agreed that some variation is indicated.

Consider first the protonic nuclei of the mechanical and magnetic moments are to be ascribed to a single proton moving outside a core in which both moments are zero, the proton is best assumed to move in an orbit and to have on the account on angular momentum 1, which is always integral, the influent contapin of the proton is then written a with value 3, and this is noted to set parallel or anti-parallel to the orbital vector, so that the result art moment I is half integral. That the magnetic moments are often large suggests that the magnetic moment of the proton is itself large; and in fact Stern! has arrived at the came conclusion from an entirely independent experiment. Working on the deflection of an atomic ray in a magnetic field, he concluded that the magnetic moment of the proton is 21 nuclear magneton, the experimental error being given as 10 per cent., Lande however, mapplying this observation to hypertine structure has found that a g factor of 4 fits the facts better than one of a.

If the proton revolves about a core, the magnetic moment may be calculated by the methods developed by Gondanit for an

<sup>\*</sup> Iwanenko, Comptex Rendus, 1932, 195 439, Lande, PR, 1933, 43 639, 15, a and Landé, 1934, 45 842a.

Landé, PR, 1933, 44 1028a; Kallmann and Schuler, ZP, 1944, 88 249

<sup>|</sup> Storn, Helv. Phys. Acta, 1933, 6 426

electron, the moment will be gI, where the splitting factor g is given by the equation

$$\begin{split} g = & \frac{I\left(I+1\right) + l\left(l+1\right) - s\left(s+1\right)}{2I\left(I+1\right)} g\left(l\right) \\ & + \frac{I\left(I+1\right) + s\left(s+1\right) - l\left(l+1\right)}{2I\left(I+1\right)} g\left(s\right) \end{split}$$

As g(l) is the splitting factor of a revolving particle, its value must be 1, g(s) is assigned the value 4 for reasons already given. The nuclear moments resulting from this system are shown in Fig. 20.34

The experimental moments do not agree very well with this theory, but as no observation can be trusted to less than 10 per cent and the calculations of different authors from the same data

l	<u>}</u>	11/2	$2\frac{1}{2}$	3 <del>1</del>	412
0 1 2 3 4 5	2 0	3 36	4 19	5 °}	6 11

Fig 20 34 Protonic nuclei Magnetic moments dictated by theory

show even wider discrepancies, comparison is not easy (Fig 20 35) The general tendency of the magnetic moments to increase with the spin is well covered by the theory, while if we concentrate attention on the nuclei with a spin of  $1\frac{1}{2}$ , the division into seven elements with magnetic moments greater than 2 and three elements with moments less than 1 is striking and in accord with theory, on the other hand the prediction that for any value of I there can be only two values of  $\mu$  seems definitely at variance with experiment, the range from sodium with an estimated moment of 2 14 to lithium with a moment of 3 29 seems to exceed the possible error, moreover, there is no doubt that the two gallium isotopes have different moments. Ways of circumventing this difficulty will, however, be better taken up when the neutronic nuclei have been considered

Landé\* has pictured the neutronic nuclei built to a similar plan, the mechanical and magnetic moments of the nucleus are due wholly to a single neutron, moving with angular moment 1 and inherent spin s round an inert core, the inherent spin is again

_		3.5		ic moment
Spin	Element	Mass	Obs	Theory
1/2	F Al Tl	19 27 203 205	3 ° 1 93 1 47 1 47	2 or 0
1 <u>1</u>	Li Na K Cu Ga As Rb Au	7 23 39 63 65 69 71 75 87	3 29 2 14 0 38 2 74 2 74 2 14 2 74 0 90 3 06 0 23	3 or 0 60
$2\frac{1}{2}$	Rb Sb	85 121	1 49 2 70	4 01 1 43
31/2	Sb Cs	123 133	2 10 2 91	5 or 2 33
41/2	In Bı	115 209	5 25 3 60	6 or 3 27

Fig 20 35 Protonic nuclei Observed magnetic moments compared with theory

 $\frac{1}{2}h/2\pi$ , but the magnetic splitting factors are different, an uncharged particle will create no magnetic field in its motion so that g(l) will be zero, and the nuclear splitting factor g will be simply

$$g = \frac{I\left(I+1\right) + s\left(s+1\right) - l\left(l+1\right)}{2I\left(I+1\right)}g\left(s\right)$$

That the magnetic moment of a neutronic nucleus is as often negative as positive has been taken to mean that the inherent magnetic moment of a neutron is negative, but it would appear that equal numbers of positive and negative moments appear provided that g(l) is equated to zero, the sign of g(s) is irrelevant

<sup>\*</sup> Inglis and Landé, PR, 1934, 45 842a

Thus if g(s) is assigned the value 1, so that the magnetic moment of the neutron is  $\frac{1}{2}$  a nuclear magneton, the permitted nuclear moments are those shown in Fig 20 36, while if g(s) is given the value -1, the numerical values will be unaltered, but the + and - signs must be interchanged.

ı	1/2	1}	21/2
0 1 2 3	+ 1/2 - 1/6	$+\frac{1}{2}$ $-\frac{3}{10}$	+½ - ½

Fig 20 36 Neutronic nuclei Magnetic moments dictated by theory

That the nuclear moments thus calculated are rather smaller than those observed is of no account, for the neutron may easily be assigned a larger magnetic moment, but the inequality of the positive and negative values is serious, for experiment suggests that positive and negative values occur over the same numerical range, indeed, all observed moments he between  $+\frac{1}{2}$  and +1 or between  $-\frac{1}{2}$  and -1 Clearly these figures are more in conformity with the suggestion that the magnetic moment of the neutron is  $-0.6~\mu$  and can set itself parallel or anti-parallel to the field, there being no orbital motion. Whether the observed moments cover too wide a range actually to invalidate this suggestion is probably still a matter of opinion

In the hope of obtaining better agreement in both protonic and neutronic nuclei, Schuler\* has proposed the introduction of another vector **r**, which shall combine with the resultant of l and s to produce **I**, while Tamm and Altschuler have proposed that in some nuclei two neutrons uncouple from the core, and combine freely with the external proton or neutron. Both authors can claim that the magnetic moments thus calculated nowhere clash with experiment, but both theories give a choice of values, which must be considered rather wide when compared with the paucity

<sup>\*</sup> Schuler, ZP, 1934, 88 323

<sup>†</sup> Tamm and Altschuler, Comptes Rendus de l'Acad de Scr de l'USSR, 1934, 1458

and maccuracy of the experimental figures Inglis and Landé\* have expressed their preference for the solution of Tamm and Altschuler, but where rapid advance is likely in the next few years, a detailed analysis of what is tentative seems hardly justified

Thus the deutonic nuclei alone remain to be considered In these the mass is even and the charge odd, so that both a neutron and a proton must be added to the core of even mass and even charge If these always combine in the same way to form the deuton nucleus of heavy hydrogen, nuclei of this type should always have the unit spin of the deuton itself, N<sup>14</sup> actually has this spin, but Li<sup>6</sup> has always been assumed to have zero spin Whereas the spins of H<sup>2</sup> and N<sup>14</sup> were obtained from band spectra, however, the spin of Li<sup>6</sup> has been obtained only from hyperfine structure and signifies therefore only that if the nucleus has a spin moment its magnetic moment is very small Indeed the lines of N<sup>14</sup> are also narrow, so that all we know of its magnetic moment is that it is certainly less than 0.2 nuclear magneton. Clearly band spectra observations which will determine the nuclear moments of the two deutonic nuclei Li<sup>6</sup> and B<sup>10</sup> are much to be desired

#### BIBLIOGRAPHY

Much the most thorough article is one by Kallmann and Schuler in Erg d Exact Naturuss 1932, 11 134 The treatment is exhaustive, but much has been learnt since 1932

\* Inglis and Landé, PR, 1934, 46 76a

#### CHAPTER XXI

## QUADRIPOLE RADIATION

### 1 Forbidden lines

1

The transition producing a normal line must satisfy two selection rules, Laporte's rule forbids a jump from even term to even term and from odd to odd, and a second limits the changes in the angular momentum of the atom, J On occasion, however, lines appear which violate these rules, in an electric field, for example both rules are violated, the phenomena being referred to as the 'completion of the multiplet' As this has been known for twenty years the more recently discovered forbidden lines have been frequently ascribed to an unsuspected electric field, the precise conditions under which forbidden lines appear are therefore important

For this purpose the forbidden lines may be classified in three divisions (1) the alkali D $\rightarrow$ S doublets, (2) the green aurora line 5577 A and some nebular lines, (3) the mercury line  $^3P_2\rightarrow^1S_0$ , 2270 A Of these the last may be dismissed as probably due to the interaction between the electrons and the nucleus, the J selection rule applying rigidly only to the total angular momentum of the atom F \* The two other divisions ment fuller discussion

The D $\rightarrow$ S lines of sodium and potassium seem to have been studied for the first time in 1922, when Datta† showed that they are absorbed by a tube of potassium vapour, the lines appeared at all pressures used from 2 5 up to 46 mm, while the potassium bands, which are known to be sensitive to electrostatic fields, did not blur until the pressure rose to 30 mm. At about the same time Foote, Mohler and Meggers‡ showed that the D $\rightarrow$ S lines are emitted in a space shielded from the applied electrostatic field, even when the field itself is very weak, though the presence of ions in the vapour may be an essential condition of the experi-

<sup>\*</sup> Rayleigh, PRS, 1927, 117 294, Huff and Houston, PR, 1930, 36 842

<sup>†</sup> Datta, PRS, 1922, 101 539

Foote, Mohler and Meggers, PM, 1922, 43 659

ment, it seems more probable that the lines are both radiated and absorbed in a field-free space. Later the lines were shown to occur also in a newly struck arc,\* the arc was struck and run until the tips of the electrodes were red hot, when caesium carbonate was fused on to both electrodes, thereafter whenever the arc was struck, the  $D \rightarrow S$  lines appeared strong for a few seconds and as they faded, the ordinary caesium lines shone forth

The next forbidden line to attract attention was the auroral line 5577 A, which McLennan† examined and traced to a forbidden transition in the Oi spectrum. As the spectrum of the night sky does not contain any nitrogen bands, the potential necessary to produce the green auroral line is presumably less than the 11.5 volts required to produce the most easily excited of these Experiment in the laboratory confirms this hypothesis, in a discharge tube containing pure oxygen the 5577 A line is swamped by the band spectrum, but if some neon or argon is introduced so that when the total pressure is 3 cm of mercury the partial pressure of the oxygen is only 3 mm, the green line comes out strongly. Now the inert gases are known to have a very small potential drop throughout the discharge, so that the oxygen lines produced when the inert gas is in large excess will be limited to those of low excitation energy.

But if the green line is produced by a potential of less than 11 5 electron volts, the energy which has to be given to the oxygen atom must be less than 4 4 volts, for oxygen can be dissociated into neutral atoms by light of wave-length 1750 A corresponding to a dissociation potential of 7 1 volts, and other evidence serves to confirm this value. The resonance potentials of atomic oxygen are, however, 9 11 volts for  ${}^5S \leftarrow {}^3P$  and 9 48 for  ${}^3S \leftarrow {}^3P$ , so that an excitation energy of 4 4 volts can hardly cause the atom to emit any lines of the triplet or quintet systems. In fact with only this potential available, the terms which can be concerned in the production of the 5577 A line seem to be limited to the five members of the  $p^4$  configuration,  ${}^3P_{2,1,0}$ ,  ${}^1D_2$  and  ${}^1S_0$ 

<sup>\*</sup> Shrum, Carter and Fowler, H W, PM, 1927, 3 27.

<sup>†</sup> McLennan and Shrum, PRS, 1925, 108 501, McLennan, PRS, 1928, 120 327

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Of these low levels <sup>1</sup>D<sub>2</sub> and <sup>1</sup>S<sub>0</sub> are metastable, and if one of them is the initial state, the final state must be <sup>1</sup>S<sub>0</sub> or one of the <sup>3</sup>P components, but even this leaves seven possible transitions To distinguish between them McLennan and his co-workers examined the longitudinal Zeeman effect, and found the two circularly polarised lines characteristic of a singlet line, a result which seems to reduce the seven alternatives to three, namely  ${}^{1}S_{0} \rightarrow {}^{1}D_{2}$ ,  ${}^{1}S_{0} \rightarrow {}^{3}P_{0}$ ,  ${}^{1}D_{2} \rightarrow {}^{3}P_{0}$  Of these the last may be rejected because in nebular spectra which show the transitions  ${}^{1}D_{2} \rightarrow {}^{3}P_{2,1}$ occurring strongly, the  ${}^{1}D_{2} \rightarrow {}^{3}P_{0}$  line is always so weak that it has so far escaped detection, accordingly if the line 5577 A line is  ${}^{1}D_{2} \rightarrow {}^{3}P_{0}$ , two other lines  ${}^{1}D_{2} \rightarrow {}^{3}P_{2,1}$  should occur even more brightly in positions which can be calculated, but in fact these lines do not appear either in the aurora or in oxygen gas excited to produce the 5577 A line A similar argument applied to  ${}^{1}S \rightarrow {}^{3}P_{0}$ transition compels us to reject it too, so that the green auroral line may be taken as  ${}^{1}D_{2} \rightarrow {}^{1}S_{0}$  without any reference to the theory of quadripole radiation, history shows indeed that this evidence was accepted in 1928, though only later was the corner stone added in an observation of the transverse Zeeman effect, work which will be discussed in a later section

While McLennan was developing this work on the auroral line, Bowen\* showed that eight strong nebular lines could be ascribed to transitions between various metastable states of oxygen and nitrogen (Fig. 21.1). Whereas stellar spectra contain lines characteristic of almost all elements, nebulae emit only a few lines and of these all that have been assigned arise from the six elements H, He, C, O, N and A, thus of a list of 79 lines between 3300 and 7300 A, 57 have been assigned to these elements † The lines due to hydrogen and helium are of no particular interest, for they are simply the lines normally produced in the laboratory, but of the lines due to the other elements many are normally forbidden

That lines forbidden in the laboratory should appear in nebulae

<sup>\*</sup> Bowen, N, 1927, 120 473

<sup>†</sup> Becker and Grotman, *EEN*, 1928, 7 56 Anv lines from Boyce, *PR*, 1935, 48 401

is not difficult to explain. The intensity of a line depends both on the transition probability and the concentration of atoms in the excited state, in nebulae a low probability may be balanced by a high concentration, but this is not usually possible in the labora-

Spectrum	Wave-length	Transition	Allowed or forbidden
0 1	6302 6364	$\substack{ 2p^4 \ ^1D_2 \rightarrow 2p^4 \ ^3P_2 \\ 2p^4 \ ^1D_2 \rightarrow 2p^4 \ ^3P_1 }$	f f
Оп	3726 3729 4076 4416 { 4649 7325	$\begin{array}{c} 2p^3  ^2D_{14} \!$	f f a a a a
0 ш	3313 3342 3445 3759 4363 4959 5007	$\begin{array}{c} 2p\ 3p\ ^3S_1\rightarrow 2p\ 3s\ ^3P_1\\ 2p\ 3p\ ^3S_1\rightarrow 2p\ 3s\ ^3P_2\\ 2p\ 3p\ ^3P_2\rightarrow 2p\ 3p\ ^3P_2\\ 2p\ 3p\ ^3D_3\rightarrow 2p\ 3s\ ^3P_2\\ 2p\ ^2\ ^1S_0\rightarrow 2p\ ^2D_2\\ 2p\ ^2\ ^1D_2\rightarrow 2p\ ^2\ ^3P_1\\ 2p\ ^2\ ^1D_2\rightarrow 2p\ ^2\ ^3P_2\\ \end{array}$	a a a f f f
Nπ	5755 6548 6584	$\begin{array}{c} 2p^2  {}^{1}S_0 \longrightarrow 2p^2  {}^{1}D_2  {}^{9} \\ 2p^2  {}^{1}D_2 \longrightarrow 2p^2  {}^{3}P_1 \\ 2p^2  {}^{1}D_2 \longrightarrow 2p^2  {}^{3}P_2 \end{array}$	f f f
N m	4097 4102 4634 4641	$\begin{array}{c} 3p^2P_{11}\!$	a. a. a. a.
A rv	4711 4740	$\begin{array}{c} 3p^3  ^2D_{24} {\rightarrow} 3p^3  ^4S_{1\frac{1}{2}} \\ 3p^3  ^2D_{1\frac{1}{2}} {\rightarrow} 3p^3  ^4S_{1\frac{1}{2}} \end{array}$	f f

Fig 21.1 Nebular lines This list is abstracted from one given by Becker and Grotrian, *EEN*, 1928, 7.56, the original gives lines of hydrogen and helium as well

tory, because atoms leave the excited state by collision. This general explanation has received interesting confirmation in a comparison of the relative intensities of the magnesium lines 2852 and 4571 A \* The first is the line  $2^{1}P \rightarrow 1^{1}S$ , which is very intense in the arc, the second  $2^{3}P_{1} \rightarrow 1^{1}S$ , which is very weak. The natural lives of the atoms in these initial states, calculated by the

<sup>\*</sup> Frayne, PR, 1929, 34 590

methods of the quantum mechanics,\* are 3  $10^{-9}$  and 4  $10^{-3}$  sec respectively, so that if the concentration of the atoms in the two states are at all comparable, the 2 P line will appear much the more intense. In the arc the number of atoms in the 2 3P state is kept down only by frequent collisions, but if the pressure is sufficiently reduced and an mert gas is introduced to prevent the magnesium atoms diffusing to the walls, the 4571 A line should increase in intensity Kinetic theory shows that if the time between successive collisions is to be reduced to  $10^{-3}$  sec, the vapour pressure must be reduced to  $10^{-4}$  mm , and in fact the vapour pressure of magnesium is of this magnitude at 500° C Working with an electrodeless discharge at this temperature Frayne found that the 4571 A line was fairly prominent and that the introduction of 10 mm of various mert gases increased the intensity 50-100 times In agreement with this work the auroral line 5577 A appears only in the presence of an inert gas, and the intensity increases with increase in the diameter of the tube

As a general explanation this hypothesis of Bowen's appears satisfactory enough, but recent theory shows that it may be made much more precise

# 2. Quantum mechanics

The quantum mechanics shows that the ordinary spectral lines arise from a dipole oscillation and that, usually, this alone is important, but mathematically it is only the first term in the series which arises when the vector potential is developed in powers of the atomic radius divided by the wave-length of the emitted light, the second and third terms indicate quadripole and octapole radiation of much lower intensity. Of these the quadripole oscillation will be shown responsible for the forbidden lines described in the last section, no line has yet been attributed to an octapole oscillation.

In agreement with this theory is the low intensity of the quadripole lines. Thus experiments in absorption suggest that 12,000 times as many atoms absorb the  $3^2P \leftarrow 1^2S$  lines of K and Rb as absorb the  $3^2D \leftarrow 1^2S$  lines, the ratio being roughly the

<sup>\*</sup> Houston, PR, 1929, 33 297

same in the two metals,\* while Rasetti,† using a more sensitive method depending on anomalous dispersion, found the intensity ratio of the emitted lines of K to be 1 1  $10^{-6}$ , and as Rasetti estimates his accuracy as only 50 per cent this may be considered in satisfactory agreement with the theoretical value of 1 5  $10^{-6}$  ‡ That the absorption measurements show rather a large error is of little account, for the authors themselves insist that their estimate was intended to be little more than qualitative

The selection rules observed in quadripole lines can be predicted from the simple hypothesis that a quadripole line results from two simultaneous dipole transitions, though this rough analogy is of course a poor substitute for the rigid argument of the quantum mechanics. Thus in a dipole jump the sum of the orbital vectors  $\Sigma l_1$  changes always from odd to even or even to odd, and accordingly in a quadripole jump the same quantity changes from even to even or odd to odd, in particular a quadripole line may be emitted when the jump is between two terms of the same configuration. Again in a dipole line

$$\Delta J = 0$$
 or  $\pm 1$ ,

so that in a quadripole line we expect

$$\Delta J = 0$$
 or  $\pm 1$  or  $\pm 2$ 

And in fact all known lines do satisfy this condition

In practice the quadripole selection rules are not used like the dipole rules to predict which lines will appear, since so few of the lines allowed have yet been produced, rather do they serve to determine whether an observed line arises from a dipole or a quadripole transition, and for this in a field-free space the Laporte rule is crucial, if a transition is known to start from one term and end in another, then it can be written down at once as a dipole or a quadripole But so often one cannot be certain whether there is a stray electric field or not, and then the Laporte rule cannot be trusted, instead one has to examine the Zeeman effect and let it decide

<sup>\*</sup> Sowerby and Barratt, PRS, 1926, 110 190

<sup>†</sup> Rasetti, Accad Lincer, Attr, 1927, 6 54

<sup>‡</sup> Stevenson, PRS, 1930, 128 591

## 3 Zeeman effect

In the Zeeman splitting of quadripole, as of dipole, lines, the term displacements are simple fractions of the Lorentz unit,

$$o_m = \frac{eH}{4\pi m_e c}$$
, so that the change in energy  $\Delta E$  of any state may

be written

$$\Delta E/hc = Mgo_m$$
,

where g has the normal Landé values given by

$$g = 1 + \frac{J(J+1) + S(S+1) - L(L+1)}{2J(J+1)} \bullet$$

But whereas in a dipole line the transitions are governed by the selection rule  $\Delta M \leq 1$ ,

ın quadrıpole lines

$$\Delta M \leqslant 2$$

And the polarisation rules too are different, as the summary given in Fig. 21 2 shows, in particular, when the pattern is viewed at an angle of 45° to the field, components appear which are invisible when the line of sight is parallel or perpendicular to the field

	Polarisation when viewed				
Transition	Across field	Diagonal at 45°	Parallel to field		
$\Delta M = -2$ $\Delta M = +2$ $\Delta M = -1$ $\Delta M = +1$ $\Delta M = 0$	σ σ π π 0	l ell r ell σ σ	0 0 1 circ r circ 0		

Fig 21 2 Quadripole radiation Transitions permitted in a magnetic field and the polarisation of the line produced

Applied to a singlet line, such as the green auroral line, this theory shows that the Zeeman pattern should be that shown in Fig. 21.3, thus when viewed parallel to the field the Zeeman pattern of a dipole and a quadripole line are identical, a fact which explains why McLennan\* was able to confirm the identification of the 5577 A line as due to  $^1D_2 \rightarrow ^1S_0$  before the quadripole theory was developed, though later Frenchs and Campbell† showed that

<sup>\*</sup> McLennan, McLeod and Ruedy, PM, 1928, 6 558, Sommer, ZP, 1928, 51 451

<sup>†</sup> Frenchs and Campbell, PR, 1930, 36 1460

it arises in a quadripole transition, for McLennan viewed the pattern along the field axis, while Frerichs and Campbell viewed it transversely. The latter obtained a beautiful confirmation of theory, finding two  $\pi$  components at a distance of one, and two  $\sigma$  components at a distance of two, Lorentz units, all four lines being of equal intensity (Fig. 21.3)

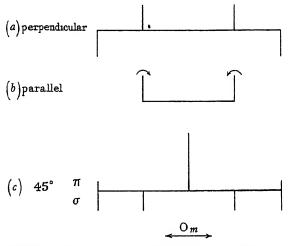


Fig 21.3 Zeeman pattern of a quadripole singlet line, when viewed (a) perpendicular, (b) parallel, (c) at  $45^{\circ}$ , to the field The intensities are proportional to the lengths of the verticals

A more rigorous because more complex confirmation of theory has been obtained by Segrè and Bakker, who measured both the Zeeman and Paschen-Back splitting of SD alkalı doublets,\* and contrasted these with the splitting of the mercury line 3680 A , this line arises as  $7p\,^3P_2\!\to\!6p\,^3P_2$  and is normally forbidden, but it appears in an electric field  $\dagger$ 

The Zeeman effect of the SD doublet was demonstrated with a field of 7500 gauss applied to the potassium lines

$$\begin{array}{c} 4d\ ^{2}D_{2^{1}}\!\rightarrow\!4s\ ^{2}S_{\frac{1}{2}}\ 4642\ 27\ A \\ 4d\ ^{2}D_{1^{\frac{1}{2}}}\!\rightarrow\!4s\ ^{2}S_{\frac{1}{2}}\ 4641\ 77\ A \end{array}\right)$$

with an interval of 2 325 cm  $^{-1}$ 

- \* Segre and Bakker, ZP, 1931, **72** 724
- † Bakker and Segre, ZP, 1932, 79 655

For this doublet the theoretical patterns are

(1) When observed parallel to the field,

$$^{2}D_{2\frac{1}{2}} \rightarrow ^{2}S_{\frac{1}{2}} \quad 4 \quad 8/5$$
 $^{2}D_{1\frac{1}{2}} \rightarrow ^{2}S_{\frac{1}{2}} \quad 1 \quad 7/5$ 

all components being circularly polarised

(2) When observed transverse to the field,

$$^{2}D_{2\frac{1}{4}} \rightarrow ^{2}S_{\frac{1}{4}}$$
 (4) (8) 10 14/5  
 $^{2}D_{1\frac{1}{4}} \rightarrow ^{2}S_{\frac{1}{4}}$  (1) (7) 11/5

The figures in brackets measure  $\pi$  components, the other figures  $\sigma$  components

(3) When observed at an angle of  $\pi/4$  to the field,

$${}^{2}D_{2\frac{1}{2}} \rightarrow {}^{2}S_{\frac{1}{2}}$$
 (2) 4 8 10 14/5  
 ${}^{2}D_{1\frac{1}{2}} \rightarrow {}^{2}S_{\frac{1}{2}}$  1 (3) 7 11/5

The figures in italics are elliptically polarised with an axis ratio of  $\sqrt{2}$  1 between the  $\sigma$  and  $\pi$  axes. The intensities in these simple transitions may be obtained from the polarisation rule and the sum rule of Burger and Dorgelo (Fig. 21.4). Fig. 21.5

		<sup>2</sup> D <sub>1‡</sub> → <sup>2</sup> S		$^{2}D_{2\frac{1}{4}}\rightarrow ^{2}S$		
	М	1/2	11/2	1/2	11/2	21/2
M	qM	2 5	ş	3 5	9 5	3
1	1	- <del>3</del> (2)	1 <sub>5</sub> (1)	$-\frac{2}{5}(3)$	<del>{ t</del> ( <del>1</del> )	2 (5)
]	-1	F (3)	U (4)	- (2)	14 (1)	

Fig. 21.4 The displacements and in brackets the intensities of the Zeeman components of a D $\rightarrow$ S doublet

shows that the experimental results are in complete agreement with theory

The Zeeman effect thus satisfactorily confirmed, Segrè and Bakker changed from potassium to sodium, in which the two lines lie so close together that they were not resolved in the instrument used The pattern should then be (1) 2/1, when observed transverse to the field Experiment confirmed this Paschen-Back effect (Fig. 21 6) though the photographs are somewhat

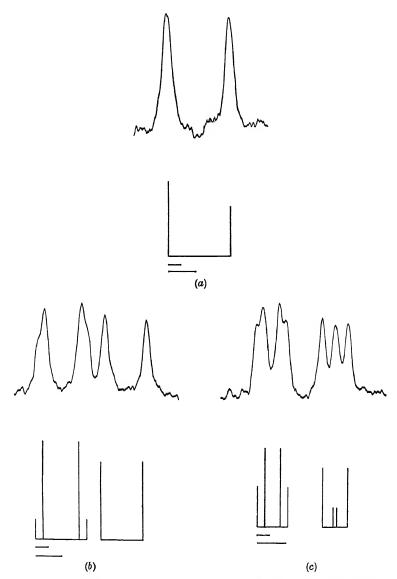


Fig 21.5 The 4642–41 A, D $\rightarrow$ S, doublet of potassium. In each figure the photometer curve appears above and the theoretical splitting below. The intensity scale is arbitrary, but the same in all figures. The  ${}^2D_{2\frac{1}{4}} \rightarrow {}^2S_{\frac{1}{4}}$  line is on the left, and the  ${}^2D_{1\frac{1}{4}} \rightarrow {}^2S_{\frac{1}{4}}$  line on the right. At the foot the scale is shown by two lines of length 0.1 A and 1 cm $^{-1}$ . The three figures show respectively (a) the doublet in the absence of a magnetic field, (b) the  $\sigma$  components viewed perpendicular to a field of 7500 gauss, and (c) the  $\pi$  components viewed from the same direction. (After Segre and Bakker, ZP, 1931, 72.728.)

distorted by the appearance of bands due to the sodium molecule, but if the intensities observed in the absence of a field are compared with those obtained with a field, the lines can be distinguished Not content with these successes the authors measured

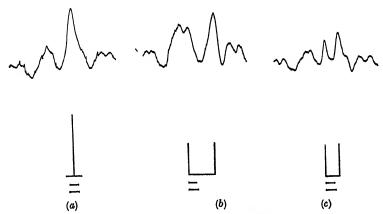


Fig 21.6 Paschen-Back effect in the 3427 A  $3^{\circ}D\rightarrow 1^{\circ}S$ , line of sodium Figure a is taken in the absence of a magnetic field, b and c in a field of 16,100 gauss, b shows the a components viewed perpendicular to the field, a the a components viewed in the same direction. The appearance of the Na<sub>2</sub> bands confuses the pictures a little, but it is the changes which occur between a on the one hand and a and a on the other which are of importance (After Segre and Bakker, aP, 1931, 72 731)

the potassium doublet in an 'intermediate field', the splitting and intensity having been calculated by Millianzuk\* with the help of Darwin's work on the gross Paschen-Back effect. A field of 17,800 gauss was used giving the ratio  $o_m/\Delta\nu$  a value of 0 35, and again satisfactory agreement was obtained

Finally Segrè and Bakker† examined the  $7p^3P_2^{\circ} \rightarrow 6p^3P_2^{\circ}$  line of mercury in order to show that it arises, not as a quadripole transition, but as a dipole conditioned by the electric field. The quantum mechanics makes this probable, for a lough calculation shows that the quadripole term in the radiation of a forbidden line is usually larger than the dipole produced by an electric field, but this is not true when a state with which both levels may com-

<sup>\*</sup> Milianczuk, ZP, 1932, 74 825.

<sup>†</sup> Segrè and Bakker, ZP, 1932, 79 655.

bine lies close to one of them,\* and in mercury the  $7p^3P_2^{\circ}$  term lies at a distance of only 188 cm  $^{-1}$  from the  $6d^3D_2$  term

An electric field modifies the ordinary selection rule, when the pattern is viewed transverse to the magnetic field,  $\pi$  components

M	-2	-1	0	1	2
Mg of 7p <sup>3</sup> P <sub>2</sub> Mg of 6p <sup>3</sup> P <sub>2</sub>	-3 -3	$-\frac{1\frac{1}{2}}{-\frac{1}{2}}$	0	$\begin{array}{c} 1\frac{1}{2} \\ 1\frac{1}{2} \end{array}$	3 3
Pattern if a dipole		(0) (3)	0 3 6	/2	
Pattern if a quadripole		(3)	6/2		

Fig 21.7 Theoretical Zeeman pattern of the 3680 A,  $7p \, ^3P_2 \rightarrow 6p \, ^3P_2$ , line of Hg I, when viewed perpendicular to the magnetic field, if it arises as (a) a dipole transition conditioned by an electric field, (b) a quadripole transition

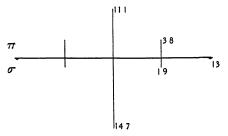


Fig 21 8 Theoretical intensities of the Zeeman components of the 3680 A line of Hg I, if it arises as a dipole in an electric field. The line is viewed transverse to the field. (After Segre and Bakker, ZP, 1932, 79 655)

arise from transitions in which  $\Delta M$  is 0 or  $\pm$  1 and  $\sigma$  components when  $\Delta M$  is 0,  $\pm$ 1 or  $\pm$ 2, so that the pattern should be (0) (3) 0 3 6/2 (Fig 21 7) and intensity calculations show that of these components the undisplaced line is far the strongest (Fig 21 8) In contrast the selection rules of a quadripole line allow  $\pi$  components to arise only when  $\Delta M$  is  $\pm$ 1 and  $\sigma$  components only when  $\Delta M$  is  $\pm$ 2, so that the pattern predicted is (3) 6/2 The photometer curve reveals simply a strong central line, but as there seems no doubt that the resolving power was sufficient to have separated the side components of a quadripole line, this may be taken as proof that the transition is a dipole.

<sup>\*</sup> Huff and Houston, PR, 1930, 36 842.

#### 4 Intensities

Theory has been able to predict the intensities of normal quadripole multiplets,\* but very little has been confirmed by experiment. In part this is due to the difficulty of producing quadripole lines in the laboratory, and in part to the restriction of theory to multiplets arising from Russell-Saunders coupling, a restriction which implies the exclusion of all inter-system lines, no general theory of the latter has yet been developed, so that the intensity of each separate line has to be calculated

#### BIBLIOGRAPHY

There are two important articles, the first by Becker and Grotrian "Uber die galaktischen Nebel und den Ursprung der Nebellinien" in Erg d Exact Naturwiss 1928, 7 8, and the second by Rubinowicz and Blaton on "Die Quadrupolstiahlung" in Erg d Exact Naturwiss 1932, 11 170 The second of these deals with the theory more thoroughly than here

\* Rubinowicz and Blaton, EEN, 1932, 11 176

### CHAPTER XXII

## FLUORESCENT CRYSTALS

## 1 The energy levels of crystals

Though the energy levels of many gases and vapours are now well known, the energy levels of solids are the hills of an unexplored land, for only two routes have yet led to quantitative results, and both of these are of limited value X-ray levels do change from one chemical compound to another,\* but as 15,000 calories correspond to a shift of between 0 1 and 0 01 X unit or 10<sup>-4</sup> of the energy involved, the measurements have to be very accurate The light scattered in the Raman effect,† on the other hand, is accurate enough, but it reveals only certain energy states out of the many which exist

A third route runs through the absorption and fluorescent spectra of crystals, though as yet this has given hardly any quantitative results. At room temperature the lines are blurred by the agitation of the molecules, for the levels of one ion are split by the electric field of the ions which surround it, but the lines sharpen as the temperature is reduced. Much valuable work has been done in liquid air, but Spedding and his co-workers in California are rapidly making this of little more than historic interest by their work in liquid hydrogen.

Many absorption lines are of course due to molecular vibrations, but in the last five years evidence has accumulated to show that in the rare earths and the phosphors of chromium at least, many lines arise as electronic transitions within the atom. This evidence is both simpler and more conclusive in chromium

# 2. Fluorescence and phosphorescence

When a solution of chlorophyll is illuminated with a beam of violet or ultra-violet light, a green band can be seen from all

- \* Siegbahn, Spektroskopie der Rontgenstrahlen, 1931, 278
- † Kohlrausch, Der Smekal-Raman-Effekt, 1931 Placzek, Rayleigh Streuung und Raman-Effekt, 1934 Symposium at Faraday Congress by Raman, Wood, Cabannes and others, Trans Far Soc 1929, 25 781 Dadieu and Kohlrausch, "Raman effect in organic chemistry", JOSA, 1931, 21 286

sides, this is an example of fluorescence Again, in time past luminous paints consisted of impure barium sulphide, if first exposed to sunlight, this remains visible in the dark for some hours, it is said to phosphoresce. Fluorescence is distinguished from phosphorescence by the persistence of the latter after the exciting rays have been extinguished. To-day, however, this distinction does not seem of great importance, it is probably related to the fact that only solids phosphoresce, though solids, liquids and gases may all fluoresce.

In general fluorescence and phosphorescence may both be excited by cathode rays and X-rays as well as by light When light is used, however, the wave-length of the exciting beam must be shorter than the wave-length of the light emitted, this law, discovered in 1853 by Sir George Stokes,\* is simply explained by the quantum theory, energy may be lost between absorption and emission, it cannot be gained This must not be taken to mean, however, that all wave-lengths shorter than those emitted are equally effective, on the contrary, a fluorescent solution or crystal absorbs only certain bands, and these are characteristic of the substance The emission spectrum too is typically independent of the exciting source

Many organic substances, such as quinine sulphate and eosin, fluoresce, but in these the cause is undoubtedly molecular. Of more interest here are the solid phosphors, a group of substances which are conveniently divided under five heads—the phosphors of chromium, the phosphors of the rare earths, the uranyl salts, the Lenard phosphors and the platino-eyanides—The phosphorescence of the first two has recently been shown to originate within the atom, and the evidence deserves detailed consideration. The phosphorescence of the other three may be atomic in origin, but no evidence is yet forthcoming, accordingly they are treated much more briefly.

# 3 Chromium phosphors

Many naturally occurring stones, such as the ruby, sapphire, red spinell, alexandrite and topaz, emit a red fluorescence. This

<sup>\*</sup> Stokes, Roy Soc., Phil Trans., 1853, 142 463, 1853, 143 385

spectrum was thoroughly studied at a time when a ruby was supposed to consist of almost pure aluminium oxide, the odd 1 per cent of chromium oxide being regarded as an unimportant impurity Of recent years however the ruby has been imitated in the laboratory, and the chromium oxide, though present in such a small proportion, has been proved an essential constituent, for without it the aluminium oxide is not fluorescent, while with it the artificial ruby exhibits a spectrum identical with that of the natural stone

In preparing one of the chromium phosphors in the laboratory a few drops of a chromium salt solution are added to the salt of some other metal, such as calcium nitrate, and heated twice to a temperature of about  $1400^{\circ}$  C. The spectrum of this phosphor does not depend on the amount of chromium, though it is brightest with a few parts per thousand present. But the oxide must be an intrusion in the regular lattice of the bedding, mixed crystals of KAl(SO<sub>4</sub>)<sub>2</sub> 12H<sub>2</sub>O and KCr(SO<sub>4</sub>)<sub>2</sub> 12H<sub>2</sub>O show no phosphorescence, whatever the proportions of chromium and aluminium,\* moreover, the  $Cr_2O_3$ , or some molecule which contains it such as  $MgCr_2O_4$ , must be isomorphous with the material in which it is bedded, for Deutschbein has shown that chromium fluoresces in:

$\alpha \mathrm{Al_2O_3}$	which is isom	orphous with	$Cr_2O_3$ ,	bot	h trigonal
MgAl <sub>2</sub> O <sub>4</sub>	,,	,,	MgCr2O4,	,,	regular
$ZnGa_2O_4$	, ,,	,,	$ZnCr_2O_4$ ,	,,	regular
$BeAl_2O_4$	,,	,,	$BeCr_2O_4$ ,	,,	rhombic
MgO beca	ause it forms m	ixed crystals wi	th MgCr.O.		regular

On the other hand, chromium does not fluoresce in

 $\gamma Al_2O_3$  because it is not isomorphous with  $Cr_2O_3$ , the one being regular and the other trigonal,

BeO because it forms no mixed crystals with  $\rm BeCr_2O_4$  , the former being hexagonal and the latter rhombic  $\dagger$ 

That Cr<sub>2</sub>O<sub>3</sub> must be isomorphous with the bedding means presumably that the outer electrons must not be much distorted,

<sup>\*</sup> Deutschbem, AP, 1932, 14 713

<sup>†</sup> Deutschbein, PZ, 1932, 33 874

and in fact the spectrum of the ruby is very sharp and bright, for the  $\rm Cr_2O_3$  molecule fits easily into the  $\alpha \rm Al_2O_3$  lattice. On the other hand, in  $\rm Mg_2TiO_4$  when the distortion is greater, the spectrum is more diffuse, moreover, the unaided eye notices that the phosphorescent light is much weaker

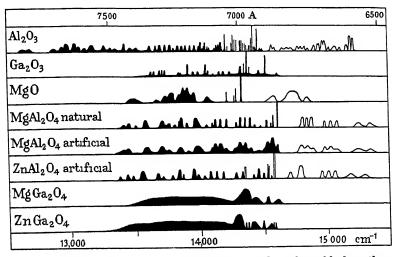


Fig 22.1 Spectra of some chromium phosphors. The lines shown black are those emitted at  $-186^{\circ}$  C, those shown in outline appear in absorption at low temperatures, but in emission only at high temperatures. Comparison of the spectra in  $Al_2O_3$  and  $(4a_2O_3)$ , crystals belonging to the same system, shows that the principal doublet appears in both, but with fivefold greater interval in  $Ga_2O_3$ , the two strongest subsidiary lines are also more widely separated in  $Ga_2O_3$ . The spectra in the regular crystal system—MgO, MgAl<sub>2</sub>O<sub>4</sub>, ZnAl<sub>2</sub>O<sub>4</sub>—show greater symmetry and a much smaller doublet interval, the doublet of MgO being still unresolved. (After Deutschbein, PZ, 1932, 33 876.)

Whether the chromium phosphors are excited by cathode rays, X-rays or ultra-violet light, the spectrum produced is always the same, moreover, the emission spectrum is very like that produced in absorption. In both the lines are easily divided into three groups, first, principal lines, which are intense, sharp and only some half-dozen in number, second, subsidiary lines, which are weaker and more numerous, and third, bands, which are weak and often lie near the lattice bands of the pure bedding. Plate V shows these three in the emission spectrum of chromium bedded

in aluminium oxide, at the short wave-length end of the spectrum lies the principal doublet, which is here some thousand times over-exposed. Then follow on the long wave-length side a few weaker but very sharp subsidiary lines, while beyond again lie some diffuse bands. That this type is general Fig. 22.1 shows

All the chrome phosphors have one or two principal lines in the red, while several exhibit also a group of three lines in the blue (Fig 22 2) Moreover, examination of a series of alums of the

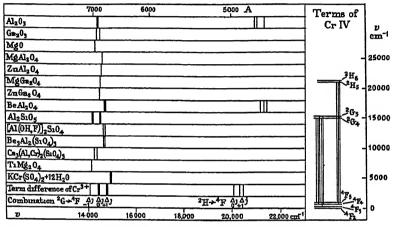


Fig 22.2 Principal emission and absorption lines of some chrome phosphors compared with the term differences of Cr IV (After Deutschbein, PZ, 1932, 38 877)

types  $RCr(SO_4)_2$   $12H_2O$  and  $RCr(SeO_4)_2$   $12H_2O$ , where R is variously K, Rb, Tl and  $(NH_4)$ , shows that in liquid air all absorb a strong doublet near 6700 A. (Fig. 22.3) \* Other chromium compounds are not of course so regular as these, but most show line absorption † The frequencies of these lines, and especially of the phosphorescent lines, are comparable with term differences found in an analysis of the Cr iv spectrum, in this the 3d³ configuration produces a  $^4F$  ground term and above it metastable  $^2G$  and  $^2H$ 

<sup>\*</sup> Sauer, AP, 1928, 87 197

<sup>†</sup> Snow and Rawlins, Camb Phil Soc Proc 1932, 28 522, Joos and Schnetzler, Z Phys Chem 1933, B, 20 1 A paper on  $KCr(SO_4)_2$  12 $H_2O$  by Spedding and Nutting, J Chem Phys 1934, 2 421, appeared after this section was written

terms, in the vapour these terms do not combine, but in the phosphors the mechanism is probably not a pure dipole, so that

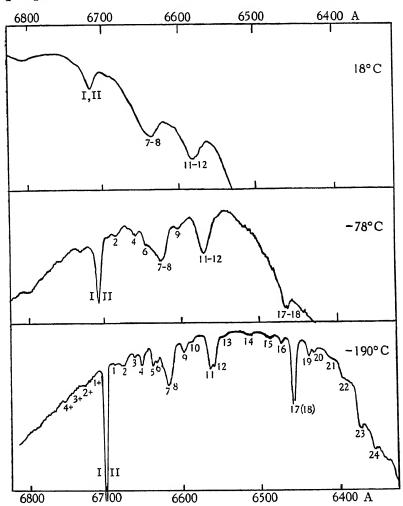


Fig 22.3 Absorption curves of RbCr(SeO<sub>4</sub>)<sub>2</sub> 12H<sub>2</sub>O at 18, - 78 and  $-190^{\circ}$  C Crystal thickness about 4 mm (After Sauer, AP, 1928,  $\bf 87$  219 )

the transitions may reasonably be allowed At any rate, Fig 22 2 shows that the frequencies agree so remarkably that the identification can hardly be doubted, the red principal lines are there

shown to arise in the  ${}^2G \rightarrow {}^4F$  transition and the blue lines in  ${}^2H \rightarrow {}^4F$ ,\* the precise transitions to which the individual lines are to be assigned are not yet clear, but as the doublet of chrome alum is still strong at  $-195^\circ$  and is not fading out, the two highest levels of the ground term,  ${}^4F_{4\frac{1}{2}}$  and  ${}^4F_{3\frac{1}{2}}$ , lying at 950 and 550 cm  $^{-1}$  above  ${}^4F_{1\frac{1}{2}}$ , may be reasonably excluded. The Boltzmann distribution would allow very few atoms in these states at so low temperature, and the law so admirably explains the fading of certain lines in samarium that it can hardly be in error †

Like the principal lines, the subsidiary do not change greatly when the temperature is reduced from 20° to -195°C, they grow rather sharper, and the whole spectrum has its wave-length reduced by a few angstroms, t but they do not otherwise change much in position or intensity They appear both in phosphorescent and absorption spectra, but they occupy very different positions in different beddings, the positions, however, are characteristic of the crystal lattice, not of the amon, indeed with practice the lattice type can be recognised from the look of the spectrum This would seem to suggest that the subsidiary lines are Stark components produced by the electric fields of the ions in the crystal lattice, but if the atomic states are split by a strong electric field all components should be Stark components, and it is not easy to see why the half-dozen lines should be so much stronger than any others Again, is it mere chance that nearly all subsidiary lines are of shorter wave-length than the principal lines? One might assume that some Cr<sub>2</sub>O<sub>3</sub> molecules are lumped together, and that these produced different lines to those spread evenly through the bedding of say Al<sub>2</sub>O<sub>3</sub>, but if the fields of Cr<sub>2</sub>O<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> are different, as is probable, we should expect all fields from that characteristic of Cr2O3 to that characteristic of Al<sub>2</sub>O<sub>3</sub>, and then the lines would be diffuse not sharp, accordingly one must suppose the Cr<sub>2</sub>O<sub>2</sub> molecules spread evenly through the Al<sub>2</sub>O<sub>3</sub> lattice like currants in a cake. The electric field is then effectively that of the Al<sub>2</sub>O<sub>3</sub> lattice

<sup>\*</sup> Deutschbein, ZP, 1932, 33 877

<sup>†</sup> Spedding, PR, 1933, 43 143a

<sup>‡</sup> Deutschbein, AP, 1932, 14 720

The bands are considerably more complicated than either the principal or the subsidiary lines, for they are not the same in emission and absorption, and grow more complex if the temperature is raised At low temperatures, however, the emission spectrum consists only of a long wave-length band lying in the red and infra-red, while the absorption spectrum consists of a short wavelength band lying in the blue If the principal lines, which lie between these two bands, are unaltered electron transitions, and the bands conform to Stokes's law, these facts are easily explained, the absorption bands must be on the high-frequency side of the principal lines, and the emission bands on the low-frequency side \* At room temperature emission still occurs chiefly in the red and infra-red, but some diffuse bands appear on the violet side of the principal lines, these short-wave or 'anti-Stokes' bands must be emitted by molecules passing from an excited state to one of low energy, so that their intensity should be proportional to the number of molecules in the excited state, this number is determined by the Boltzmann law and decreases rapidly with decrease of temperature Again, in the absorption spectrum there appear at room temperature bands of wave-length longer than the principal lines, these anti-Stokes absorption bands can be explained in the same way as the anti-Stokes emission bands, they are due to absorption by molecules which are already in an excited state †

The frequencies of some of the stronger bands are also of interest. The Raman spectrum of pure  $\alpha Al_2O_3$  reveals a lattice frequency of 417 cm<sup>-1</sup>. Now in the emission spectrum of a ruby, the principal doublet and a strong band he at 14,416 and 14,006 cm<sup>-1</sup> respectively, thus in the phosphor a band occurs with a frequency difference slightly less than that of pure  $Al_2O_3$ , 410 instead of 417 cm<sup>-1</sup>. This relationship is not uncommon in the chrome phosphors, and is accounted due to a decrease in the lattice frequency caused by the introduction of the chromium oxide molecules \*

<sup>\*</sup> Dcutschbein, ZP, 1932, 77 490

<sup>†</sup> For the effect of a magnetic field on the lines of a ruby Du Bois and Elias, AP, 1908, 27 233, 1911, 35 617, Du Bois, PZ, 1912, 13 128.

# 4 Rare earth phosphors

As long ago as the eighties of last century Crookes\* showed, during the course of his pioneer work on high vacua, that when rare earth minerals are irradiated with cathode rays, they emit a strong phosphorescent spectrum, but his work is only of historic interest, because very few of his rare earth preparations were pure. More recent work shows that salts, which are colourless like those of lanthanum, gadolinium and ytterbium, exhibit no after-glow, but the smallest trace of active impurity makes the substance phosphorescent, 4 10<sup>-6</sup> gm of samarium in 1 gm of calcium oxide is sufficient to produce a red after-glow, while the spectrum is brightest if the active earth is present in a proportion of only 1 per cent, thus the smallest trace of dysprosium in yttrium, or of terbium in gadolinium, can easily be detected †

Naturally occurring fluorites too have long been known to exhibit blue, yellow and green fluorescence, when excited with radium, but little progress was made until synthetic calcium fluoride was used and 1/10 per cent of a rare earth added. Then it was shown that the blue band appears only when europium is present, and the yellow-green band only when ytterbium. The active agent of the red band has not yet been traced, all other rare earths are mactive. As europium and ytterbium are the two rare earths which most readily become divalent, and the fluorescence may be excited by heating the activated fluorite in a reducing flame, the transition from tri- to divalent form is clearly linked with the fluorescence §

Of all the rare earth phosphors, samarium has been most thoroughly studied (Fig 22 4), as elsewhere the spectrum is much the same if excited by ultra-violet light instead of by cathode rays. The lines are somewhat sharper than those of the chromium phosphors, especially at room temperature, while at low temperatures even naturally occurring fluorspar emits lines which are as sharp as the D lines of a flame poor in sodium || Again lare

<sup>\*</sup> Crookes, Chem Soc J 1889, 55 255

<sup>†</sup> Urbain, Chem Rev 1924, 1 167

 $<sup>\</sup>ddagger$  Jantsch and Klemm, Z f anorg und allgem Chemie, 1933, 216 80

<sup>§</sup> Haberlandt, Karlık and Przibram, Akad Wiss Wien, Ber 1934, 143 151

<sup>||</sup> Tomaschek, AP, 1927, 84 329, 1047

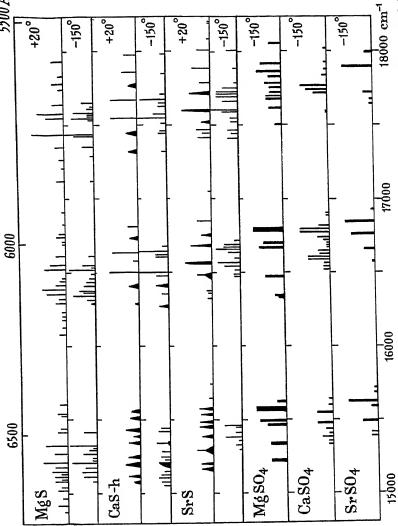


Fig. 22 4 Phosphorescent spectra of samanum bedded in various sulphides and sulphates (After Tomaschek, AP, 1928, 84 374, 382)

earth compounds need not be isomorphous with the bedding, and this can very probably be related to the sharpness of the lines. In contrast to the chromium phosphors, however, a phosphorescent spectrum of the rare earths is usually much more complicated than the absorption spectrum \* This may be ascribed to two causes, first absorption lines all arise in levels less than 500 cm<sup>-1</sup> above the ground term, but emission lines may end in much higher levels, and second all absorption lines arise in atomic transitions,

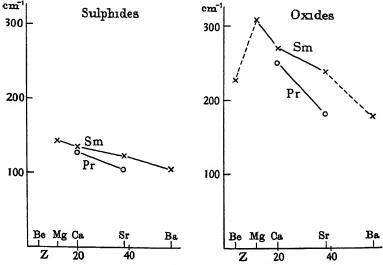


Fig 22.5 Term displacements of samarium and praseodymium phosphors, when bedded in the sulphides and oxides of the alkaline earths. The heavier the rare earth and the smaller the diameter of the alkaline earth atom, the greater the displacement (After Tomaschek, PZ, 1932, 33 878)

while some emission lines arise in the rare earth molecule and others in the lattice of the bedding

In the rare earth phosphors the vibrations of the bedding lattice are rather slower than those calculated for the pure crystal, and this is significant for the rare earth molecules may be supposed to act as mert loads. If this explanation is correct, the change of frequency should be greater the larger the rare earth and the smaller the bedding molecule, these predictions experi-

<sup>\*</sup> Spedding, PR, 1933, 43 143a

ment confirms The praseodymium ion has a diameter 3 per cent greater than the samarium ion, and the change of frequency is slightly greater, barium oxide has a larger diameter than calcium

em <sup>-1</sup>	16,000	17	,000	18,000	α	A-X	Type
Mg0		1	1		4 21	2 10	
Ca0		1 1	1		4 80	2 38	
Sr0		ا. ، ا	1	,1	5 15	2 59	1de
Ba0		1	ال ،	1,	5 50	2 77	chloride
MgS		11	1	1	5 19	2 52	
CaS		11			5 69	2 80	Sodium
SrS		11		11	6 01	3 00	So
BaS		انا			6 37	3 18	
CaF <sub>2</sub>		J I,			5 45	2 36	
SrF <sub>2</sub>		1			5 78	2 50	بو
BaF <sub>2</sub>		1 1			6 19	2 68	Fluorite
$ZrO_2$	1	111.	11 .		5 10	2 21	Fla
CeO <sub>2</sub>		١,	1		5 40	2 34	
Th0	2	 			5 57	2 42	
$Al_20_2$	11		. 1		5 15	1 84 1 99	Corun-
Ga <sub>2</sub> O	3	1	. 1		5 28		ပြင်
$L_{12}SQ$	4	11					
CaSO		11					
SrSO	4			, Ì	1		
BaSC	24						
λ	620	0 6000	5800	5600 A			

Fig 22.6 The two short wave line groups of some samarium phosphors arranged by the crystal type of bedding  $\alpha$  is the lattice constant and A-X the distance between the electropositive and electronegative centres in the lattice, both are in angstroms (After Tomaschek, PZ, 1932, 33 880)

oxide, and the change of frequency produced by bedding samarium in it is much less (Fig  $\,$  22 5) \*

Though in their general features the spectra of samarium in

<sup>\*</sup> Tomaschek, PZ, 1932, 33 878

different beddings are similar, a closer examination reveals many differences. Thus in Fig. 22.6 a series of spectra are arranged according to their crystal types, the figures alongside being the lattice constant a and the distance between the positive and negative ions, both in angstroms. The crystal type is here revealed as an important influence, but in fact this is clearer still in the original photographs,\* for in them a practised eye can recognise the crystal type at a glance  $\dagger$ 

With so few principal lines in the samarium emission spectrum, one naturally asks whether they may not be interpreted, like the principal lines of the chromium phosphors, as electronic transitions within the ion As the spectrum of samarium vapour has not been analysed, the way is by no means clear, but the fact that the rare earths do not have to be isomorphous with their bedding, suggests that the outer electrons can hardly be concerned, rather are the transitions likely to occur between different terms of the  $4f^n$  configuration, the brightest lines arising between terms of the same multiplicity If transitions between the  $4f^n$  and  $4f^{n-1}$  5d configurations are responsible for some lines, as Laporte has suggested, they are likely to be much more diffuse than the lines arising within the  $4f^n$  configuration, indeed it is tempting to identify a diffuse spectrum, photographed beside the sharp one by Fagerberg in neodymium and by Tomaschek‡ in samarium, with these predicted lines

Assuming that the principal lines arise within the  $4f^n$  configuration, their positions can be calculated by the method which Goudsmit developed § This method gives the extreme intervals of the various terms, if the coupling is Russell-Saunders, and the individual terms can then be interpolated with the interval rule. The calculations are laborious, but the results are eminently satisfactory, especially in praseodymium, whose emission spectrum has been recently measured by Evert || The lines shown in

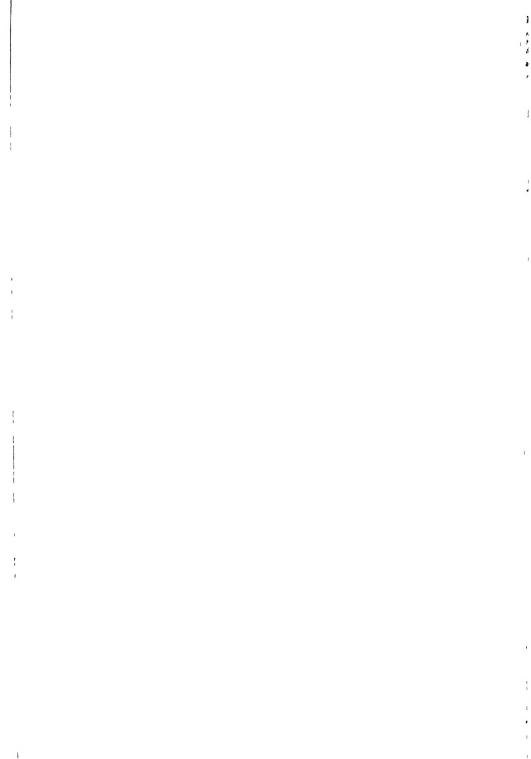
<sup>\*</sup> Photographs, AP, 1927 84 Taf IX-XI Cf Z Elect 1930, 36 737

<sup>†</sup> Tomaschek, PZ, 1932, 33 879.

<sup>‡</sup> Tomaschek, PZ, 1932, 33 882

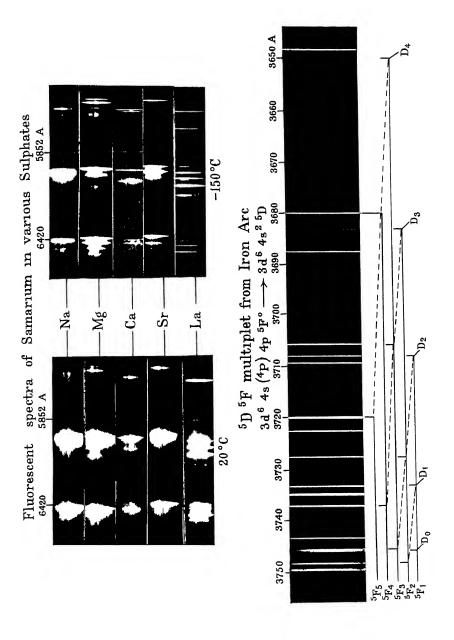
<sup>§</sup> Goudsmit, PR, 1928, 31 948, and chapter xviii of this book

<sup>||</sup> Evert, AP, 1932, 12 144



#### PLATE VIII

- 1 Fluorescent spectra of samarium bedded in various sulphates at 20 and  $-150^{\circ}$  C At room temperature the lines are so blurred that the photographs do little more than show that the positions of the multiplets are independent of the bedding, but they sharpen as the temperature is reduced The samarium lines are much sharper in La<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> than in any other bedding, probably because lanthanum like samarium is trivalent (After Tomaschek, AP, 1927, 84, Taf X, XI)
- 2 DF quintet from the iron arc. This multiplet arises as 3d6 4s (4P) 4p  $^5F^\circ \rightarrow 3d^6 4s^2 ^5D$  (Lent by Prof. H. Dingle.)



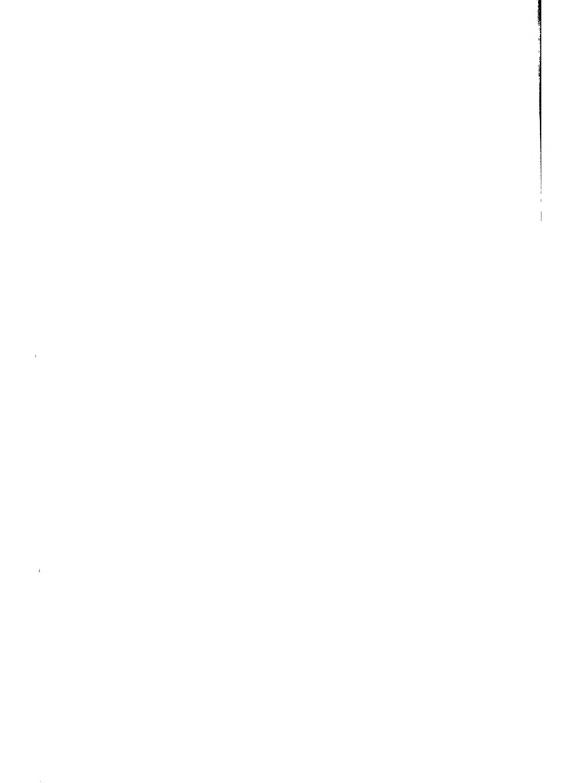


Fig 22.7, taken from left to right, arise in transitions between the following values of J

for 
$${}^{3}F\rightarrow {}^{3}H$$
 4-6, 3-5, 2-4, 4-5, 3-4, 4-4, for  ${}^{1}G\rightarrow {}^{3}H$  4-5, 4-4

Since quadripole transitions are probable, J has been allowed to change by two units. These predictions are compared with the phosphorescent spectrum of the metal plotted above the line, and the absorption spectrum plotted below

Besides praseodymium satisfactory agreement is obtained in neodymium and erbium, spectra arising from 3 and (14-3) electrons respectively. In samarium only the terms of highest multiplicity have yet been calculated, for when there are five electrons the work becomes very heavy, but the  ${}^6{\rm F} \rightarrow {}^6{\rm H}$  transition accounts apparently for three strong lines in the infra-red

# 5 Uranyl salts\*

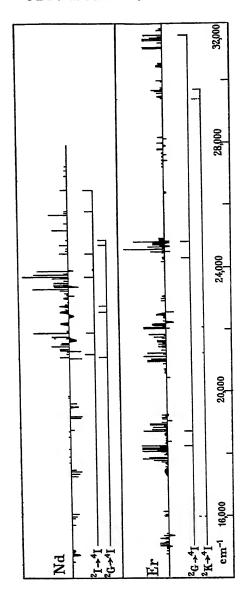
Like the rare earths the uranyl salts are fluorescent in their own right, and are not dependent on the crystal in which they happen to be embedded, but fluorescence is a property of the uranyl radical  $\mathrm{UO}_2$ , not of the uranium atom, for salts in which uranium is quadrivalent do not fluoresce. On the other hand the absorption spectra of all uranium compounds are so similar, that the uranyl radical cannot be considered peculiar in the energy it absorbs, but only in re-emitting some of this energy as visible light

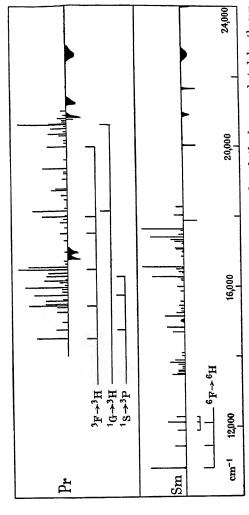
At room temperature and viewed in a spectroscope of low resolving power, both the fluorescent and absorption spectra of uranyl salts consist of bands. In the emission spectra some seven or eight bands appear in the yellow and red, while in absorption a smaller number appear in the green and blue, the emission band of shortest wave-length coincides with the longest absorption band. The emission bands are equally spaced in the scale of frequency, the interval varies a little from salt to salt, but is never far from 830 cm<sup>-1</sup> Again, all emission bands show the same variation in intensity, but the intensity distribution in absorption bands is quite different (Fig. 22.8)

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<sup>\*</sup> Pringsheim, Fluorescenz und Phosphorescenz, 1928, 238, Nichols and Howes, The fluorescence of the uranyl salts, Carnegie Institute Publication, 1919, No 298





Above the line is the phosphorescent spectrum when bedded in CaO, below, the absorption of salts in Fig 22.7 Multiplets of some rare earth phosphors compared with the lines predicted by theory solution (After Tomaschek, PZ, 1932, 33 883)

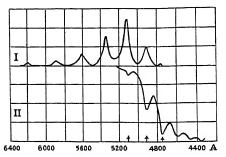


Fig 22.8 Spectra of uranyl potassium sulphate at  $25^{\circ}$  C I, the fluorescent spectrum showing the intensity increasing towards the blue, II, the absorption spectrum showing the intensity decreasing towards the blue. The three marked with arrows appear in both emission and absorption (After Pringsheim, Fluorescenz und Phosphorescenz, 1928, 241)

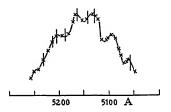


Fig 22.9 Structure of a single fluorescent band of uranyl sulphate. The curve gives the intensity at room temperature, the lines are those observed at  $-185^{\circ}$ C (After Pringsheim, Fluorescenz und Phosphorescenz, 1928, 243, and Wick, PR, 1918, 11 126)

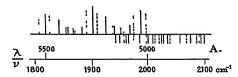


Fig 22 10 Spectra of uranyl potassium chloride at  $-186^{\circ}$  C The fluorescent lines are shown above the horizontal, the absorption lines below The lines are polarised parallel and perpendicular to the principal axis of the crystal, the ordinary spectrum is shown by full and the extraordinary by dotted lines. The lengths of the lines indicate intensities (After Pringsheim, Fluorescenz und Phosphorescenz, 1928, 243)

At low temperatures high resolution splits these bands into a number of components, indeed in liquid hydrogen, at 20°A, many lines are as fine as the lines of a spark spectrum (Fig 22 9) But rather curiously even these sharp lines show no trace of broadening in a magnetic field of 2500 gauss. In both emission and absorption spectra many lines are polarised parallel or perpendicular to the principal axis, in Fig 22 10 these lines are represented by continuous and dotted lines respectively, and their different positions show that when the phosphorescent spectrum is viewed through a nicol prism, two entirely different spectra appear as the nicol is rotated

The spectra of the uranyl salts resemble those of chromium sufficiently closely to make one wonder whether the frequencies of the strong lines are not equally significant, but as yet none of the higher spark spectra of uranium has been analysed

# 6 Lenard phosphors

Many phosphorescent compounds, whether occurring naturally as minerals or artificially produced, consist of a crystalline salt carrying a trace of some other substance which will not fit into the crystal lattice, the intruding substance is commonly a metal, and the greater number of these phosphors may be regarded as members of a family of which the alkaline earth sulphides activated by a heavy metal may be considered the prototype. Having been exhaustively studied by Lenard and his school, they are commonly known as Lenard phosphors

As the intruding metal seems responsible for the fluorescence, one might have hoped for a line spectrum, instead of the broad bands actually observed, though as many workers have used spectroscopes of low resolving power combined with a slit 1 mm wide the evidence is not so extensive as could be desired. When a substance exhibits several bands these often behave independently when a change is made in the wave-length of the exciting light or in the temperature, some bands fade and others grow brighter. Further, the positions of the bands change when either the active element or the bedding is changed.\*

<sup>\*</sup> Pringsheim, Hb d Phys 1929, 21 600

Like the Lenard phosphors the platino-cyanides phosphoresce only when bedded in some mert material, neither the pure salts nor their solutions are themselves phosphorescent, but the phosphorescence appears so regularly that it has been attributed to the platino-cyanide molecule in the absence of other evidence. The details of the emission spectra depend largely on the crystal type, and change when water of crystallisation is added. The polarisation depends on the polarisation of the incident light

At room temperature the emitted light lasts a very short time, but if a body at  $-250^{\circ}$  C is illuminated, it phosphoresces only when allowed to warm up. In this the platino-cyanides are like the Lenard phosphors

#### BIBLIOGRAPHY

The most thorough study of the older work is Lenard, Schmidt u Tomaschek, "Phosphorescenz und Fluorescenz", Handbuch der Experimental Physik, 1928, 23 This fills two large volumes, briefer summaries have been provided by Pringsheim, Fluorescenz und Phosphorescenz, 1928, Pringsheim, "Luminescenzspektra", Handbuch der Physik, 1929, 21 574

The newer work of Spedding, Tomaschek and Deutschbein, with which this chapter is chiefly concerned, does not seem to have been written up

#### APPENDIX V

# KEY TO REFERENCES

The periodicals, in which most papers appear, I have cited by the capitals introduced by Gibbs, the less common by the usual abbreviations A key to the former is given here, a key to the latter may be found in *Science Abstracts* 

AJ Astrophysical Journal AP Annalen der Physik

BSJ Bureau of Standards, Journal of Research
EEN Ergebnisse der Exacten Naturwissenschaften
JOSA Journal of the Optical Society of America

N Nature

Nw Naturwissenschaften PM Philosophical Magazine

PR Physical Review

PRS Proceedings of the Royal Society, London, series A

PZ Physikalische Zeitschrift ZP Zeitschrift fur Physik

An author s initials are not given in the text unless two authors of the same name occur, but all authors are given their initials in the index

### APPENDIX VI

# BIBLIOGRAPHY

The bibliography is divided into three sections

- A Books of reference
- B Spectra of the elements
- C Hyperfine structure of the elements

In the last two sections I follow Bacher and Goudsmit in arranging the elements in the alphabetical order of their chemical symbols

# A Books of reference

The following books are frequently needed for reference, because they contain experimental data conveniently arranged. Books dealing with a particular subject are discussed at the end of the chapter on that subject

- 1 Gibbs, J C 'A complete bibliography of individual spectra for the years 1920–1931' Rev Mod Phys 1932, 4 278
- 2 Bacher, R F and Goudsmit, S Atomic energy states, 1932 The terms of all known spectra, but no wave-lengths
- 3 Kayser, H and Konen, H Handbuch der Spektroskopie, vol viii, 1932 A complete review of the first nineteen elements in alphabetical order, that is A, Ag, Al, As, Au, B, Ba, Be, Bi, Br, C, Ca, Cd, Ce, Cl, Co, Cr, Cs, Cu Wavelengths, terms, magnetic splitting factors and hyperfine structure are all given with a bibliography
- 4 Grotrian, S Graphische Darstellung der Spektren von Atomen mit ein, zwei und drei Valenzelektronen, 1928 The energy diagrams of vol II show the transitions which produce all the strong lines
- 5 Fowler, A Report on series in line spectra, 1922 Paschen, F and Gotze, R Seriengesetze der Linienspektren, 1922 Both books contain lists of terms and lines for the elements of the first three columns

# B The spectra of the elements

These lists are select, where one paper provides a satisfactory summary, earlier papers are not cited. The papers deal chiefly with the analysis into systems of terms, but papers on intensities and the Zeeman effect have been included when they deal with a particular spectrum.

When one of the books of reference, Kayser and Konen, Grotrian and Fowler, deals with a spectrum, I have included the author's name in the bibliography, as these sources are too easily overlooked

The abbreviations are those used in the text.

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# A Argon 18

A Kayser and Konen

A I Meissner, ZP, 1926, 39 172, 40 839 Terms and lines
Dorgelo and Abbink, ZP, 1927, 41 753 Extension in ultra-violet
Gremmer, ZP, 1928, 50 716 Extension in infra red
Rasmussen, Nw, 1930, 18 1112 Bergmann series
Terrien and Dijkstra, J de Phys 1934, 5 443 Zeeman effect
Pogány, ZP, 1935, 93 364 Zeeman effect
Boyce, PR, 1935, 48 396 Extreme ultra-violet

A II Compton, Boyce and Russell, PR, 1928, 32 179 Extreme ultra-violet Bakker, de Bruin and Zeeman, ZP, 1928, 51 114, 52 299, K Akad Amsterdam, 1928, 31 780 Zeeman effect de Bruin, ZP, 1930, 61 307, K Akad Amsterdam, 1930, 33, 198 Complete term scheme and lines

Boyce, PR, 1935, 48 396 Extreme ultra-violet

A m Keussler, ZP, 1933, 84 42 Lmes and terms Boyce, PR, 1935, 48 396 Extreme ultra-violet Boyce, PR, 1936, 49 351 Intersystem lines

A IV Boyce and Compton, Proc Nat Acad Sci 1929, 15 656 Lines and terms Boyce, PR, 1935, 48 396 Extreme ultra-violet

# Ag Silver 47

Ag Kayser and Konen

Ag I Fowler Grotrian

Blair, PR, 1930, 36 1531 Extension of series

Ag II Shenstone, PR, 1928, 31 317 Terms and lines Blair, PR, 1930, 36 173 Two new terms Gilbert, PR, 1935, 47 847 High terms

Ag III Gilbert, PR, 1935, 47 847 Lines and terms

#### Al Aluminium 13

Al Kayser and Konen

Alı Fowler Grotrian

Al II Sawyer and Paschen, AP, 1927, 84 1 Terms and classified lines Ekefors, ZP, 1928, 51 471 New ultra-violet lines

Al III Paschen, AP, 1923, 71 152 Terms and lines Ekefors, ZP, 1928, 51 471 New terms

Al IV Edlén and Ericson, Comptes Rendus 1930, 190 116, 173 Resonance lines

Al v Ibid

# Al vi Ibid As Arsenic 33

As Kayser and Konen

As I Meggers and de Brum, BSJ, 1929, 3 765 Lines and terms Rao, K R, PRS, 1929, 125 238 Lines and terms Rao, A S, Proc Phys Soc 1932, 44 243

As II Rao, A S, Proc Phys Soc 1932, 44 343

As III Lang, PR, 1928, 32 737 Series Rao, K. R., Proc. Phys. Soc. 1931, 43 68 Series

As IV Sawyer and Humphreys, PR, 1928, 32 583

As v Ibid

As Arsenic 33 (cont)

As vi Borg and Mack, PR, 1931, 37 470 Series

Au Gold 79

Au Kayser and Konen

Au I Grotman

McLennan and McLay, PRS, 1926, 112 95 Terms and lines Symons and Daley, Proc. Phys. Soc. 1929, 41 431 Zeeman effect

Au II McLennan and McLay, T Roy Soc Canada, 1928, 22 103 Terms and lines

Sawyer and Thompson, PR, 1931, 38 2293 Ground term Mack and Fromer, PR, 1935, 48 357 Pt 1 130electronic sequence

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#### B Boron 5

B Kayser and Konen

Br Bowen, PR, 1927, 29 231 Terms and lines Smith and Sawyer, JOSA, 1927, 14 287 Series

BII Bacher and Goudsmit, 1932 Terms from unpublished material

B m Ibid

Edlén, ZP, 1931, 72 763 Ground term

B IV Edlén, N, 1931, 127 405

Ba Barium 56

Ba Kayser and Konen

Ba I Fowler Grotman Russell and Saunders, AJ, 1925, 61 38

Ba II Fowler Grotrian Rasmussen, ZP, 1933, 83 404 New terms

Be Beryllium 4

Be Kayser and Konen

Be I Paschen and Kruger, AP, 1931, 8 1005 Series extended

Be m Ibid

Be III Edlén and Erroson, ZP, 1930, 59 656 Series Edlén, N, 1931, 127 405

Be rv Edlén and Ericson, ZP, 1930, 59 656 Edlén, N, 1931, 127 405

#### B<sub>1</sub> B<sub>1</sub>smuth 83

B<sub>1</sub> Kayser and Konen

Bi I Thorsen, ZP, 1926, 40 642 Terms and lines
 Toshniwal, PM, 1927, 4 774 Terms and lines
 Zeeman, Back and Goudsmit, ZP, 1930, 66 1 Interpretation of low terms Zeeman effect

Bi II McLennan, McLay and Crawford, PRS, 1930, 129 579 Series

Bi III Lang, PR, 1928, 32 737 Series

Bi vi Mack and Fromer, PR, 1935, 48 357 Pt i isoelectronic sequence

Br Bromme 35

Br Kayser and Konen

Br I Kiess, C C and de Bruin, BSJ, 1930, 4 667 Lines and terms

Br II Deb, PRS, 1930, 127 197 Series

Br m Ibid

Br Bromme 35 (cont )

Deb, PRS, 1930, 127 197 Series Br TV

Br v Ibid

#### C Carbon 6

Kayser and Konen  $\mathbf{C}$ 

Hopfield, PR, 1930, 35 1586 Ionisation potential Ст Paschen and Kruger, AP, 1930, 7 1 Terms and lines Birkenbeil, ZP, 1934, 88 1 Extension in infra-red

Fowler and Selwyn, PRS, 1928, 120 312 Terms and lines Сп Bowen, PR, 1931, 38 128 Edlen, ZP, 1935, 98 561 New terms

Bacher and Goudsmit, using unpublished material CmBowen, PR, 1931, 38 128 Extension and revision of series Edlén, ZP, 1931, 72 559 Series

Edlén and Stenman, ZP, 1930, 66 328 Teim system C  $\mathbf{r}\mathbf{v}$ Bacher and Goudsmit, using unpublished material

# Ca Calcium 20

Kayser and Konen Ca

Fowler Grotrian Сат Russell and Saunders, AJ, 1925, 61 38 Displaced terms Back, ZP, 1925, 33 579 Zeeman effect Russell, AJ, 1927, 66 191 New terms

Fowler Grotrian Сап Saunders and Russell, AJ, 1925, 62 1 Terms and lines Russell, AJ, 1927, 66 283

Bowen, PR, 1928, 31 497 Ca III

Ca rv Ibid

#### IbidCa. v

# Cb Columbium 41

Meggers, J Wash Acad Scr 1924, 14 442 Zeeman effect Cbr Meggers and Kiess, C C, JOSA, 1926, 12 417 Lines and terms King and Meggers, PR, 1931, 37 226a Furnace spectrum Meggers and Scribner, BSJ, 1935, 14 629 New terms

Meggers and Kiess, C C , JOSA, 1926, 12 417 Multiplets and Zeeman Cbn

King and Meggers, PR, 1931, 37 226a Furnace spectrum Meggers and Scribner, BSJ, 1935, 14 629 New terms

Gibbs and White, PR, 1928, 31 520 Multiplets Cb III Eliason, PR, 1933, 43 745 New multiplets

Gibbs and White, PR, 1928, 31 520 Multiplets Cb iv

# Cd Cadmium 48

Kayser and Konen Cd

Fowler Grotrian CdI Ruark, JOSA, 1925, 11 199 Higher terms added

McLennan, McLay and Crawford, T Roy Soc Canada, 1928, 22 45  $Cd \pi$ Takahashi, AP, 1929, 3 27 Series

Cd III Gibbs and White, PR, 1928, 31 776 Multiplets

#### Ce Cerium 58

Ce Kayser and Konen

Ce I Karlson, ZP, 1933, 85 482 Terms and lines

Се п Haspas, ZP, 1935, 96 410 Terms and Zeeman effect

Ce III Kalia, Indian J Phys 1933, 8 137 Terms and lines

Ce IV Gibbs and White, 1929, 33 157 Doublets of stripped atoms Badami, Proc Phys Soc 1931, 43 53 Lines and terms Lang, Can J Research, 1935, A 13 1 New terms Lang, PR, 1936, 49 552 a Ground term

# Cl Chlorine 17

Cl Kayser and Konen

Cli Kiess, C C and de Bruin, BSJ, 1929, 2 1117 Lines and terms

Cl II Bowen, PR, 1928, 31 34, 1934, 45 401 New lines and terms.

Murakawa, ZP, 1931, 69 507 Terms and lines

Murakawa, ZP, 1935, 96 117 New terms

Cl m Bowen, PR, 1928, 31 34, 1934, 45 401 Lines and terms

Cl IV Ibid

Cl v Ibid

Cl vi Bowen and Millikan, PR, 1925, 25 591 Lines and terms

Cl vii Bowen and Millikan, PR, 1925, 25 295 Lines and terms

# Co Cobalt 27

Co Kayser and Konen

Co I Catalan, ZP, 1928, 47 89 Terms and classified lines Catalan, An Soc fis y quim (Madrid), 1929, 27 832

Co II Findlay, PR, 1930, 36 5 Lines, terms and Zeeman effect

Co v Gilroy, PR, 1931, 38 2217 V i isoelectronic sequence

#### Cr Chromium 24

Cr Kayser and Konen

Cr I Kiess, C C, BSJ, 1930, 5 775 Terms and lines Allen and Hesthal, PR, 1935, 47 926 Intensities

Cr II Kromer, ZP, 1928, 52 531 Zeeman effect Kiess, C C, BSJ, 1930, 5 775 Terms and lines Gilroy, PR, 1931, 38 2217 V I isoelectronic sequence

Cr III White, PR, 1929, 33 914 Ti I isoelectronic sequence Cr IV White, PR, 1929, 33 676 Sc I isoelectronic sequence

Cr IV White, PR, 1929, 33 676 Sc I isoelectronic sequence Cr V White, PR, 1929, 33 543 Ca I isoelectronic sequence

Cr vi Gibbs and White, PR, 1929, 33 157 Doublets of stripped at co

#### Cs Caesium 55

Cs Kayser and Konen

Cs I Fowler Grotrian

Cs II Bacher and Goudsmit, 1932, using unpublished material Laporte, Miller and Sawyer, PR, 1931, 37 845, 1932, 39 458.
Olthoff and Sawyer, PR, 1932, 42 766 Analysis extended

# Cu Copper 29

Cu Kayser and Konen

Cu I Sommer, ZP, 1926, 39 711 Zeeman effect
Bacher and Goudsmit, 1932, using unpublished material

Cu II Shenstone, PR, 1927, 29 380 Terms and lines Bacher and Goudsmit, 1932, using unpublished material Eu Europium 63

Eu I Russell and King, PR, 1934, 46 1023 Low terms

Eu II Albertson, PR, 1934, 45 499a Low terms

# F Fluorine 9

F<sub>I</sub> Bowen, *PR*, 1927, **29** 231 Ground state from ultra-violet lines Dingle, *PRS*, 1928, **117** 407 Terms and lines Edlén. *ZP*, 1935, **98** 445 New terms

F m Dingle, PRS, 1930, 128 600 Series.

F III Dingle, PRS, 1929, 122 144 Series

F IV Bowen, PR, 1927, 29 231

F vi Edlén, ZP, 1934, 89 179

F vii Edlén, ZP, 1934, 89 179

#### Fe Iron 26

Fe I Laporte, ZP, 1924, 23 135, 26 1 Classification and Zeeman effect Laporte, Proc Nat Acad Sci 1926, 12 496 Series Moore and Russell, AJ, 1928, 68 151 Terms
Burns and Walters, Alleghany Observatory Publications, 1929, 6 159

Fe II Russell, AJ, 1926, 64 194 Terms and classified lines Meggers and Walters, Bur of Standards, Sci Pap 1927, 22 205 Low terms

Dobbie, PRS, 1935, 151 703 New terms

Fe IV Gilroy, PR, 1931, 38 2217 V I isoelectronic sequences

Fe v White, PR, 1929, 33 914 Ti I isoelectronic sequences

Fe vi Bowen, PR, 1935, 47 924

# Ga Gallium 31

Ga I Grotrian

Sawyer and Lang, PR, 1929, 34 718 Lines and terms

Ga II Sawyer and Lang, PR, 1929, 34 712 Series

Ga III Lang, PR, 1927, 30 762

Garv Mack, Laporte and Lang, PR, 1928, 31 748

Gd Gadolinium 64

Gd I Albertson, PR, 1935, 47 370 Ground term

Ge Germanium 32

Ge I Gartlem, PR, 1928, 31 782 Lines and terms Rao, K R, PRS, 1929, 124 465 Lines and terms

Ge II Lang, PR, 1929, 34 697 Lines and terms Gartlein, PR, 1931, 37 1704a Series

Ge III Lang, PR, 1929, 34 697 Series

Ge IV Lang, PR, 1929, 34 697 Series

Ge v Mack, Laporte and Lang, PR, 1928, 31 748 Lines and terms

# H Hydrogen 1

H I Fowler Grotrian
Bracket, AJ, 1922, 56 154 A new series
Pfund, JOSA, 1924, 9 139
Hansen, AP, 1925, 78 558
Houston, AJ, 1926, 64 81
Kent, Taylor and Pearson, PR, 1927, 30 266 Fine structure

### H Hydrogen 1 (cont)

H I Houston and Hsieh, PR, 1934, 45 263 Intervals of Balmer lines Williams and Gibbs, PR, 1934, 45 491a Correction to  $R_{\rm H}$ 

#### He Helium 2

He I Fowler Grotrian

Burger, ZP, 1929, 54 643 Intensity

Hopfield, AJ, 1930, 72 133 Ultra-violet series extended

Kruger, PR, 1930, 36 855 New lines classified

Gibbs and Kruger, PR, 1931, 37 1559 Structure of 3888A line

He II Fowler Grotrian

Paschen, AP, 1927, 82 689 Fine structure

Kruger, PR, 1930, 36 855 New lines classified

#### Hf Hamum 72

Hf I Meggers and Scribner, BSJ, 1930, 4 169 Terms and lines

Hf m Meggers and Scribner, JOSA, 1928, 1783 Terms
Meggers and Scribner, BSJ, 1934, 13625 Terms, intensities and

Zeeman effect

# Hg Mercury 80

Hg I Fowler Grotrian

Takamine and Suga, Inst Phys and Chem Tolio, 1930, 13 1 New series in infra-red

Hg II Paschen, Berlin Akad Sitz 1928, 32 536 Terms and lines McLennan, McLay and Crawford, PRS, 1931, 13441 Terms and lines

Hg III McLennan, McLay and Crawford, T Roy Soc Canada, 1928, 22 247
Terms and lines

Mack and Fromer, PR, 1935, 48 357 Pt I isoelectronic sequence

#### I Iodine

II Evans, PRS, 1931, 133 417 Lines and terms Deb. PRS, 1933, 139 380 Lines and terms

I rv Krishnamurty, Proc Phys Soc 1936, 48 277 Lines and terms

#### In Indium 49

In I Fowler Grotrian

Sawyer and Lang, PR, 1929, 34 718 New terms Lansing, PR, 1929, 34 597 New terms

Lang, PR, 1930, 35 126a Ionisation potentials

In II Bacher and Goudsmit, 1932, using unpublished data

In III Lang, Proc Nat Acad Sci 1927, 13 341, 1929, 15 414
Rao, K. R., Narayan and Rao, A. S., Indian J. Phys. 1928, 2 482

In IV Gibbs and White, PR, 1928, 31 776 Some multiplets

#### Ir Iridium 77

Ir I Meggers and Laporte, PR, 1926, 28 642 Low levels Albertson, PR, 1932, 42 443 a Low terms

#### K Potassium 19

KI Fowler Grotrian

Ferschmin and Frisch, ZP, 1929, 53 326 Doublet structure of D terms Edlen, ZP, 1935, 98 445 Doublets resolved

K Potassium 19 (cont )

Bowen, PR, 1928, 31 497 Terms and lines Кπ Whitford, PR, 1932, 39 898 Zeeman effect

de Bruin, ZP, 1929, 53 658 K mRam, Indian J Phys 1933, 8 151

Bowen, PR, 1928, 31 497 One multiplet  $\mathbf{K}\mathbf{r}\mathbf{v}$ Ram, Indian J Phys 1933, 8 151

Kr Krypton 36

Gremmer, ZP, 1929, 54 215 Lines and terms Krı Meggers, de Bruin and Humphreys, BSJ, 1929, 3 129, 1931, 7 643 Lines and terms Pogány, ZP, 1933, 86 729 Zeeman effect

Bakker and de Bruin, ZP, 1931, 69 36 Zeeman effect New terms Kr IIde Brum, Humphreys and Meggers, BSJ, 1933, 11 409

Kr III Deb and Dutt, ZP, 1931, 67 138 Series Humphreys, PR, 1935, 47 712 Lines and terms

La Lanthanum 57

Meggers, BSJ, 1932, 9 239 Lines and Zeeman effect Laı Russell and Meggers, BSJ, 1932, 9 625 Lines and terms

Russell and Meggers, BSJ, 1932, 9 625 Lines and terms La II

La m Russell and Meggers, BSJ, 1932, 9 625 Lines and terms

L<sub>1</sub> L<sub>1</sub>th<sub>1</sub>um 3

Fowler Grotrian Lıı

Werner, N, 1925, 116 574, 1926, 118 154 Series Lı II Schuler, ZP, 1926, 37 568, 1927 42 487 Fine structure Erreson and Edlén, ZP, 1930, 59 656 Ground term

Edlén and Ericson, ZP, 1930, 59 656 Two lines Lım Gale and Hoag, PR, 1931, 37 1703a New lines

Lu Lutecium 71

Meggers and Scribner, BSJ, 1930, 5 73 Lines and terms Luı

IbidLu II Lu III Ibid

Mg Magnesium 12

Fowler Grotrian Mgι Bowen and Millikan, PR, 1925, 26 150 PP' multiplets

Fowler Grotrian Mg II

Mg III Mack and Sawyer, Science, 1928, 68 306, 1761 Series Edlén and Ericson, Comptes Rendus, 1930, 190 116 Doublet

Mg rv Edlén and Ericson, Comptes Rendus, 1930, 190 173 Extreme ultraviolet

Mack and Sawyer, PR, 1930, 35 299 Screening doublets

IbidMgν

Mn Manganese 25

McLennan and McLay, T Roy Soc Canada, 1926, 20 89 Lines and Mn 1 Russell, AJ, 1927, 66 184, 347 Configurations assigned Seward, PR, 1931, 37 344 Intensities

Mn Manganese 25 (cont )

Mn II Russell, AJ, 1927, 66 233
 Duffendack and Black, PR, 1929, 34 42 Lines and terms
 Seward, PR, 1931, 37 344 Intensities

Mn III Gibbs and White, Proc Nat Acad Sci 1927, 13 525 Multiplets Gilroy, PR, 1931, 38 2217 Lines and terms

Mn IV White, PR, 1930, 33 914 TI I isoelectronic sequence

Mn v White, *PR*, 1929, **33** 678 Sc i isoelectronic sequence Bowen, *PR*, 1935, **47** 924 New terms

Mn vII Gibbs and White, Proc Nat Acad Sci 1926, 12 676

### Mo Molybdenum 42

Mo I Catalan, An Soc fis y quim (Madrid), 1923, 21 213 Lines and terms Wilhelmy, AP, 1926, 80 305 Zeeman effect Meggers and Kiess, JOSA, 1926, 12 417 Lines and terms

Mo II Meggers and Kiess, JOSA, 1926, 12 417 Lines and terms Wilhelmy, AP, 1926, 80 305 Zeeman effect

Mo IV Eliason, PR, 1933, 43 745 Multiplets

Mo v Trawick, PR, 1935, 48 223 Sr i isoelectronic sequence

#### N Nitrogen 7

N I Ingram, PR, 1929, 34 421 Terms and lines Hopfield, PR, 1930, 36 789 Adds some higher terms Ekefors, ZP, 1930, 63 437 Lines and terms Stucklen and Carr, PR, 1933, 43 944a One term

N m Fowler, A and Freeman, *PRS*, 1927, **114** 662 Lines and terms Bowen, *PR*, 1927, **29** 231 Lines and terms Freeman, *PRS*, 1929, **124** 654 New terms Bowen, *PR*, 1929, **34** 534 Series

N m Freeman, PRS, 1928, 121 318 Lines and terms

N IV Freeman, *PRS*, 1930, 127 330 Lines and terms Edlen, *N*, 1931, 127 744 Singlets

Bacher and Goudsmit, using unpublished material N v  $\,$  Edlen and Ericson,  $ZP,\,1930,\,64.64\,$  Series

# Na Sodium 11

Na I Fowler Grotrian

Ferschmin and Frisch, ZP, 1929, 53 326 Doublets structure of D terms

Na II Bowen, PR, 1928, 31 967 Lines and terms Frisch, ZP, 1931, 70 498 Lines and terms Vance, PR, 1932, 41 480 Lines and terms

Na III Edlen and Ericson, Comptes Rendus, 1930, 190 173 Extreme ultra violet

Mack and Sawyer, PR, 1930, 35 299 New lines and levels Vance, PR, 1932, 41 480 Lines and terms

Soderqvist, ZP, 1932, 76 316 Lines and terms

Na r. Vance, PR, 1932, 41 480

# Ne Neon 10

100

Ne I Paschen, AP, 1918, 60 405 Paschen and Gotze Ne Neon 10 (cont )

Ne r Back, AP, 1925, 76 317 Zeeman effect
Lyman and Saunders, Proc Nat Acad Sci 1926, 12 92 Low levels
Gremmer, ZP, 1928, 50 716 New levels from infra-red lines
Murakawa and Iwama, Inst Phys and Chem Tokio, 1930, 13 283
Zeeman effect

Ne II Russell, Compton and Boyce, Proc Nat Acad Sci 1928, 14 280 Lines and terms
Frisch, ZP, 1930, 64 499 Two new terms
de Bruin and Bakker, ZP, 1931, 69 19 Zeeman effect

Ne III Boyce and Compton, Proc Nat Acad Sci 1929, 15 656 Series de Bruin, ZP, 1932, 77 489 New lines and terms Keussler, ZP, 1933, 85 1 Ground term

Ne IV Boyce and Compton, Proc Nat Acad Sci 1929, 15 656 Sciles

N<sub>1</sub> N<sub>1</sub>ckel 28

N<sub>1</sub> I Russell, PR, 1929, 34 821 Lines and terms
Ornstein and Buoma, PR, 1930, 36 679 Intensities
Marvin and Baragar, PR, 1933, 43 973 Zeeman effect

N<sub>1 II</sub> Shenstone, PR, 1927, 30 255 Lines, terms and Zeeman effect Menzies, PRS, 1929, 122 134 Ground term Ornstein and Buoma, PR, 1930, 36 679 Intensities

Ni vi Gilroy, PR, 1931, 38 2217 V i isoelectronic sequence

O Oxygen 8

O<sub>I</sub> Hopfield, *PR*, 1931, 37 160 Lines and terms de Bruin, *N*, 1932, **129** 469

On Russell, PR, 1928, 31 27 Terms and lines

O III Fowler, A, PRS, 1928, 117 317 Lines and terms Freeman, PRS, 1929, 124 654 Series

O rv Bowen, PR, 1927, 29 231 Freeman, PRS, 1930, 127 330

Ov Edlén, N, 1931, 127 744 Singlets Bacher and Goudsmit, 1932, using unpublished material.

O vi Edlén and Ericson, ZP, 1930, 64 64 Li-like spectra

Os Osmium 76

Os I Meggers and Laporte, PR, 1926, 28 642 Six low levels

P Phosphorus 15

P<sub>I</sub> Kiess, C C, BSJ, 1932, 8 393 Lines and terms Robinson, PR, 1936, 49 297 New terms

Рп Bowen, PR, 1927, 29 510 Lines and terms Robinson, PR. 1936, 49 297 New terms

P III Millikan and Bowen, PR, 1925, 25 600 Lines and terms Saltmarsh, PRS, 1925, 108 332 Higher terms Bowen, PR, 1928, 31 34 New lines Bowen, PR, 1932, 39 8 New terms

Prv Bowen and Millikan, *PR*, 1925, **25** 591 Terms and lines Bowen, *PR*, 1932, **39** 8 New terms

Pv Millikan and Bowen, PR, 1925, 25 295 Lines and terms

#### Pb Lead 82

Pb I Gleseler and Grotrian, ZP, 1925, 34 374, 1926, 39 377 Series Back, ZP, 1926, 37 193 Zeeman effect Bacher and Goudsmit, 1932, using unpublished material

Pb II Gieseler, ZP, 1927, 42 265 Lines and terms

Pb III Smith, PR, 1929, 34 393, 1930, 36 1 Terms and lines Green and Loring, PR, 1932, 41 389 Zeeman effect

Pb IV Smith, PR, 1930, 36 1 Lines and terms

Pb v Mack, PR, 1929, 34 17 Lines and terms

Mack and Fromer, PR, 1935, 48 357 Pt I isoelectronic sequence

### Pd Palladium 46

Pd I Shenstone, PR, 1930, 36 669 Lines, terms and Zeeman effect

Pd II Shenstone, PR, 1928, 32 30 Lines and terms Blair, PR, 1930, 36 173 New terms

#### Pt Platmum 78

Pt I Haussmann, AJ, 1927, 66 333, PR, 1928, 31 152 Zeeman effect and terms

Livingood, PR, 1929, 34 185 Lines and terms

#### Ra Radium 88

Ra I Rasmussen, ZP, 1934, 87 607

Ra II Fowler

Rasmussen, ZP, 1933, 86 24

#### Rb Rubidium 37

Rb I Fowler Grotrian

Ramb, AP, 1931, 10 311 Doublets resolved

Rb II Laporte, Miller and Sawyer, PR, 1931, 38 843 Series

# Re Rhenium 75

Re I Meggers, BSJ, 1931, 6 1027 Lines and terms

#### Rh Rhodium 45

Rh I Sommer, ZP, 1927, 45 147 Lines, terms and Zeeman effect

Rh m Bacher and Goudsmit, 1932, using unpublished material

#### Rn Radon 86

Rn I Rasmussen, ZP, 1933, 80 726 Lines and terms

#### Ru Ruthenium 44

Ru I Sommer, ZP, 1926, 37 1 Lines, terms and Zeeman effect

Ru  $\pi$  Meggers and Shenstone, PR, 1930, 35 868

Bacher and Goudsmit, 1932, using unpublished material

#### S Sulphur 16

S I Frerichs, ZP, 1933, 80 150 Lines and terms
 Meissner, Bartelt and Eckstein, ZP, 1933, 86 54 Additional terms
 Ruedy, PR, 1933, 44 757 New terms

S II Ingram, PR, 1928, 32 172 Lines and terms Gilles, Ann de Phys 1931, 15 267 Terms Bartelt and Eckstem, ZP, 1933 86 77 New terms

S III Ingram, PR, 1929, 33 907 Lines and terms

S IV Millikan and Bowen, PR, 1925, 25 602 Lines and terms

S Sulphur 16 (cont)

SIV Bowen, PR, 1928, 31 38 New terms

Millikan and Bowen, PR, 1925, 25 591, 26 150 Lines and terms Sv

Svi Millikan and Bowen, PR, 1925, 25 295 Doublet Laws

Sb Antimony 51

McLennan and McLay, T Roy Soc Canada, 1927, 21 63 Lines and Sbı

Lowenthal, ZP, 1929, 57 822 Zeeman effect and new terms.

Lang and Vestine, PR, 1932, 42 233 Terms Sb II

Sb m Lang, PR, 1930, 35 445 Terms and lines

Green and Lang, Proc Nat Acad Sci 1928, 14 706 Lines and Sb rv

Badami, Proc Phys Soc 1931, 43 538 Series

Lang, Proc Nat Acad Sci 1927, 13 341 Series. Sb v Badami, Proc Phys Soc 1931, 43 538 Series

Sc Scandium 21

Russell and Meggers, Bur Stand, Sci Papers, 1927, 22 329 Lines and ScI

Russell and Meggers, Bur Stand, Sci Papers, 1927, 22 329 Lines and Sc II terms Russell and Meggers, BSJ, 1929, 2 733 Comparison with Y

Russell and Lang, AJ, 1927, 66 13 Lines and terms Sc m Smith, Proc Nat Acad Sci 1927, 13 65 Extension of series

Majumdar and Toshniwal, N, 1928, 121 828 Screening doublets Se rv

Se Selenium 34

McLennan, McLay and McLeod, PM, 1927, 4 486 Lines and terms SeI Gibbs and Ruedy, PR, 1932, 40 204 New terms

Badami and Rao, K R, PRS, 1933, 140 387 Lines and terms  $Se \pi$ Martin, PR, 1935, 48 938 Lines and terms

Pattabhiramayya and Rao, A S, Indian J Phys 1929, 3 531 Series Se rv

Sawyer and Humphreys, PR, 1928, 32 583 Series Se v

Sawyer and Humphreys, PR, 1928, 32 583 Series Se vi

Si Silicon 14

Fowler, A, PRS, 1929, 123 422 Lines and terms SiI Kless, C C, BSJ, 1933, 11 775 New terms

Fowler, A, Phil Trans R S 1925, 225 1 Series SıII Bowen and Millikan, PR, 1925, 26 150 PP° multiplets. Bowen, PR, 1928, 31 34 Series

Fowler, A, Phil Trans RS 1925, 225 1 Series  $S_{1}m$ Sawyer and Paschen, AP, 1927, 84 1 Comparison with Al  $\pi$ 

Fowler, A, Phil Trans RS 1925, 225 1 Series S1 TV

Edlén and Ericson, Comptes Rendus, 1930, 190 116 Doublets. Sıv

Sm Samarıum 62

Albertson, PR, 1935, 47 370 Ground term Sm I

Sn Tm 50

Back, ZP, 1927, 43 309 Lines, terms and Zeeman effect. SnI Green and Loring, PR, 1927, 30 575 Terms, lines and Zeeman effect Bacher and Goudsmit, 1932, using unpublished material. 17-2

# Sn Tin 50 (cont )

Sn. II Grotrian

Green and Loring, PR, 1927, 80 574 Lines, terms and Zeeman effect Narayan and Rao, KR, ZP, 1927, 45 350 Terms Lang, PR, 1930, 35 445 Lines and terms

Sn III Gibbs and Vieweg, PR, 1929, 34 400 Cd I isoelectronic sequence Green and Loring, PR, 1931, 38 1289 Multiplets and Zeeman effect

Snrv Rao, K R, Narayan and Rao, A S, Indian J Phys 1928, 2 476 Series

Sn v Gibbs and White, Proc Nat Acad Sci 1928, 14 345 Series

#### Sr Strontium 38

Sr I Fowler Grotrian
Russell and Saunders, AJ, 1925, 61 39 Lines and terms
Sr II Fowler Grotrian

#### Ta Tantalum 73

Ta I McLennan and Durnford, PRS, 1928, 120 502 Zeeman effect Kless, C C and Kless, H K, BSJ, 1933, 11 277 Lines and terms

#### Te Tellurium 52

Te I Bartelt, ZP, 1934, 88 522 Lines and terms

Te III Krishnamurty, PRS, 1935, 151 178 Lines and terms

Te IV Rao, K R, PRS, 1931, 133 220 Lines and terms

Te v Gibbs and Vieweg, PR, 1929, 34 400 Cd I isoelectronic sequence

Te VI Lang, Proc Nat Acad Sci 1927, 13 341 Lines and terms Rao, K. R., PRS, 1931, 133 220 Lines and terms

#### Ti Titanium 22

Ti I Russell, AJ, 1927, 66 347 Lines and terms Harrison, JOSA, 1928, 17 389 Intensities White, PR, 1929, 33 914 Ti I isoelectronic sequence

Ti  $\pi$  Russell, AJ, 1927, 66 283 Lines and terms

Ti III Russell and Lang, AJ, 1927, 66 13 Terms Ti IV Russell and Lang, AJ, 1927, 66 13 Terms

# Tl Thallium 81

Tl I Fowler Grotman

Tl II McLennan, McLay and Crawford, PRS, 1929, 125 570 Lines and terms Smith, PR, 1930, 35 235 Extension of series Ellis and Sawyer, PR, 1936, 49 145 New lines and terms

TI m McLennan, McLay and Crawford, PRS, 1929, 125 50 Lines and terms

TI rv Rao, K. R., Proc. Phys. Soc. 1929, 41 361 Terms
Mack and Fromer, PR, 1935, 48 357 Pt 1 isoelectronic sequence

#### V. Vanadium 23

VI Bacher and Goudsmit, 1932, using unpublished material Gilroy, PR, 1931, 38 2217 New lines and terms

V II Meggers, ZP, 1925, 33 509, 39 114 Lines, terms and Zeeman effect Russell, AJ, 1927, 66 184, 194 Terms named
 White, PR, 1929, 33 914 New terms and lines

V m White, PR, 1929, 33 672 Sc I isoelectronic sequence

### V Vanadium 23 (cont)

V IV White, PR, 1929, 33 542 Ca I isoelectronic sequence

V v Gibbs and White, PR, 1929, 33 157 Doublets of stripped atoms

# W Tungsten 74

W I Benning, ZP, 1927, 42 146 Zeeman effect Bacher and Goudsmit, 1932, using unpublished material Laun, PR, 1935, 48 572a New terms

WII Beining, ZP, 1927, 42 146 Zeeman effect

### Xe Xenon 54

Xe I Rasmussen, ZP, 1932, 72 779
 Humphreys and Meggers, BSJ, 1933, 10 139 Lines and terms
 Pogány, ZP, 1935, 93 364 Zeeman effect

Xe II Humphreys, de Bruin and Meggers, BSJ, 1931, 6 287 Lines and terms

Xe III Deb and Dutt, ZP, 1931, 67 138

### Y Yttrium 39

Y I Meggers and Russell, BSJ, 1929, 2 733 Lines and terms

Y II Meggers and Russell, BSJ, 1929, 2 733 Lines and terms

Y m Meggers and Russell, BSJ, 1929, 2 733 Lines and terms

#### Zn Zinc 30

Zn I Fowler Grotrian

Sawyer, JOSA, 1926, 13 431 PP° multiplets

Zn II Lang, Proc Nat Acad Sci 1929, 15 414 Lines and terms Takahashi, AP, 1929, 3 27 Lines and terms

Zn III Laporte and Lang, PR, 1927, 30 378 Series

# Zr Zirconium 40

Zrı Kıess, C C and Kıess, H K, BSJ, 1931, 6 621 Lmes, terms and Zeeman effect

 ${
m Zr}\,\pi$  Kiess, C C and Kiess, H K, BSJ, 1930, 5 1205 Lines, terms and Zeeman effect

Zr III Kiess, C C and Lang, BSJ, 1930, 5 305 Lines and terms

Zr IV Kiess, C C and Lang, BSJ, 1930, 5 305 Lines and terms

# C The hyperfine structure of the elements

Ag Tolansky, PPS, 1933, 45 559 No hyperfine structure in Ag I Williams and Middleton, N, 1933, 131 691 No hyperfine structure found Jackson, N, 1933, 131 691 No hyperfine structure found Hill, PR, 1934, 46 536 No hyperfine structure found

G1bbs and Kruger, PR, 1931, 37 656 $\alpha$  No hyperfine structure in 4 lines White, PR, 1931, 37 1175 $\alpha$  Interpretation of G1bbs and Kruger Tolansky, ZP, 1932, 74 336 Narrow lines suggests g(I) small Williams and Sabine, PR, 1933, 43 362 $\alpha$  No hyperfine structure in Al III Paschen and Ritschl, AP, 1933, 18 867 Hyperfine structure of Al II shows  $I = \frac{1}{2}$ 

Brown and  $\tilde{\text{Cook}}$ , PR, 1934, 45 731  $\alpha$  Work of Paschen shows  $\mu = 24$ 

- As Tolansky, PRS, 1932, 137 541, ZP, 1933, 87 210 I=1½ in As π Rao, A S, ZP, 1933, 84 236 I is 1½ in As π Crawford and Crooker, N, 1933, 131 655 As π confirms Tolansky and Heard, PRS, 1934, 146 818 Intensities of As π confirm
- Ba Ritschl and Sawyer, ZP, 1931, 72 36 Resonance lines of Ba  $\pi$  Kruger, Gibbs and Williams, PR, 1932, 41 322  $I=2\frac{1}{2}$  in 135 and 137
- Be Kruger and Wagner, PR, 1932, 41 373a Three lines of Be I and two lines of Be II appear sharp
  Parker, PR, 1933, 43 1035a I is probably ‡
- B1 Goudsmit and Back, ZP, 1927, 43 321, 1928, 47 174 Hyperfine structure in magnetic field shows  $I=4\frac{1}{2}$  McLennan, McLay and Crawford, PRS, 1930, 129 579 Bi II and Bi III Zeeman, Back and Goudsmit, ZP, 1931, 66 1 Magnetic analysis of Bi I Fisher and Goudsmit, PR, 1931, 37 1057 Analysis of partially resolved patterns
- Br de Bruin, N, 1930, 125 414 Hyperfine structure shows  $I=1\frac{1}{2}$  Tolansky, PRS, 1932, 136 585 Confirms de Bruin Brown, PR, 1932, 39 777 Band spectrum shows  $I=1\frac{1}{2}$  or  $2\frac{1}{2}$  in Br<sup>79</sup> and Br<sup>81</sup>
- **Cb** Ballard, PR, 1934, 46 806  $I=4\frac{1}{2}$ ,  $\mu=3$  7
- Cd Schuler and Bruck, ZP, 1929, 56 291 Hyperfine structure shows I=0 in even and I=½ in odd isotopes
  Schuler and Keyston, ZP, 1931, 71 413 Abnormal intensities
  Jones, Proc Phys Soc, 1933, 45 625 In Cd π μ is -0 625
  Schuler and Westmeyer, ZP, 1933, 82 685 Isotope displacement in Cd π
- C1 Elhott, PRS, 1930, 127 638 Band spectrum shows  $I=2\frac{1}{2}$  Tolansky, ZP, 1931, 73 470, 1932, 74 336 Hyperfine structure shows  $\mu$  is small, isotope displacement
- Co Grace, PR, 1933, 43 762a I is probably  $3\frac{1}{2}$  More, PR, 1934, 46 470  $I=3\frac{1}{2}$ ,  $\mu$  is between 2 and 3 Kopfermann and Rasmussen, ZP, 1935, 94 58  $I=3\frac{1}{2}$  confirmed
- Cs Jackson, PRS, 1934, 143 455 Hyperfine intensity ratio shows  $I=3\frac{1}{2}$  Granath and Stranathan, PR, 1934, 46 317  $\mu$  is 2 45 Kopfermann, ZP, 1932, 73 437  $I=3\frac{1}{2}$  in Cs ii Cohen, PR, 1934, 46 713 Atomic ray shows  $I=3\frac{1}{2}$  Heydenburg, PR, 1934, 46 802 Polarisation of resonance radiation shows  $\mu$  between 2 40 and 2 52
  - shows  $\mu$  between 2 40 and 2 52 Jackson, ZP, 1935, 93 809 Intensity ratios in 4555 A line
  - Granath and Stranathan, PR, 1935, 48 725 Hyperfine structure shows  $\mu$  between 2 4 and 3 0
- Cu Ritschl, ZP, 1932, 79 1 I is 1½ in both isotopes. Cu i Isotope displacement
   Schuler and Schmidt. ZP, 1936, 100, 113, 11-2, 5 in 62 and 11-2, 6 in 65.
  - Schuler and Schmidt, ZP, 1936, 100 113  $~\mu\!=\!2~5$  in 63 and  $~\mu\!=\!2~6$  in 65 Electric quadripole moment
- Eu Schuler and Schmidt, ZP, 1935, 94 457  $I=2\frac{1}{2}$  in 151 and 153, both  $\mu$ 's are positive,  $\mu_{151}$   $\mu_{153}=2$  2 Abnormal intervals

F Gale and Monk, PR, 1929, 33 114 Band spectrum shows  $I = \frac{1}{2}$  Campbell, ZP, 1933, 84 393 In F I,  $I = \frac{1}{2}$  Brown and Bartlett, PR, 1934, 45 527  $\mu$  is about  $3\mu_N$ 

Ga Jackson, ZP, 1932, 74 291 Resonance lines of Ga I

Campbell, N, 1933, 131 204 I=1 in 69 and 71 from Ga  $\pi$ 

**H**<sup>1</sup> Kapuściński and Eymers, PRS, 1929, **122** 58 Band spectrum shows  $I=\frac{1}{2}$ 

Rabi, Kellogg and Zacharias, PR, 1934, 46 157  $\mu$  for proton is 3 25

H<sup>2</sup> Urey, Brickwedde and Murphy, PR, 1932, 40 1 Mass effect in Balmer lines

Murphy and Johnston PR, 1934, 46 95, Rand spectrum shows I-1

Murphy and Johnston, PR, 1934, 46 95 Band spectrum shows I=1 Estermann and Stern, N, 1934, 133 911  $\mu$  is  $0.7\mu_N$ 

Rabı, Kellogg and Zacharıas, PR, 1934, 46 163  $~\mu$  for deuton is  $0.75\pm0.2$ 

Schuler and Keyston, ZP, 1931, 72 423 Hg I Isotope displacement
Schuler and Jones, ZP, 1932, 74 631 Hg II Isotope displacement
Schuler and Jones, ZP, 1932, 77 801 Irregularities
Mrozowski, Acad Pol Sci et Lettres, 1931, 9 464 2537 A line
Inglis, ZP, 1933, 84 466 Magnetic wandering of 2537 A line
Schuler and Schmidt, ZP, 1935, 98 239 Asymmetry of electric field of Hg<sup>201</sup>

Venkatesachar and Sibaiya, Indian Acad of Sci Proc 1934, 1 8 Hyperfine structure of Hg II

I Loomis, PR, 1927, 29 112 Band spectrum shows I is large Tolansky, PRS, 1935, 149 269 Hyperfine structure of I II shows  $I=2\frac{1}{2}$  Tolansky, PRS, 1935, 152 663 I I confirms A perturbed term Strait and Jenkins, PR, 1936, 49 635a Alternating intensities confirm

I =  $2\frac{1}{2}$ In Jackson, ZP, 1933, 80 59 Hyperfine intensity ratio shows  $I = 4\frac{1}{2}$ Paschen, Sitz d Preusz Akad d Wiss Phys-Math 1934, 456 Departures from interval rule in In II

Ir Schuler and Schmidt, ZP, 1935, 94 460 I is probably  $\frac{1}{2}$  in 191 and 193

K Loomis and Wood, PR, 1931, 38 854 Band spectrum shows  $I > \frac{1}{2}$  Schuler, ZP, 1932, 76 14 Isotope displacement Fermi and Segré, ZP, 1933, 82 749 Hyperfine structure cannot be resolved

Frisch, PZ Sowjetunion, 1933, 4 557 30 lines of K II are single Jackson and Kuhn, PRS, 1934, 148 335 Hyperfine structure of resonance lines shows  $I \ge 2\frac{1}{2}$ 

Millman, Fox and Rabi, PR, 1934, 46 320 Splitting of atomic rays gives  $I=1\frac{1}{2}$  and  $\mu=0$   $38\mu_N$ 

Millman, PR, 1935, 47 739  $I > \frac{1}{2}$  in  $K^{41}$ 

Fox and Rabi, PR, 1935, 48 746 Atomic ray shows  $\mu=0$  379 in K<sup>39</sup> and  $I \approx 2\frac{1}{2}$  in K<sup>41</sup>

Kr Kopfermann and Wieth-Knudsen, ZP, 1933, 85 353 Work on Kr I shows in Kr<sup>83</sup> I is  $\geqslant 3\frac{1}{2}$  and  $\mu$  probably negative

- La Anderson, PR, 1934, 45 685, 46 473 Hyperfine structure shows  $I=3\frac{1}{2}$  and  $\mu=2.5$ 
  - Crawford, PR, 1935, 47 768 Hyperfine structure of La I confirms Anderson
- L1 Schuler, AP, 1925, 76 292, ZP, 1927, 42 487 Hyperfine structure of L1 m

Harvey and Jenkins, PR, 1930, 35 789 Band spectrum shows  $I=1\frac{1}{2}$  in  $L_1$ <sup>7</sup>

Hughes and Eckart, PR, 1930, 36 694 Mass effect

van Wijk and van Koeveringe, PRS, 1931, 132 98 Band spectrum shows  $I = 1\frac{1}{2}$  in Li<sup>7</sup>

Guttinger and Pauli, ZP, 1931, 67 743 Perturbations in Li II

Goudsmit and Inglis, PR, 1931, 37 328 a Hyperfine structure of Li II Granath, PR, 1932, 42 44 From 5485A of Li II,  $I=1\frac{1}{2}$  and  $\mu=3$  29 $\mu_N$  Grav. PR. 1933. 44 570  $I=1\frac{1}{2}$  confirmed

Ladenburg and Levy, ZP, 1934, 88 449 Alternating intensities suggest  $I=2\frac{1}{2}$  in Li

Fox and Rabi, PR, 1935, 48 746 Atomic ray shows  $I \ge 1$  in Li<sup>6</sup> and  $\mu=3$  20 in Li

Fock and Petrashen, PZ Sowjetunion, 1935, 8 547 Theory suggests  $\mu=4$  57

Bartlett and Gibbons, PR, 1936, 49 552a Comment on Fock and Petrashen

Schuler and Schmidt, ZP, 1936, 99 285 If I=1 in Li<sup>6</sup>, then  $\mu=0$  6

Lu Schuler and Schmidt, ZP, 1935, 95 265  $I=3\frac{1}{2}$ , deviations from interval rule

- Mg Murakawa, ZP, 1931, 72 793 Absence of hyperfine structure in Mg1 suggests I=0
  - Jackson and Kuhn, PRS, 1936, 154 679 Isotope displacement in resonance line
- Mn White, PR, 1929, 34 1404 Hyperfine structure shows  $I = 2\frac{1}{2}$  White and Ritschl, 1930, 35 1146 Vector coupling in Mn I
- N Ornstein and van Wijk, ZP, 1928, 49 315 Band spectrum shows I=1

Bacher, PR, 1933, 43 1001 Magnetic moment of nucleus  $\geqslant 0.2\mu_N$  since lines very fine

Na Frisch, PZ Sowjetunion, 1933, 4 559 Lines of Na  $\Pi$  show  $I=1\frac{1}{2}$  Rabi and Cohen, PR, 1933, 43 582 Atomic rays show  $I=1\frac{1}{2}$  van Atta and Granath, PR, 1933, 44 61 $\alpha$   $\mu=2$  6 $\mu$  Joffe, PR, 1934, 45 468 Band spectrum shows  $I=1\frac{1}{2}$  Rabi and Cohen PR 1934, 46 707 Atomic rays have I=1

Rabi and Cohen, PR, 1934, 46 707 Atomic ray shows  $I = 1\frac{1}{2}$ 

Larrick, PR, 1934, 46 581 Polarisation of resonance radiation explained by  $I=1\frac{1}{2}$ 

Fox and Rabi, PR, 1935, 48 746 Method of "zero moments" shows  $\mu$ =2 08

Ne Nagaoka and Mishima, P Imp Acad Tokio, 1929, 5 200, 1930, 6 143

Mass effect and magnetic splitting

Bartlett and Gibbons, PR, 1933, 44 538 Isotope displacement theory

**P** Herzberg, PR, 1932, 40 313 Band spectrum Ashley, PR, 1933, 44 919 Band spectrum shows  $I=\frac{1}{2}$ Jenkins, PR, 1935, 47 783a Alternating intensities confirm Ashley

**Pb** Murakawa, ZP, 1931, 72 793 I=0 for 206 and 208, but  $\frac{1}{2}$  for 207 Kopfermann, ZP, 1932, 75 363 Isotope displacements Schuler and Jones, ZP, 1932, 75 563 Hyperfine structure shows new isotope

Rose and Granath, PR, 1932, 40 760 Isotope displacements Dickinson, PR, 1934, 46 498 Isotope displacements Rose, PR, 1935, 47 122 Isotope displacements reviewed

**Pr** White, PR, 1929, 34 1397 In Pr II,  $I=2\frac{1}{2}$ 

Pt Fuchs and Kopfermann, Nw, 1935, 23 372 Jaeckel and Kopfermann, ZP, 1936, 99 492  $I=\frac{1}{2}$  in Pt<sup>195</sup>, isotope displacements Jaeckel, ZP, 1936, 100 513 Confirms  $I=\frac{1}{2}$ 

Kopfermann and Krebs, ZP, 1936, 101 193 Isotope proportions present

Rb Kopfermann, ZP, 1933, 83 417 Rb  $\pi$  shows  $I=1\frac{1}{2}$  in 87 and  $2\frac{1}{2}$  in 85  $\mu_{87}$  is twice  $\mu_{85}$  No isotope displacement Jackson, ZP, 1933, 86 131 Confirms Kopfermann

Re Zeeman, Gısolf and de Bruin, N, 1931, 128 637 Zeeman effect of hyperfine structure shows  $I=2\frac{1}{2}$  Meggers, King and Bacher, PR, 1931, 38 1258 Hyperfine structure shows  $I=2\frac{1}{2}$  in both isotopes

Sommer and Karlson, Nw, 1931, 19 1021 Confirms Meggers

Sb Tolansky, PRS, 1934, 146 182  $I=2\frac{1}{2}$  in 121 and 123,  $\mu_{121}=2$  75,  $\mu_{123}=2$  0 Crawford and Bateson,  $Can\ J$  Research, 1934, 10 693 Sb III shows  $I=2\frac{1}{2}$  in 121 and  $3\frac{1}{2}$  in 123,  $\mu_{121}=4$  0,  $\mu_{123}=3$  2

Sc Kopfermann and Rasmussen, ZP, 1934, 92 82  $I=3\frac{1}{2}$  and  $\mu=3$  6

Se Rafalowski, Acta Phys Polonica, 1933, 2 119 Lines are single Olsson, ZP, 1934, 90 134 Band spectrum shows I=0 in Se<sup>80</sup>

Srn Schuler and Schmidt, ZP, 1934, 92 148 Isotope displacements

Sn Tolansky, PRS, 1934, 144 574 Sn II shows  $I=\frac{1}{2}$  in 117 and 119,  $\mu$  is  $0.89\mu$ , in both One line of Sn I confirms I Isotope displacement

Sr Benson and Sawyer, PR, 1933, 43 766a No hyperfine structure wider than 0 05 cm<sup>-1</sup>

Ta Gisolf and Zeeman, N, 1933, 132 566 Hyperfine structure shows  $I=3\frac{1}{2}$  McMillan and Grace, PR, 1933, 44 949 Hyperfine structure shows  $I=3\frac{1}{2}$ 

Te Rafalowski, Acta Phys Polonica, 1933, 2 119 Lines are single

T1 Schuler and Keyston, ZP, 1931, 70 1 Isotope displacement Tl I,
Tl II

Crooker, PM, 1933, 16 994 Paschen-Back effect Wills, PR, 1934, 45 883  $\mu$ =2 7 A perturbed term

V Kopfermann and Rasmussen, ZP, 1935, 98 624 Hyperfine structure shows I=3

W Grace and White, PR, 1933, 43 1039a No value of I Lines complex

- **Xe** Kopfermann and Rindal, ZP, 1933, 87 460  $I=\frac{1}{2}$  in 129 and  $1\frac{1}{2}$  in 131  $\mu_{129}$  is negative,  $\mu_{131}$  is positive  $\mu_{129}/\mu_{131}$  is 1 1 No isotope displacement Gwynne-Jones, PRS, 1934, 144 587 Xe i confirms
- Y Kruger and Challacombe, PR, 1935, 48 111 a Earlier report incorrect
- Zn Schuler and Bruck, ZP, 1929, 56 291 No hyperfine structure found Zn I Murakawa, ZP, 1931, 72 793 Absence of hyperfine structure in Zn I suggests I=0
  - Schuler and Westmeyer, ZP, 1933, 81 565 Zn II shows isotope displacement In Zn 67,  $I=1\frac{1}{2}$
  - Billeter, Helv Phys Acta, 1934, 7 413 No hyperfine structure found in resonance line

## SUBJECT INDEX

## Numbers in Clarendon refer to the second volume

Absorption spectra, 68 rare earths, 81 X-rays, 193 Alkalme earths, are and spark spectra, inter system lines, 57 interval rule, 63 isoelectronic spectra, 212 jj coupling, 142 singlets and triplets, 47 Alkalis, doublet series, 23, 31-2 doublet intensities, 107 forbidden lines, 215 isoelectronic spectra, 212 Alternating intensities, 200–2 Aluminium, 22-4 absorption spectrum, 68 displaced terms, 7 displacement law, Al III, 177 Landé's doublet formula, 215 perturbed series, 151 Analysis, hyperfine, 189 multiplet, 48 series, 18 Zeeman, 99 Angstrom unit, 5 Anomalous Zeeman effect, 85, 144 Antimony, 28-32 fluorescence, 80 Arc spectra, 46 Argon, 39-44 10nized, 38, 145 level diagram, 40 nebular lines, 218 Arsenic, 28-32 Atomic magnetism, atomic rays, 129 electronic theory, 129 paramagnetic ions, 135 Atomic rays, 129 nuclear spm, 201 velocity selector, 200 Atomic volumes, 161 Auroral line, 35, 215-17 Balmer series, 2, 5, 7, 9 fine structure, 41 reversal, 69 Band spectra, 172

nuclear spin, 201

Bands, anti-Stokes, 233 in phosphores, 233 Barium, 46-58, 50 abnormal intensities, 135 Bergmann series, 22 Beryllium, 46-58 displaced terms, 6 Moseley diagram, 204 Bismuth, 28-32 hyperfine structure, 169-70, 181-3, magnetic moment, 133 X-ray spectrum, 197-8 Bohr magneton, 87, 128, 130 Boltzmann distribution law, 70, 85, 234 Boron, 22-4 Bromine, 36-9 Cadmium, 46-58 displaced terms, 7 hyperfine structure, 170-1, 207 ionised, 67 magnetic moment, 132 Caesium, 18-39, 50 doublet structure, 30 intensities, 107-8 level diagram, 39 series, 39 Calcium, 46-58, 50 diffuse triplets, 56 displaced terms, 1 doublet limit, 158 effective quantum numbers, 51 ıntensities, 102 ionised, 178, 205 level diagrams, 50, 52, 2 perturbed series, 151 series, 48 Carbon, 24-8 Catalysts, 188 Centroid of a multiplet, 65 Cerium, 53, 78 Chlorine, 36-9 hyperfine structure, 207 level diagram, 37 Chromium, 57-8 g factors, 125 intensities, 106

intervals, 148-9

Chromium (cont) Doublet formulae (cont) phosphores, 229–32 screening, 206 Zeeman patterns, 117 Sommerfeld's, 210-11 Cobalt, 61, 63 spin, 208 intensities, 106 Doublet series, 23, 31-2 magnetic moment, 134 Coloured ions, 188 Earth metals, 22-4 Effective nuclear charge, 203 Columbium, 54, 57 Zeeman patterns, 103 Effective quantum number, 22 Column III, 22-4 Electric field, see Stark effect, 144 IV, 24-8, 140-2 Electron, in nucleus, 209-10 V, 28–32 magnetic moment of, 96 ,, VI, 33-4 mass of, 14, 44, 84 Combination of electrons, energy rules, Electron impact, 76 Electron orbits, 10-13, 26-8, 207 Electron theory of magnetism, 127 equivalent electrons, 11 Electronic angular momentum, see J, inverted terms, 17 unlike electrons, 9 34 Combination principle, 21, 24 Electronic displacements, 147-50 Configurations, 179-93 Electronic structures, 179-95 elements tabulated, 194-5 Electrovalency, 167 Energy of interaction of two vectors, Copper, 66-9 orbital and spin vectors, 65 g factors, 155 level diagram, 69 in strong magnetic field, 112 magnetic moment, 132 in weak magnetic field, 97 perturbed series, 151-4 Energy rules, multiplet, 15 Zeeman patterns, 103-4, 118 Enhanced lines, 46 Correspondence principle, 13, 36, 93 Equivalent electrons, 11 Coupling, deviations from Russell-Erbium phosphores, 242 Erect terms, 35 Saunders, 43-4, 122 Europium, hyperfine structure, 199 **]**], 28, 136–43 Russell Saunders, 3-5, 22 phosphores, 236 Covalency, 167, 172 valency, 78 Excitation, by electron impact, 76 Crystals, energy levels, 228 by monochromatic light, 78 Deutonic nuclei, 205, 214 potentials, 73 Diamagnetism, 127 Exclusion principle, periodic system, Diffuse series, 18 doublets, 31, 34, 37 combination of electrons, 11, 17 formula, 23 Stark effect, 158 Fine structure, constant, 210 triplets, 54-6 of helium, 44-5, 60-1Zeeman types, 83 of hydrogen, 40-4 Displaced terms, alkaline earths, 1 Fluorescence, in crystals, 228 Be and Mg, 6 hyperfine, 192 Zn, Cd and Hg, 7 m vapours, 80 Displacement law for spectra, 175-8 Fluorescent crystals, chromium phos-Displacements, atomic, 19, 128, 133 phores, 229 electronic, 19, 128-33, 147-50 energy levels, 228 m electric field, 145, 157-60 Lenard phosphores, 245 in magnetic field, 112, 124 platino cyanides, 246 sum rule, 124, 126 rare earth phosphores, 236 Distribution law, Boltzmann's, 70, 85, uranyl salts, 241 Fluorine, 36–9 Doublet formulae, 1rregular, 206 Fluorite, 236 Lande's, 212-16 Forbidden lines, 27, 151, **21**5 regular, 208 Frame elements, 184

Fundamental series, 22 Intensities (cont) doublets, 32, 37 normal multiplet, 35, 91 formula, 23 quadripole, 227 triplets, 57 rares ultimes, 120 sum law, 93, 135 g, see Magnetic splitting factor, 90 super multiplet, 101 Gadolinium, 83 tables, 95–9 Gallium, 22-4 X ray, 196 nucleus, 211 Zeeman, 98, 108 Γ, see Displacement Zeeman tables, 112–15 Germanium, 24–8 Intermediate magnetic fields, 116 Inter system lines, 57 Gold, 66-7 magnetic moment, 132 jj coupling, 28 Ground terms, 68 Zeeman effect, 116 elements tabulated, 194 Interval quotient, 65 long periods, 187, 45-7 Interval rule, 63 hyperfine, 173 rare earths, 192, 80 short periods, 183 hyperfine perturbed, 197-9 perturbation, 155 Invariance, of g sum, 123, 123–6 Hafmum, 58-4 of  $\Gamma$  sum, 124, 126 Halogens, 36 Heavy hydrogen, 15, 167 Inverted terms, 35, 16-20Iodine, 36–9 nucleus, 206, 214 jj coupling, 142 Helium, 59-62 Ionisation potentials, from electron imionised, 14, 44-5 pact, 72 level diagram, 59 Stark effect, 151-4 from series limit, 20-1 long periods, 187, 189 Hydrogen atom, Bohr's theory, 10 electron orbits, 28 rare earths, 192, **74** short periods, 182-3 magnetic moment, 132 Iron, 59-61 mechanical moment, 11 magnetic moment, 132 wave mechanics, 15 Hydrogen spectrum, Balmei's series, 2, Iron frame elements, ground terms, 5, 13 compared with other frames, 70-4 fine structure, 40-3 paramagnetic ions, 140-3 series, 5 Irregular doublet law, 206 Stark effect, 145-51 Isoelectronic sequences, Moseley law Hyperfine structure, empirical, 166 203 - 5ıntensıtıes, 183 screening doublets, 206-8 isotope displacement, 187 spin doublets, 211–12 nuclear mass, 167 Isotope displacement, 187-97 Paschen Back effect, 173 vector model, 168 J, definition, 34 Zeeman effect, 173 orientation in magnetic field, 88, 129-Indium, 22-4 series limit, 159 absorption spectrum, 69-70 11 coupling, 28, 136-43 Inert gases, 36–41 intensities, 150 diamagnetism, 139 q factors, 146-7 Krypton, 39-44 intervals, 127 Inner quantum number, see J, 34 Landé's doublet formula, 212 Intensities, alkalı doublets, 107 Lanthanum, 50, 53 experimental, 90 q factors, 155 hyperfine, 183–7 Lead, 24-8 iron frame elements, 104

11 coupling, 150

fluorescence, 79

Lead (cont)	Mercury (cont)
isotope displacements, 197	ionised, 67
magnetic moment, 133	isotope displacements, 193-5
Lenard phosphores, 245	level diagram, 53
Level diagrams, optical, 11, 24	magnetic moment, 132
X-ray, 197-8	quadripole radiation, 222
Limit, calculation of series, 20	resonance radiation, 79
displaced, 3	Zeeman effect, 118
multiplet, 31, 42, 159	Molecules, symmetrical, 201-2
	Molybdenum, 57–8
Lithium, 18–39	intervals, 148–9
hyperfine structure, 166, 168	Moseley's law, optical, 199
level diagram, 25	X ray, 203-5
Moseley diagram, 204	Multiplets, 62
nucleus, 214	analysis, 48
series, 19	intensities, 94–9
Zeeman patterns, 105	Multiplicaties in iron row, 175
Long periods, analysis, 48	minimiphotos in 202 2000, 200
configurations, 48	Nebular lines, 217
ground terms, 45	Neodymum phosphores, 242
ındıvıdual spectra, 49–70	
ın periodic system, 183–7	Neon, 39-48
three rows compared, 70–4	absorption spectrum, 69
Lorentz umt, 84	hyperfine structure, 168
Lutecium, 50, 53	intervals of a terms, 134
hyperfine structure, 199	jj coupling, 141
	series limits, 43, 159-60
Magnesium, 46–58	Stark effect, 155
displaced terms, 6	Neutronic nuclei, 205, 212-13
intensities, 218	Neutrons in nucleus, 209-10
intervals, 150	Nickel, 63–5
ionised, 177	g factors, 155
Paschen Back effect, 115, 117	intensities, 105–6
Zeeman effect, 105, 119	magnetic moment, 134
Magnetic field, see Zeeman effect, 82	Stark effect, 158–60
Magnetic moment, of atoms, 132-4	Nitrogen, 28–32
of electrons, 96	inverted terms, 20
of ions, 135–43	level diagram, 29
	nebular lines, 218
of nucleus, 203  Magnetic splitting factor, atomic rays,	nucleus, 206–7, 214
	triplet limit, 32
131 3-6	Normal Zeeman triplet, 134
definition, 90	Notation in complex spectra, 4
sum law, 123	Nucleus, electric field of, 200
tabulated, 92–3, 100–1	magnetic moment of, 208-6
Magnetism, 187	spin of, 200
Manganese, 58-9	structure, 208
intensities, 100, 106	types of, 204-5, 208
Zeeman effect, 116	oy pos 62, 201 0, 201
Mass effect in hyperfine structure, 167	One line spectra, 76
Matching strong and weak terms, 118	Orbits, exclusion principle, 201
Mercury, 46-58	general atom, 26-8
absorption spectrum, 70-2	
displaced terms, 7	hydrogen, 10–13
excitation potentials, 75	Orbital vector, 26
forbidden line, 215	Oxygen, 33-5
hyperfine intervals, 197–9	auroral line, 216–17
hyperfine structure, 190-2	intensities, 101
intensities, 101–3	level diagram, 33

Potassium (cont) Oxygen (cont)  $g \text{ sum, K } \pi, 126$ magnetic moment, 134 nebular lines, 218 hyperfine structure, 207 Paschen-Back effect, 106, 115 magnetic moment, 132, 138 Moseley diagram, 205 Palladium, 63–5 quadripole line, 222-5 Palladium frame elements, 188 Stark effect, 178 Praseodymium phosphores, 238, 240, ground terms, 47 paramagnetism, 143 243 Paramagnetism, classical theory, 136-8 Principal series, 18 frame elements, 140-3 doublets, 31, 36 formula, 23 gases, 138 Langevin's theory, 127 triplets, 51, 55 rare earths, 138-40 Zeeman types, 83 Partial Paschen Back effect, 115 Protonic nuclei, 204, 210-12 intensities, 118-19 Protons in nucleus, 209–10 Paschen Back effect, empirical, 105 Quadripole radiation, forbidden lines, hyperfine structure, 173 intermediate fields, 117 invariance of g sum, 123 intensities, 227 invariance of  $\Gamma$  sum, 125 polarisation rule, 221 matching strong and weak terms, quantum mechanics, 219 selection rules, 220 119 partial effect, 115 Zeeman effect, 221 Quantum mechanics, hyperfine perquadripole, 225 turbation, 199 vector model, 111 Paschen-Back effect, 117 Penetrating orbits, 27 quadripole radiation, 219 Periodic system, 161–202 valency, 172 displacement law, 175 Zeeman effect, 97 electronic structures, 179 Quantum of action, 10 exclusion principle, 201 rare earths, 75 valency, 166 Radium, 46-58, 50 Rares ultimes, 120 Periodic table, 163, 165 Raman spectra, 228, 235 Perturbation, 150-7 Rare earths, 75-89 hyperfine, 197–8 Phosphores, chromium, 229 absorption spectra, 81 arc and spark spectra, 79 Lenard, 245 configurations, 190-2 rare earth, 236 in periodic system, 75 Phosphorescence, 228-9 ionisation potentials, 192 Phosphorus, 28–32 paramagnetism, 138 hyperfine structure, 207 phosphores, 236, 242-3 Photometry, 90 Platino-cyanides, 246 valency, 77 Regular doublets, 208 Platinum, 66 Platinum frame elements, 189 Resonance potentials, 72 ground terms, 47 Resonance radiation, 78 paramagnetism, 143 Rhenium, 59 Polarisation in, Paschen Back effect, Rhodium, 63 Rubidium, 18-39, 50 112-13electron impact, 78 quadripole radiation, 220 Stark effect, 148, 154 g sum, Rb II, 126 Zeeman effect, 112, 109 nucleus, 209 Russell-Saunders coupling, 3-5, 22 Potassium, 18-39, 50 deviations from, 122 displacement law, 178 electron impact, 78 Ruthemum, 59, 61 T sum, 132 forbidden lines, 215

Rydberg constant, 2	Sodium (cont)
for helium, 14	nuclear spin, 201
for hydrogen, 12	Paschen-Back effect, 115
for other atoms, 19	quadripole lines, 223-5
	Stark effect, 155
Samarium, 85–9	Zeeman patterns, 85
phosphores, 286-40, 243	Spark spectra, 46
valency, 78	Spectroscopic terms, 62
Scandium, 50–3	Spin doublets, 208
ionised, 178, 205	X-ray, 130
Screening, constant, 203	Spin of nucleus, 200
doublet, 206	Spinning electron, doublet series, 32
Selection rules, displaced terms, 4	Zeeman effect, 94
for $J$ , 57	Stark effect, 144–60
for L, 26	experimental, 144
Paschen Back, 112–13	forbidden lines, 215
quadripole, 220	ın crystals, 234
Stark, 148, 154	ın hydrogen, 145
X ray, 196	in other elements, 151
Zeeman, 89	Stationary states, 3, 10
Selenium, 33-5	Statistical weight of a term, 66
Self-reversal, 18, 69	Stripped atoms, 207
Serial number, 19, 23, 49	Strong field, 106
Series, 5, 18	Strontium, 46–58, <b>50</b>
	intensities, 102
formula, 18–21	
intensities, 104	perturbation, 157
limits, 10–11, 21, 158–65	Sulphur, 33–5
Sharp series, 18	Sum rules, g sum, 123
doublet, 31, 36	Γ sum, 126
formula, 21–3	intensity, 135
Stark effect, 158	Super multiplet, intensities, 101
triplet, 54–5	
Zeeman types, 83	Tellurium, 33–5
Short periods, 181–3	Temperature class, 49
deep terms, 14	Terbium, valency, 78
elements, 21	Terms, 3, 9, 11
ground terms, 16-18	Thallium, 22–4
irregularities, 22	absorption, 69-70
Silicon, 24–8	fluorescence, 79
doublet limit, 160	hyperfine structure, 172–89
ionised, 177	intensities, 108
level diagram, 25	isotope displacement, 194
Silver, 66-7	level diagram, 23
hyperfine structure, 207	magnetic moment, 132
magnetic moment, 130-2	nucleus, 206
Singlet spectra, 47	Tin, 24-8
Sodium, 18–39	magnetic moment, 133
	Titanium, 53–4
absorption spectrum, 68	
controlled electron impact, 77	g factors, 155
D lines in magnetic field, 106–10, 112–	I sum, 132
13	intensities, 101, 106
displacement law, 177	ionised, 178, 205
fluorescence, 79–81	Transition elements, 184
forbidden lines, 215	Triplet terms, 49
Landé's doublet formula, 215	Tungsten, 58
level diagram, 33	77 2 2 20
magnetic moment, 132	Uranyl salts, 241

Valency, 166-75
rare earths, 77
Vanadium, 54, 57
Vector model, alkali doublets, 29
combination of several electrons, 9
displaced terms, 3
general coupling, 135
hyperfine intervals, 199
hyperfine structure, 168, 172
hyperfine Zeeman effect, 173
interval rule, 65
jj coupling, 27-8
Paschen-Back effect, 111-12
Stark effect, 157
Zeeman effect, 88-9

Wave mechanics, 3 hydrogen atom, 15 hyperfine structure, 176, 179 Wave numbers, 5 Weak field, 106

X rays, 193-200, 228 spin doublets, 209-11, 130 Xenon, 39-43 Stark effect, 156-7 Ytterbium, phosphores, 236 valency, 78 Yttrium, 50, 53

Zeeman effect, 82-104 analysis, 99 anomalous types, 85 hyperfine, 173 intensities, 98, 108-20 magnetic splitting factors, 92-3, 100-1 normal triplet, 82 quadripole, 221 quantum theory, 86 spinning electron, 94 unresolved patterns, 106 Zmc, 46-58, 67 displaced terms, 7 Lande's doublet formula, 215 magnetic moment, 132 Zu conium, 53-4 doublet limit, 161 g factors, 154, 156 intensities, 106



## AUTHOR INDEX

Numbers in Clarendon refer to the second volume

Aston, F W, 188, 208 Bacher, R F, short periods, 44, long periods, 74, hyperfine structure, 173, 199 Back, E., Paschen-Back effect, 104-6, 115-18, 126, g factors, 147, hyper fine structure, 169, 178, 180, 187 Bakker, C J, halogens, 36, g sum, 125, quadripole Zeeman effect, 222-6 Balmer, J J, 2, 5 Barratt, S, 220 Bartlett, J H, 150 Bear, R. S, 85, 88-9 Bechert, K , 150 Becker, F , 217, 227 Becquerel, J, 82-3 Blair, H A, 104, 125 Blaton, J , 227 Bohr, N, 3, H atom 10f, He 10n, 14, selection rule, 89, Stark effect, 157, periodic table, 163-4, 180-91, rare earths, 75, 79 Boltzmann, L., 2, 70, 85, 234 Born, M , 175, 202 Bourland, L T, 143 Bowen, I S, doublet laws, 204, 207, 212, nebular lines, 217-19 Boyce, J C, nitrogen, 20, nebular lines, 217-19 Brackett, F S, 7 Bragg, W H, 202 Bragg, W L, 202 Breit, G, matching terms, 120, isotope displacements, 194-7, nuclear spin, 201 Brickwedde, F G, 167 Bruck, H , 170-1 Bryden, S D, 209 Buoma, T , 106 Burger, H C, helium, 60, intensities, 101-4, Zeeman intensities, 108-10, photometry, 121

Albertson, W, 79

Arnot, F L, 81

Allen, J S V, 106 Altschuler, S, 213

Andrade, E N da C, 69, 78, 81

Cabannes, J, 228 Cabrera, P, 139 Campbell, J S, 84, 221 Capel, W H, 139 Carter, N M, 27, 216 Casımır, H , 199, 200 Chalk, L , 149, 150 Charola, F, 80 Chenault, R L, 8 Coelingh, M, 102 Cohen, V W, 131, 200-1 Compton, K T, 20 Cotton, A, 84 Condon, E U, 158-9 Crookes, W, 236 Curie, S , 127 Curtis, W E, 7

Dadieu, A, 228 Darwin, C G, Paschen Back effect, 117, quantum mechanics, 211, Paschen-Back intensities, 118 Darwin, K , 109-10 Datta, S , 215 Davis, B , 74-5 de Boer, J H, 167, 172, 202 de Broglie, L, 15 de Brum, T L, 36, 125 de Gramont, A , 120 de Haas, W J, 139 Dennison, D M, 200 Deutschbein, O, rare earths, 83, chrome phosphores, 230-5 Dewar, J, 2 Dickinson, R G, 201 Dijkstra, H , 147 Dirac, P A M, 93 Dobson, G M B, 90 Dorgelo, H B, 91-3, 109 du Bois, H, 285

Eastman, E D, 209
Eckart, C, 167
Ehrenfest, P, 82
Ehas, G J, 285
Ehason, A Y, 95, 150
Epstein, P S, 147
Evans, E J, 14, 168
Evans, S F, 142

Evert, H, 240 Eymers, J G, 102

Fagerberg, S, 240 Fermi, E , 108, 203–7 Ferschmin, A , 40 Filippov, A , 107 Fisher, R A, 104 Foote, P D, 215, 8 Fortrat, R, 68 Foster, J S , 149-51, 155 Fowler, A, helium, 14, series laws, 21, doublet series, 31, Moseley's law, 205, carbon, 28 Fowler, H W, 27, 216 Franck, J , 76, 81 Frank, A , 139 Fraser, R G J, 129-30, 143 Fraunhofer, J, 68 Frayne, J G , 218-19 Freed, S , 139, 83-5 Frerichs, R, intensities, 106, 121, auroral line, 221 Fridrichson, J, 76 Frisch, S, 40

Fuchtbauer, C, 71, 107

Gale, H G, 15

Gebauer, R, 145 Gehrcke, E , 84 Gerlach, W , 129, 132–3, 138 Gibbons, J J, 197 Gibbs, R C,  $H_{\alpha}$ , 43, He atom, 61, doublet laws, 208, 212-16, f elec trons, 14, cerium, 80 Gotze, R , 23, 1 Goucher, F S, 74-5 Goudsmit, S A, spinning electron, 32-4, fine structure of hydrogen, 40-5, He atom, 58, Paschen Back effect, 111, doublet laws, 209-10, 216, short periods, 44, long periods, 74, combination of electrons, 20, q, 126, 143, Γ sum, 180-2, jj coupling, 142, perturbation, 156, hyperfine structure, 169, 173, 180, 199, nuclear moments, 208-7, rare earth phosphores, 240 Grace, N S, 43, 197

Granath, L P, 168 Grebe, L, 197 Green, J B, Paschen-Back effect, 117, doublet laws, 216, perturbation, 155, hyperfine structure, 175-7,

183-6 Griffith, I O, 90, 121 Grotrian, W, hydrogen, 40, hehum, 40, 58, aluminium, 68, indium, 70, Stark effect, 155, Moseley diagrams, 205, nebular lines, 217, 227 Guthrie, A. N., 143

Haberlandt, H, 236
Hansen, G, helium, 41, 60, hyperfine structure, 168
Harkness, H W, 156, 160
Harrison, D N, photometry, 90, 121
Harrison, G R, intensities, 106, 135
Heard, J F, 156, 160
Heisenberg, W, hydrogen, 40, helium, 61, Paschen-Back effect, 117, 120,

intensities, 91, 111, nuclear struc-

ture, 209
Heitler, W, 174
Hellmann, H, 202
Herhhy, J, 108
Hertz, G, 69, 76, 206
Hesthal, C E, 106
Hevesy, G v, 75, 81, 89
Hill, E L, 185
Hiyama, S, 145
Hoag, J B, 15
Honl, H, 93, 111
Hopfield, J J, 35

Hopfield, J J, 35
Houston, W V, hydrogen, 41-3,
helium, 60, Lorentz unit, 84, perturbed g factors, 155, 178, quadripole radiation, 215, 219, 226

Howes, H L, 241
Hsieh, Y M, 43
Hubner, H J, 107
Huff, L D, 215, 226
Hughes, D S, 167-8

Hund, F, electronic structures, 193, energy rules, 15, combination of electrons, 20, short periods, 24–86, 44, mert gases, 42, long periods, 74, series limit, 160–3

Idel, S, 200, 206
Inglis, D R, perturbed, terms, 156, nucleus, 210, 212, 214
Ishida, Y, 145
Iwama, T, 147

Jack, R, 102
Jackson, D A, 207
Janes, R B, 143
Jantsch, G, 236
Jenkms, H G, 120
Jevons, W, 174, 202, 201
Jog, D S, 28
Johnson, M H, 106, 135

Iwanenko, D , 210

Jones, E G, 197-8, 207 Joos, G, 107, 232 Jordan, P , hydrogen, 40, energy levels, 81, Paschen Back effect, 117, 120, Zeeman intensities, 111

Kaha, P N, 79 Kallmann, H, hyperfine structure, 194-6, 210, 214 Karlık, B , 236 Karlson, P, 79 Kassner, L, 147 Kast, W , 157 Kayser, H , 214 Kellogg, J M B, 201 Kent, N A, 41 Keyston, J E, 171, 185-91, 193 Kiess, C. C., q factors, 90, 100, zirconium, 106, perturbation, 154, series limit, 161 Kless, H K, 106, 154 King, A S, 46, 49, 79 Klemm, W, 236 Koch, J, 151 Kohlrausch, K W F, 228 Kohn, H , 107 Kossell, W, 169, 176, 186 Kramers, H A, 147, 154 Kromer, E, 125 Kronig, R de L, intensities, 93, 104, 150, Zeeman intensities, 111 Kruger, P G, 61 Kuhn, H , 207

Kurt, E 0, 134 Ladenburg, R, 71, 155 Lande, A, selection rule, 57, interval rule, 63, q factors, 90, Zeeman effect, 104,  $\Gamma$  sum, 125, doublet formula, 212, oxygen, 35, neon, 41, g sum, 125, nucleus, 210-14 Lang, R J, 80, 161 Langer, R M, 152 Langevin, P , 127

Langstroth, G O, 135, 156 Laporte, O, interval rule, 64, paramagnetic ions, 141, raies ultimes, 121, g sum, 126, perturbation, 156, selection rule, 220, rare earth phosphores, 240 Lenard, P, 73, 246

Leu, A, 132-3 Lewis, G N, 170 Liveing, G D, 2 London, F, 174 Lorentz, H A, 82, 84 Loring, R A, 155

ij

Lo Surdo, A, 145 Lyman, T, 7, 58, 39

McLeod, J H, 221

McLennan, J C, 35, 216, 221

Mack, J E , 162 Masaki, O, 40 Meggers, W F, q factors, 90, 100, mtensities, 104, raies ultimes, 121, g sum, 125,  $\Gamma$  sum, 132, forbidden lines, 215

Meissner, K W, caesium, 38, rubidium, 40, neon, 69, atomic rays, 130

Mendeléeff, D, 162, 165 Mensing, L, 117 Metcalfe, E P, 70 Meyer, S, 139 Milianczuk, B, 225 Miller, G R , 126

Millikan, R A, doublet laws, 204, 207

212, displaced terms, 6 Minkowski, R , 147, 160 Mishima, T , 168 Mitchell, A. C. G., 81 Mohler, F L, 79, 215 Moll, W J H, 121 More, K R, 197 Moseley, H G J, 199, 203 Mrozowski, S., 192 Mulliken, R S, 174 Murakawa, K , 147 Murphy, E J, 167

Nagaoka, H, 168 Newman, F H, 77 Nichols, E L, 241 Nutting, G C, 84, 232

Ornstein, L S, intensities, 101-4, 106, Zeeman intensities, 108-10, photometry, **121** 

Paschen, F, hydrogen, 7, serial numbers, 23, hehum, 45, 58, Paschen-Back effect, 105-6, 115, oxygen, 35, neon, 39, 42, perturbed series, 151

Pauli, W, matching terms, 119, q sum, 124, Stark effect, 158, exclusion principle, 201, g sum, 125, hyperfine structure, 166, 168

Pauling, L, doublet laws, 209, 216, combination of electrons, 20, \( \Gamma\) sum, 132, jj coupling, 142

Pearson, H, 41 Pfluger, A, 71 Pfund, A H, 7 Phipps, T E , 134
Piccardi, G , 192, 75
Pickering, W H , 14
Placzek, G , 228
Planck, M , 10
Poetker, A H , 7
Pogány, B , 42, 145-7
Preston, T , 85, 105
Pringsheim, P , absorption spectra, 69, 78, 81, fluorescence, 241, 244-6
Przibram, K , 236

Rabi, I I, atomic rays, 129, 131, 143, nuclear spin, 200-1 Raman, C V, 228 Ramb, R, 40 Ramsauer, G, 155 Rasetti, F, 107-8, 220 Rawlins, F I G, 232 Rayleigh, Lord, 80-1, 215 Ritz, W , 3, 21, 24 Rolla, L, 192, 75 Roschdostwenski, D, 107-8 Rosenthal, A H, 36 Rowles, W, 155 Ruark, A E, 180, 202 Rubinowicz, A., 89, 227 Ruedy, J E, 221 Rumer, G, 174 Rump, W, 79 Runge, C, 58, 85, 214 Russell, H N, series laws, 21, notation. 34, unresolved patterns, 104, matching terms, 120, xenon, 158, displaced terms, 1, 5, notation, 4, combination of electrons, 10, euro-

Rydberg, J. R., Rydberg constant, 2, series formula, 18, combination principle, 21, 24 Ryde, J. W., 120

pium, 79, intensities, 93, 104-5,

g sum, 125,  $\Gamma$  sum, 132, perturbed

Ryde, J. W , 120 Ryde, N , 156

series, 151, 154

Saha, N K, 83
Sømbursky, S, 108
Sauer, H, 232-3
Saunders, F A, 1, 5, 39
Sawyer, R A, 7, 126, 151
Scheffers, H, 130
Schlapp, R, 151
Schmidt, T, isotope displacements, 195, hyperfine structure interval rule, 199, nuclear structure 209, fluorescence, 246

Schnetzler, K, 232
Schrodinger, E, 149
Schuler, H, hyperfine structure, lithium, 166, vector model, 170-1, intensities, 185-7, isotope displacement, 189-97, perturbation, 197-9, nucleus, 204-5, 209-10, 213-14
Schuster, A, 2
Scribner, B F, 121
Segré, E, nuclear moments, 203-7, quadripole radiation, 222-6
Selwyn, E W H, 205

Selwyn, E W H, 205 Seward, R S, 106 Sexl, T, 200 Shane, C S, 15, 43

Shenstone, A. G., unresolved patterns, 104, notation, 34,4, inverted terms, 19, g sum, 125, I sum, 132, per turbation, 151, 154-5, series limit, 161

Sherman, A, 202 Shrum, G M, 27, 216 Sidgwick, N V, 167, 172, 202 Siegbahn, M, 200, 202, 228 Slater, J C, 58, 174, 130 Smith, D M, 120 Snow, C P, 232 Sommer, L A, 221

Sommerfeld, A, intensity rule, 35, H I and He II, 40-5, Paschen-Back effect, 115, matching terms, 119; paramagnetism, 141, displacement law, 176, doublet laws, 210-11, 216, intensities, 91-3

Sowerby, A L M, 220

Spedding, F H, H<sub>a</sub>, 15, 43, paramagnetism, 139, rare earths, 83-9, chromium compounds, 232-4, rare earth phosphores, 238

Spencer, J E, 89 Stark, J, 144-5, 150, 160 Stern, O, 129, 132, 210 Stevenson, A F, 220 Stokes, G G, 229 Stoner, E C, 136, 143 Stoney, G J, 2

Takamme, T, 158-9, 8
Tamm, I, 218
Taylor, J B, 132
Taylor, L B, 41
Temple, G, 209
Terenin, A, 80
Terrien, J, 147
Thomas, E, 168
Thornton, R L, 149

Tomaschek, R, rare earths, 83, fluor escence, 242-3, 246, rare earth phosphores, 236-40
Traubenberg, H, R, v, 145
Turner, L, A, 34, 4
Twyman, F, 120

Uhlenbeck, G. E., spinning electron, 32, H r and He II, 40-5, helium, 58, doublet laws, 210, g factor, 143 Unsold, A., 45 Ulbain, G., 236 Urey, H. C., periodic system, 180, 202, combination of electrons, 20, hyperfine structure, 167

Van Arkel, A E, 167, 172, 202 Van Geel, W C, 117, 110, 116-21 Van Lohuizen, T, 87 Van Vleck, J H, 138-9, 143, 202 Van Wijk, W R, 101 Venkatesachar, B, 70 Voigt, W, 105-6, 108, 117 von Baeyer, A, 84

Weiss, P, 84

Wentzel, G , 196, 5 West, G D, 15 Weyl, A , 174 Whiddington, R, 13 White, H E, doublet laws, 208, 212, 216, combination of electrons, 14, cerium, 80, intensities, 95, 150, perturbation, 151, series limit, 163 Whitford, A E, 126 Wick, F G, 244 Wiersma, E C, 139 Wilber, D T, 14 Williams, J H , 43 Williams, S E, 108 Wolff, H W, 107 Wood, R W, 68, 79, 228 Wrede, E , 132 Wulff, J, hyperfine structure, 175-8, 183-7

Zacharias, J. R., 201
Zahrahmicek, J., 211
Zeeman, P., Zeeman effect, 82, 104, aluminium, 36, hyperfine structure, 169, 180
Zemansky, M. W., 81